

On Semi pre-generalized-closed sets

Marwah Munther Hassan

College of Education for Pure Sciences, Wasit University, Iraq

Marwamontherhassen1994@gmail.com

Ali Khalaf Hussain

College of Education for Pure Sciences, Wasit University, Iraq

alhachamia@uowasit.edu.iq

Abstract:- In this paper, a new class of *generalized – closed sets* called *semi pre – generalized – closed sets* in *topological spaces* are introduced and studied. Also some of their properties have been investigated. We also introduce *sp – T1/2 space*, *submaximal space*, and studied the relationship between *spg – closed set* and some space in *topological spaces* as well discuss some properties, theorem, corollary and examples.

Keywords: *sp – closed set*, *sp – T1/2 space*, *submaximal space*, *spg – closed set*.

1 Introduction

The concepts of *semi – open sets* were introduced and studied by Levin [1] in 1963, and in 1970, Levin [2] began and studied *generalized closed sets* and *generalized open sets* as a *generalization* of *closed sets* and *open sets*. Dunham [3] came up with the concept of *generalized closure* using Levine *generalized closed sets* and explained their properties. The investigation of *generalized closed sets* has led to many interesting concepts in topology. Recently, topologists have studied diverse and closed *generalized sets* in *topological spaces*. In 1982, Mashhour, Abdul-Moncef and Deeb [4] identified *conquest pre – sets* and *pre – continuous functions*. The class of previously *generalized closed sets* that were used to obtain properties of *pre – T1/2 spaces* was introduced by Maki, Umehara and Noiri [5] in 1996. In 1986, D. Andrijevic [6] studied *semi – open sets* in *topology*. Later, many authors studied these previously *semi – open sets* and *semi – closed* and *generalized continuous functions*. In 1995, Dontchev [7] identified *generalized semi – open sets*. Mackey introduced the concepts of *pg – closed sets* and *gp – closed sets* in a similar way in [8]. These concepts are *generalizations* of *closed sets* and have been studied by Dontchev and Maki [9] leading to a new decomposition of *pre – continuity*. In this paper, our goal is to introduce new types of *generalized sets* in the *topological space* called *semi pre – generalized – closed sets* and study the relationship between them and some *sets* in the *topological space* and verify their basic properties.

2 Preliminaries

Definition 2.1

Let (X, T) be a topological space, A subset B of X is called:

1. *Semi – open set* (briefly, *s – open*) if there is an *open set* V in X such that $V \subseteq B \subseteq \overline{V}$, the complement of *semi – open set* is *semi – closed set* (briefly, *s – closed*).[10]
2. *pre – open* or *locally dense set* (briefly, *p – open*) if $B \subseteq (\overline{B})^o$, the family of all *pre – open sets* in a space X is denoted by $P.O. (X)$ and the complement of *pre – open set* is a *pre – closed set* and denoted by $P.C.(X)$.[11]
3. *Semi pre – open set* (briefly, *sp – open*) if $B \subseteq \overline{((\overline{B})^o)}$, The complement of *semi pre – open set* is a *semi pre – closed set* (briefly, *sp – closed*) and represent that $((\overline{B}^o))^o \subseteq B$.[12]
4. *generalized – open set* (briefly, *g – open*) if $\overline{B} \subseteq V$, whenever $B \subseteq V$ and V is a closed set. The complement of *g – open set* is a *generalized – closed set* (briefly, *g – closed*).[13]

Remark 2.2

1. Every *closed set (open set)* is a *s – closed (s – open)* set, but the converse does not necessary to be true.[10]
2. Every *closed set (open set)* is a *p – closed (p – open)* set, but the converse does not necessary to be true.[11]
3. Every *closed set (open set)* is a *sp – closed (sp – open)* set, but the converse does not necessary to be true.[12]
4. Every *closed set (open set)* is a *g – closed (g – open)* set, but the converse does not necessary to be true.[13]

Remark 2.3

1. The intersection of all *s – closed subsets* of X which is containing B is said to be a *s – closure* of B and it is denoted by \overline{B}^s .[10]
2. The intersection of all *p – closed subsets* of X which is containing B is said to be a *p – closure* of B and it is denoted by \overline{B}^p .[14]

3. The intersection of all sp – closed subsets of X which is containing B is said to be a sp – closure of B and is denoted by \overline{B}^{sp} . [12]

4. We can write the relationship between p – closure of B , sp – closure of B and closure of B : $\overline{B}^{sp} \subseteq \overline{B}^p \subseteq \overline{B}$. [12]

Corollary 2.4

Let (X, T) be a topological space and let $B, C \subseteq X$, if $B \subseteq C$ then $\overline{(B)}^{sp} \subseteq \overline{(C)}^{sp}$. [16]

Theorem 2.5

Let (X, T) be a topological space, $B \subseteq X$ then B is a semi pre – closed set if and only if $B = \overline{(B)}^{sp}$. [16]

Proof:

Let B be a sp – closed subset of X

It is clear that $B \subseteq \overline{(B)}^{sp}$ (1) [2.2(3)]

Since B is a sp – closed set

So $\overline{(B)}^{sp} \subseteq B$ (2)

From (1) and (2) we get $\overline{(B)}^{sp} = B$

Conversely

Suppose that $\overline{(B)}^{sp} = B$

Since $\overline{(B)}^{sp}$ is a sp – closed set

So B is a semi pre – closed set.

Theorem 2.6

Let (X, T) be a topological space, the singleton $\{x\}$ is an open set or semi pre – close set. [12]

Proof :

Let $x \subseteq X$

So $\{x\} \subseteq X$ is singleton set

So either $\{x\}^o = \emptyset$ or $\{x\}^o \neq \emptyset$

If $\{x\}^o = \emptyset$ then $\overline{(\{x\}^o)} = \emptyset$ and $\overline{(\overline{(\{x\}^o)})}^o = \emptyset$

Therefore $\overline{(\overline{(\{x\}^o)})}^o \subseteq \{x\}$

Hence $\{x\}$ is a *sp – closed set*

If $\{x\}^o \neq \emptyset$

Then $\{x\}^o = \{x\}$

Hence $\{x\}$ is an *open set*.

Theorem 2.7

Let (X, T) be a *topological space* and let $B \subseteq X$ then B is the intersection of *s – open set* with *dense set* if B is a *sp – open set*. [17-22]

Proof :

Suppose that $B = C \cap H$ such that C is a *s – open set* and H is *dense set* such that

$$\overline{(B)}^s = \overline{(C)}^s. \text{ And since } B \subseteq C \subseteq \overline{(C)}^s = \overline{(B)}^s$$

$$\text{So } B \subseteq C \subseteq \overline{(B)}^s$$

Hence B is a *sp – open set*.

Definition 2.8

Let (X, T) be a *topological space* and let $B \subseteq X$ then the set B is called *semi pre general ized – closed set (semi pre – generalized – open)* if $\overline{(B)}^{sp} \subseteq V$ whenever $B \subseteq V$ and V is a *semi pre – open set (semi pre – closed)* in X and denoted by *spg – closed (spg – open)* set.

Example 2.9

Let $X = \{1, 2, 3, 4, 5\}$ and let $T = \{X, \emptyset, \{1\}, \{3, 4\}, \{1, 3, 4\}\}$ be a *topological defined* on X .

Let $B = \{2, 5\}$ and $C = \{3, 4\}$ be a *subset* of X

It is clear that B is a *spg – closed set*

since the *semi pre – open* which contain B is:

$X, \{2,3,5\}, \{2,4,5\}, \{1,2,4,5\}, \{2,3,4,5\}, \{1,2,3,5\}, \{1,2,5\}, \{2,5\}$ and also, it contains $\overline{(B)}^{sp} = \{2,5\}$

and C is a *spg – open set* since the *semi pre – closed set* which contain C is:

$X, \{3,4\}, \{2,3,4,5\}, \{1,3,4\}$ and it contains $\overline{(C)}^{sp} = \{3,4\}$

Remark 2.10

Every *closed set (open set)* is a *spg – closed set (spg – open)*, but the converse does not necessarily to be true for example:

Example 2.11

Let $X = \{1,2,3,4,5\}$ and let $T = \{X, \emptyset, \{1\}, \{3,4\}, \{1,3,4\}\}$ be a *topological* defined on X .

Let $B = \{1,2,5\}$ and $C = \{3\}$ be a *subset* of X .

So B is a *spg – closed set* but it is not *closed set* and C is a *spg – open set* but it is not *open set*.

Proposition 2.12

Let (X, T) be a *topological space* and let $B \subseteq X$ then B is a *spg – closed set* if B is a *pg – closed set*.

Proof:

Let X be a *topological space*

And let V is a *p – open set* in X

Such that $(\overline{B}^p) \subseteq V$ whenever $B \subseteq V$

So B is a *pg – closed set*

Since every *p – open set* is a *sp – open set*

So V is *sp-open set*

And since $\overline{(B)}^{sp} \subseteq (\overline{B}^p)$ and $(\overline{B}^p) \subseteq V$

So $\overline{(B)}^{sp} \subseteq V$ whenever $B \subseteq V$

So B is a *spg – closed set*.

Proposition 2.13

Let (X, T) be a *topological space* and let B be a *subset* of X then B is a *spg – closed set* if B is a *sp – open set* and *pg – closed set*.

Proof:

Let (X, T) be a *topological space*

And let B be an *open set* in X

So B is a *p – open set* in X

Since every *p – open set* is *sp – open set*

So B is a *sp – open set* in X

Hence B is a *sp – open set*

let V be an *open set* in X such that $\overline{(B)} \subseteq V$ whenever $B \subseteq V$

Since every *open set* is *p – open set*

So V is a *p – open set*

And since $(\overline{B}^p) \subseteq \overline{(B)}$ [2.2 (4)]

So $(\overline{B}^p) \subseteq \overline{(B)} \subseteq V$

Hence $(\overline{B}^p) \subseteq V$ whenever $B \subseteq V$ and V is *p-open set*

Since every *p-open set* is *sp-open set*

So V is *sp-open set* in X

Therefore $(\overline{B}^p) \subseteq V$ whenever $B \subseteq V$ and V is a *sp – open set*

And since $\overline{(B)}^{sp} \subseteq (\overline{B}^p) \subseteq V$ [2.2 (4)]

So $\overline{(B)}^{sp} \subseteq V$ whenever $B \subseteq V$ and V is a *sp – open set*

Hence B is a *spg – closed set*.

Proposition 2.14

Let (X, T) be a *topological space* and let $B \subseteq X$ if B is a *sp – closed set* then B is a *spg – closed set*.

Proof:

Suppose that B is a *sp – closed set* in X

And let V is a *sp – open set* in X such that $B \subseteq V$

Since B is a sp – closed set, so $\overline{(B)}^{sp} = B$ [2.5]

Hence $\overline{(B)}^{sp} \subseteq V$

So B is a spg – closed.

Definition 2.15

Let (X, T) be a topological space, then X is a semi pre – $T_{1/2}$ space if:

- 1) every spg – closed set in X be a semi pre – closed set.
- 2) every singleton be a semi pre – closed set or semi pre – open.

Remark 2.16

In definition (2.15) (1) and (2) are equivalent.

Proof:

Suppose that (1) is a verified

We will prove (2)

Let X be a semi pre – $T_{1/2}$ space and $x \in X$

Let $\{x\}$ is not sp – closed set

So $B = X - \{x\}$ is not sp – open set

Hence X is a sp – open set which contain B and also $\overline{(B)}^{sp} \subseteq X$

So B is a spg – closed set

And by definition [(2.15) (1)], so B is a sp – closed set

Hence $\{x\}$ is a sp – open set

And to proof conversely suppose that definition [(2.15) (2)] is verified.

Assume that $B \subseteq X$ be a spg – closed set

We will prove that B is a sp – closed set

That means $\overline{(B)}^{sp} = B$

It is clear that $B \subseteq \overline{(B)}^{sp} \dots (*)$

Suppose that $x \notin B$ and $x \in \overline{(B)}^{sp}$

So $B \subseteq X - \{x\}$

And by definition [(2.15) (2)] then $\{x\}$ is a sp – open set or sp – closed set.

So if $\{x\}$ is a *sp – open set*

Then $X - \{x\}$ is a *sp – closed set*

Since $B \subseteq X - \{x\}$, then $\overline{(B)}^{sp} \subseteq \overline{(X - \{x\})}^{sp}$ [2.4]

Hence $\overline{(B)}^{sp} \subseteq X - \{x\}$

And since $x \in \overline{(B)}^{sp} \subseteq X - \{x\}$, this means $x \in X - \{x\}$ and this is contradiction

So $x \in B$ and hence $\overline{(B)}^{sp} \subseteq B$... (**)

From (*) and (**) we get $\overline{(B)}^{sp} = B$

Hence B is a *sp – closed set*

Either if $\{x\}$ *sp – closed set*

Then $X - \{x\}$ is a *sp – open set*

And since $B \subseteq X - \{x\}$ and B is a *spg – closed set*

So $\overline{(B)}^{sp} \subseteq X - \{x\}$

And since $x \in \overline{(B)}^{sp} \subseteq X - \{x\}$, this means $x \in X - \{x\}$ and this is contradiction

So $x \in B$ and hence $\overline{(B)}^{sp} \subseteq B$... (***)

And from (*) and (***) we get $\overline{(B)}^{sp} = B$

Hence B is a *sp – closed set*.

From theorem 2.6 and definition 2.15(2) and remark 2.2(3) we get the following corollary:

Corollary 2.17

Every *topological space* be a *semi pre – $T_{1/2}$ – space*.

From this corollary and definition 2.15(1) and proposition 2.14 we can be writing the relationship between *spg – closed set* as we will explain it through the following corollary:

Corollary 2.18

Let (X, T) be a *topological space* and let $B \subseteq X$ then B is a *spg – closed set* if and only if B is a *sp – closed set*.

Definition 2.19 [15]

Let (X, T) be a *topological space*, we say that X is a *submaximal space* if every *dense set* in X is an *open set*, we can prove that X is a *submaximal space* if and only if each *sp – open set* in X is an *open set*.

Theorem 2.20

Let (X, T) be a *topological space*, then X is a *submaximal space* if every *dense set* in X is an *open set*.

Proof:

Suppose that (X, T) be a *topological space*

And let $B \subseteq X$ such that B is a *sp – open set*

So $B = C \cap D$ such that D is a *denes set* and C is an *open set* [2.7]

Since X is a *submaximal space* then D is an *open set*

Thus B is an *open set*.

Conversely

Assume that B is a *denes set* in X

So $B \subseteq (X)^o$

Since B is a *denes set*, so $\overline{B} = X$

Hence $B \subseteq (\overline{B})^o$

$(\overline{B}) \subseteq ((\overline{B})^o)$

So B is a *sp – open set*

And by assumption B is an *open set*

Hence X is a *submaximal space*.

Proposition 2.21

Let (X, T) be a *submaximal space*, then every *sp – closed set* in X is a *closed set*.

Proof:

Let $B \subseteq X$ is a *sp – closed set*

Then B^c is a *sp – open set*

And since X be a *submaximal space*

So B^c is an *open set* [2.20]

Hence B is a *closed set*.

Through the corollary 2.18 we clarify the relationship between *spg – closed set* and *sp – closed set* and from the above proposition 2.21 we can get the following result:

Corollary 2.22

Let (X, T) be a *submaximal space*, then every *spg – closed set* in X be a *closed set*.

Remark 2.23

The intersection of two of *spg – closed sets* is a *spg – closed set*, as we will explain for the following theorem:

Theorem 2.24

Let (X, T) be a *topological space*, and let B, C are a *spg – closed set* then $B \cap C$ be a *spg – closed set* in X .

Proof:

Since B is a *spg – closed set*

So, for every *sp – open set* V in X

Then if $B \subseteq V$ then $\overline{(B)}^{sp} \subseteq V$

And also, for C if $C \subseteq V$ then $\overline{(C)}^{sp} \subseteq V$

Suppose that $B \cap C \subseteq V$

We will prove that $\overline{(B \cap C)}^{sp} \subseteq V$

Since $B \cap C \subseteq V$ so $B \subseteq V \cup C^c$

So V is a *sp – open set* and C^c is a *spg – open set*

Also which is a *sp – open set* [2.18]

So $V \cup C^c$ is a *sp – open set*

And since B is a *spg – closed set* and $B \subseteq V \cup C^c$

So $\overline{(B)}^{sp} \subseteq V \cup C^c$

And in the same way we can prove that $\overline{(C)}^{sp} \subseteq V \cup B^c$

Since $\overline{(B \cap C)}^{sp} \subseteq \overline{B}^{sp} \cap \overline{C}^{sp}$ [2.2(4)]

So $\overline{(B \cap C)}^{sp} \subseteq (V \cup C^c) \cup (V \cup B^c)$

Suppose that $x \in \overline{(B \cap C)}^{sp}$

So $x \in (V \cup C^c)$ and $x \in (V \cup B^c)$

So $x \in V$

Hence $\overline{(B \cap C)}^{sp} \subseteq V$

So $B \cap C$ is a *spg – closed set*.

Remark 2.25

The union of two *spg – closed set* does not necessarily to be *spg – closed set* for example:

Example 2.26

Let $X = \{1,2,3,4,5\}$ and let $T = \{X, \emptyset, \{1,3,4\}\}$ be a *topological* defined on X .

And let $B = \{1,3\}$ and $C = \{3,4\}$

So, the *sp – open sets* which contain B and C is: $X, \{1,3,4\}$ and also contain \overline{B}^{sp} and \overline{C}^{sp} .

Hence each of B and C are a *spg – closed set* and since $B \cup C = \{1,3,4\}$

So $\overline{(B \cup C)}^{sp} = X$

Hence $B \cup C \subseteq \{1,3,4\}$ and $\overline{(B \cup C)}^{sp} \not\subseteq \{1,3,4\}$

So $B \cup C$ is not *spg – closed set*.

Theorem 2.27

Let (X, T) be a *topological space* and let $B \subseteq X$ is a *spg – closed set* and $C \subseteq X$ is a *closed set* then $B \cup C$ is a *spg – closed set*.

Proof:

Suppose that B is a *spg – closed set* and C is a *closed set* in X

We will prove that $B \cup C$ is a *closed set*

Let W be a *sp – open set* in X such that $B \cup C \subseteq W$

We will prove that $\overline{(B \cup C)}^{sp} \subseteq W$

Suppose that $x \in \overline{(B \cup C)}^{sp}$

Since $\overline{(B \cup C)}^{sp} = (B \cup C) \cup (\overline{((B \cup C)^o)})^o$ [15]

So $x \in (B \cup C) \cup (\overline{((B \cup C)^o)})^o$

So $x \in (B \cup C)$

Hence $\overline{(B \cup C)}^{sp} \subseteq B \cup C$

But $B \cup C \subseteq W$ [by assumption]

So $\overline{(B \cup C)}^{sp} \subseteq W$, hence $B \cup C$ is a *spg – closed set*

Or $x \in (\overline{((B \cup C)^o)})^o$

We will prove that $(\overline{((B \cup C)^o)})^o \subseteq B \cup C$

Since B is a *spg – closed set*

So B is a *sp – closed set*

Hence $(\overline{(B^o)})^o \subseteq B$

And since C is a *closed set*, so $C = \overline{C}$ [16]

So $(\overline{(B^o)})^o \cup \overline{C} \subseteq B \cup C$

But $(\overline{((B \cup C)^o)})^o \subseteq (\overline{(B^o)})^o \cup \overline{C} \subseteq B \cup C$

Since $x \in (\overline{((B \cup C)^o)})^o$

So $x \in B \cup C$

Hence $\overline{(B \cup C)}^{sp} \subseteq B \cup C$

Since $B \cup C \subseteq W$

So $\overline{(B \cup C)}^{sp} \subseteq W$

Thus $B \cup C$ is a *spg – closet set*.

Proposition 2.28

Let (X, T) be a *topological space*, and let B is a *spg – closed set* in X , if $B \subseteq C \subseteq \overline{(B)}^{sp}$ then C is a *spg – closed set* in X .

Proof:

Suppose that $C \subseteq V$ such that V is a *sp – open set* in X

We will prove that $\overline{(C)}^{sp} \subseteq V$

Since $C \subseteq V$ so $B \subseteq V$ [by assumption $B \subseteq C$]

And also B is a *spg – closed set* in X

So $\overline{(B)}^{sp} \subseteq V$

And since $C \subseteq \overline{(B)}^{sp}$

So $\overline{(C)}^{sp} \subseteq \overline{(B)}^{sp}$ [2.4]

Hence $\overline{(C)}^{sp} \subseteq V$

So C is a *spg – closed set*.

Through the remark 2.25 we clarify the union of two *spg – closed set* is not necessarily *spg – closed set*.

As for the *spg – open set*, this is true as we will show from the following corollary:

Corollary 2.29

Let (X, T) be a topological space, and let each of B, C are a *spg – open sets* in X then $B \cup C$ is a *spg – open set* in X .

proof:

let B, C are a *spg – open set* in X

So B^c, C^c are a *spg – closed set* in X

Hence $B^c \cap C^c$ is a *spg – closed set* in X [2.24]

So $(B^c \cap C^c)^c$ is a *spg – open set* in X

Hence $B \cup C$ is a *spg – open set* in X .

Remark 2.30

The intersection of two *spg – open sets* does not necessarily to be *spg – open set*, for example:

Example 2.31

Let $X = \{1,2,3\}$ and let $T = \{X, \emptyset, \{2,3\}\}$ be a *topological* defined on X

It is clear that $\{1,3\}, \{1,2\}$ is a *sp – open set* in X

but $\{1,3\} \cap \{1,2\} = \{1\}$ is not *sp – open set* in X .

Theorem 2.32

Let (X, T) be a *topological space* and let $B \subseteq X$ is a *spg – open set* and $C \subseteq X$ is an *open set* then $B \cap C$ is a *spg – open set*.

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