# A Comparative Study of Graph Search Algorithms for Planar Manipulator to Avoid Obstacle Collision

Mustafa Laith Muhammed<sup>1</sup>, Amjad Jaleel Humaidi<sup>2</sup>, Enass Hassan Flaieh<sup>3</sup>

<sup>1,3</sup>Mechanical Engineering Department, University of Technology, Baghdad, Iraq

<sup>2</sup>Control and Systems Engineering Department, University of Technology, Baghdad, Iraq

<sup>1</sup>me.19.08@grad.uotechnology.edu.iq, <sup>2</sup>Amjad.j.humaidi@uotechnology.edu.iq,

<sup>3</sup>Enass.h.flaieh@uotechnology.edu.iq

Abstract— The search algorithms are characterized by their ability to find the optimal path in a short calculation time. In this study, a comparative analysis has been conducted to perform path planning of planar manipulator for static obstacle avoidance based on graph search algorithms. Four methods have been taken into account to establish a comparison platform; namely, conventional A\*, modified A\*, Chaos A\*, and circulation heuristic search (CHS) algorithms. The performance of comparison is evaluated in terms of length of optimal path and consumption time of calculation. All algorithms have been coded and simulated within the MATLAB software environment. According to computer simulation, the results showed that CHS algorithms outperform the other graph search ones in terms of generated path length, while the Choas A\* could give the least calculation time as compared to its counterparts.

Index Terms— Path planning, A-Star, Modified A-Star, Chaos A-Star, CHS, Planar manipulator.

#### I. INTRODUCTION

The aim of robot path planning is to determine how a robot will move and maneuver within a specific team in order to maintain its objectives. The path planning task requires the robot to generate a collision-free path between a start and a destination point in addition to avoiding obstacles. Furthermore, the robot must meet certain requirements or improve specific performance aspects. The type of path planning is influenced by the amount of information available about the environment (totally unknown, partially known, and completely known). Most of the time, the environment is only partially known, with the robot identifying certain regions inside the workplace before moving on to path planning. The obstacle is said to be static (dynamic) when its position and orientation stay stationary (change) relative to fixed reference frame over the time [1].

When information from sensors installed is continually gathered while the manipulator is moving, local path planning occurs. In this technique of path planning, the robot manipulator reacts instantly to changes in the environment and changes its orientation accordingly. When the robot's surroundings are well-known and static, the planning is known as global path planning. In this mode, the planning algorithm will generate the full path before the movement begins [2][3].

In this study, the main contribution can be listed below:

- 1. A several modifications in classical A\* path planning method has been proposed by extending search area of adjacent nodes around current node or changing search techniques.
- **2.** A comparison study has been conducted between the proposed modified methods with the conventional one.

## II. RELATED WORKS

A review of the most recent studies in the field of current work in order to determine the analysis strategies, Raheem A. and Abdul-Kareem A. introduced a new approach of manipulator path planning based on probabilistic roadmap and the artificial potential field methods and then used A\* method to enhanced roadmap [4]. The study has applied Non-uniform B-spline (NURBS) curve for enhancing the generated path. Huang X. et al., used modified A-star algorithm to develop novel collision-free path planning for articulated space manipulator. The neural network algorithm has been used to ensure optimal time cost of path planning [5]. T. Nayl et al., presented a new approach to find smooth path planning with obstacles avoidance in fully known environment based on modified A-Star algorithm for articulated manipulator with obstacle avoidance based on data acquisition of local range sensors, which are mounted on the manipulator arms [6]. F. Li et al., presented an improved A-star algorithm based on collision-detection algorithm for optimal and collision-free path planning. This study has been applied to take a needle, fixed at the gripper of 6 DOF articulated robot, to inject a target point accurately and smoothly [7]. AL-Qassar A. and Abdulnabi A. utilized Bezier curve and A-star algorithm to achieve collision-free path planning for 5 DOF robot manipulator [8]. J. Silva et al, used graph search algorithm A\* to implement path planning for pick-and-place operations in configuration free space with the presence of obstacles. The proposed method could successfully perform shortest path and avoid both joint limitations and obstacles for articulated manipulator [9]. P. Tavares et al, proposed new path planning approach for multiple robotic manipulators operating in the configuration space based on double A\* algorithm by using multiple universal robot arm 5 (UR5) [10]. S. Gunawan etal, proposed modified A\* algorithm to perform path planning for nonholonomic mobile robots. The proposed method showed smooth and continuous path planning in virtual environment [11]. F. Duchon et al, introduced modifications in the A-star algorithm for mobile robot path planning. The estimation time and the path optimality are the main modified index in this study, which has been applied in different scenarios with high complexity in working environment [12]. X. Li et al proposed a path planning approach in unknown environment by fusing the improved A-star algorithm with improved Dynamic Window Approach (DWA) algorithm. The hybrid methodology could address the drawbacks in the classical A-star algorithm like the capability to avoid obstacles and the use of numerous turning points [13]. X. Lan et al., have developed an improved path planning algorithm method by combing ant colony algorithm (ACA) with A-star algorithm to find local optimal path in mobile robot applications with static obstacles and complex environments [14]. T. Zheng et al., have improved the A-star algorithm in complex environment by firstly utilizing the cost function of angle evaluation to reduces the number of inflection points in the search path and secondly by using the jump search strategy to reduce the number of search nodes [15].

# III. ROBOT MANIPULATOR MODELLING

The Kinematic analysis describes the analytical link between joint positions, position and orientation of end-effector in a Cartesian coordinates by neglecting the moments and forces producing the structural motion [16]. The Kinematic analysis can be classified into forward kinematics (F.K.) and inverse kinematics (I.K.).

The F.K. of robot manipulator is concerned with calculation of the position and orientation of endeffector frame relative to joint coordinates  $\theta$ , while the I.K. focuses on finding specifies joint angles
based on specified cartesian points of end-effector to obtain desired orientation and position of endeffector. *Fig. 1* shows the forward and inverse kinematics for planar manipulator [17][18].

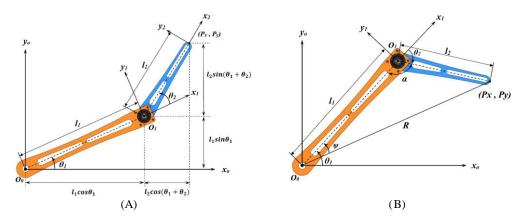


FIG. 1. 2R PLANAR MANIPULATOR (A) ELBOW DOWN CONFIGURATION (B) ELBOW UP CONFIGURATION.

Based on elbow up configuration, one can deduce the cartesian positions as follows:

$$P_{x} = L_{1} \cdot \cos \theta_{1} + L_{2} \cdot \cos \left(\theta_{1} + \theta_{2}\right) \tag{1}$$

$$P_{\nu} = L_1 \cdot \sin \theta_1 + L_2 \cdot \sin (\theta_1 + \theta_2) \tag{2}$$

where  $L_1$  and  $L_2$  are the link lengths of manipulator. For elbow up configuration and based on geometric analysis, the I.K. can be obtained according to the following equations:

$$R^2 = P_x^2 + P_y^2 (3)$$

Using the cosines law to have

$$R^2 = l_1^2 + l_2^2 - 2l_1 l_2 \cos \alpha \tag{4}$$

It easy to get  $\alpha$ ,

$$\alpha = \cos^{-1}\left(\frac{l_1^2 + l_2^2 - R^2}{2l_1 l_2}\right) \tag{5}$$

According to Fig. 1B, one can have

$$\theta_2 = \alpha - \pi \tag{6}$$

$$\theta_2 = \cos^{-1}\left(\frac{l_1^2 + l_2^2 - R^2}{2l_1 l_2}\right) - \pi \tag{7}$$

$$\psi = tan^{-1} \left( \frac{l_2 \sin \theta_2}{l_1 + l_2 \cos \theta_2} \right) \tag{8}$$

$$\theta_{2} = \cos^{-1}\left(\frac{l_{1}^{2} + l_{2}^{2} - R^{2}}{2l_{1}l_{2}}\right) - \pi$$

$$\psi = \tan^{-1}\left(\frac{l_{2}\sin\theta_{2}}{l_{1} + l_{2}\cos\theta_{2}}\right)$$

$$\theta_{1} = \tan^{-1}\left(\frac{P_{y}}{P_{x}}\right) + \tan^{-1}\left(\frac{l_{2}\sin\theta_{2}}{l_{1} + l_{2}\cos\theta_{2}}\right)$$
(9)

## IV. CLASSIC A\* ALGORITHM

The A-Star algorithm is heuristic method which is devoted to search feasible and optimal path in certain environment. The algorithm divides the space into several cells. The evaluation of path length is based on cost function which can be defined by:

$$f(n) = g(n) + h(n) \tag{10}$$

where g(n) denotes the actual distance from the current cell (node) to the start point, h(n) define the heuristic distance from the current cell to the destination point, and f(n) represents the total path distance from the start point to destination point via selected sequence of cells [17].

The classic A\* searches for a cell in the space grid for the optimal way to go from a start point to a destination point. In Fig. 2, the A-star algorithm is applied to eight neighborhoods nodes around a current node.

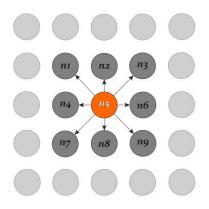


FIG. 2. A\* ALGORITHM SEARCHING DIAGRAM.

In order to move the robot arm from the start point to the goal point in the presence of obstacles, a sequence of joint angles along the path have to be determined [19]. The problem of finding a feasible collision free path, from start to goal, can be solved by applying A\* algorithm, a number nodes within the acceptable area of the workspace will be found by Eq. 10, and used to generate the path. The A\* path planning algorithm to move the arm through the chosen nodes to reach the desired goal point is illustrated via the Pseudo Code listed in *Fig. 3*.

```
Classic_A_star_WSA()
                                                                   Set Open_List = (), Close_List = ();
Begin
                                                                   Insert (Start_Node, Open_List);
 //Workspace Analysis Generation:
     Set Workspace Parameter;
                                                                   Current_Node = Start_Node;
     Set Manipulator Parameter;
                                                                   Determine Eight Neighbor_Node;
                                                                   Insert (Neighbor_Nodes, Open_List);
     Initiate Workspace;
                                                                       For n=1 to Neighbor_Nodes, do
        For i=1 to All Point in Workspace, do
                                                                            F(n) = G(n) + H(n)
             Calculate:Inverse_Kinematic_Elbow_Up
                                                                        End For (n)
        End For (i)
                                                                    Remove (min_cost_Node, Open_List);
     Read Number, Shape, Size, Position of Obstacles;
                                                                    Insert (min_cost_Node, Close_List);
     Identify Acceptable Points;
                                                                         IF the Node is the Target_Node, then
     Identify Forbidden Points;
                                                                               Write: The Path from Targrt_Node
     While (All Points in Workspace are Analyzed)
                                                                                      to Start_Node
                                                                         ELSE
          IF Manipulator Collide the Obstacles, then
                   Repeat Process
                                                                               Find Node Successor that NOT in
          ELSE
                                                                               Close_List, put in Open_List and
                   Write: Free Workspace Analysis
                                                                               calculate the cost functions.
          End IF
                                                                         End IF
 //Path Planning Generation:
                                                                    While (All Nodes are Analyzed)
                                                             End
      Set Search Space Parameter;
```

Fig. 3 The Pseudo Code to execute Path planned of 2 DOF manipulator based on A\* Algorithm.

#### V. MODIFIED A\* ALGORITHM

In the search based on standard A\* algorithm, the work space grid is limited to 8 adjacent nodes surrounding the current node as illustrated in *Fig. 2*. Since the generated path is based on linking the closet possible nodes, this will lead to zigzag style path and hence this is not quite desirable due to sharp edges in finding optimal path.

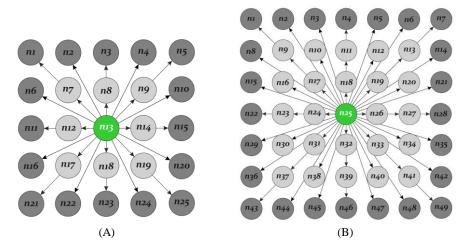


Fig. 4. Modified A\* algorithm searching diagram (a) 24 neighborhood nodes. (b) 48 neighborhood nodes.

The modification of classic  $A^*$  algorithm is to extend searching neighborhoods of the current node. Instead of using searching nodes of 8-nodes, an extension of 24-nodes around the current node has been proposed. Of course, this will reduce the sharp edges as indicated in Fig. 4. However, the evaluation function is calculated in the same principle as in Eq. 10. For path generation, the usage of the node from outer or inner sets is performed based on the presence of the obstacles or the rational calculation of each node, see Fig. 4A. The Pseudo code which represents the steps of modified  $A^*$  algorithm taking into account the planar manipulator and obstacle avoidance is developed in Fig. 5:

```
Modified_A_star_WSA()
                                                                 Set Open_List = (), Close_List = ();
Begin
                                                                 Insert (Start_Node, Open_List);
//Workspace Analysis Generation:
    Set Workspace Parameter;
                                                                 Current_Node = Start_Node;
                                                                 Read Neighbor_Nodes_Matrix_Size;
    Set Manipulator Parameter;
    Initiate Workspace;
                                                                 Determine nth Neighbor_Nodes;
    Do
                                                                 Insert (Neighbor_Nodes, Open_List);
      For i=1 to All Point in Workspace, do
                                                                  For n=1 to Neighbor_Nodes, do
            Calculate: Inverse_Kinematic_Elbow_Up
                                                                          F(n) = G(n) + H(n)
                                                                   End For (n)
    Read Number, Shape, Size, Position of Obstacles;
                                                                 Remove (min_cost_Node, Open_List);
    Identify Acceptable Points;
                                                                 Insert (min_cost_Node, Close_List);
    Identify Forbidden Points;
                                                                   IF the Node is the Target_Node, then
    While (All Points in Workspace are Analyzed)
                                                                         Write: The Path from Targrt_Node to
        IF Manipulator Collide the Obstacles, then
                                                                         Start Node
                  Repeat Process
                                                                   ELSE
        ELSE
                                                                         Find Node Successor that NOT in
                  Write: Free Workspace Analysis
                                                                         Close_List, put in Open_List and
        End IF
                                                                         calculate the cost functions.
//Path Planning Generation:
                                                                   End IF
    Set Search Space Parameter;
                                                                 While (All Nodes are Analyzed)
    Set Search Space Parameter;
                                                           End
```

FIG. 5. THE PSEUDO CODE TO EXECUTE PATH PLANNED OF 2 DOF MANIPULATOR BASED ON MODIFIED A\* ALGORITHM.

# VI. CHAOS A\* ALGORITHM

The necessity behind developing such a modification is either to increase the smoothness of the generated path or to reduce the time needed to reach the destination node, or both, as explained in the previous modification. Because of the search is based on the standard A\* algorithm, the work space grid is limited to 8 adjacent nodes surrounding the current node, as shown in *Fig. 2*, according to that it

take much longer time to reach destination node, so it necessary to develop an algorithm reach destination node with significant less estimation time.

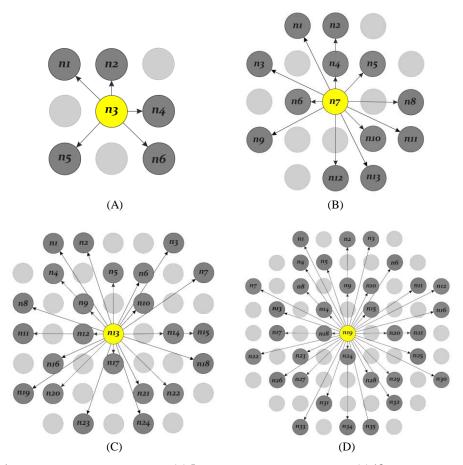


Fig. 6. CA\* algorithm searching diagram (a) 5 random neighborhood nodes. (b) 12 random neighborhood nodes. (c) 23 random neighborhood nodes. (d) 34 random neighborhood nodes.

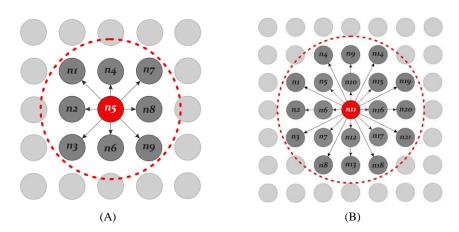
The Chaos A-star (CA\*) algorithm is also a modification of the classic A\* algorithm which extend searching neighborhoods of the current node. The expansion strategy takes the structure of an octagon with a specific radius to distribute neighboring nodes, but in a random distribution manner; for example, if the number of adjacent nodes is 48, only 23 of them are randomly distributed as shown in Fig. 6C. The objective of this modification is to minimize the time necessary to search for the destination node or the transition time from the start node to the end node in the presence of obstacles by more than 50% when compared to previous modified algorithms with the same number of search nodes. However, the evaluation function is calculated in the same principle as in Eq. 10. For path generation, the selection of the node in the searching process is performed based on the presence of the obstacles or the rational calculation of each node, see Fig. 6B, C, D. The Pseudo code which represents the steps of Chaos A\* algorithm is developed in Fig. 7.

```
Chaos_A_star_WSA ()
                                                               Insert (Start_Node, Open_List);
Begin
//Workspace Analysis Generation:
                                                               Current Node = Start Node;
    Set Workspace Parameter;
                                                               Read Search Radius of Octagon from
    Set Manipulator Parameter;
                                                               Current_Node;
    Initiate Workspace;
                                                               Determine nth Neighbor Nodes Randomly;
                                                               Insert (Neighbor_Nodes, Open_List);
      For i=1 to All Point in Workspace, do
                                                                  For n=1 to Neighbor_Nodes, do
       Calculate: Inverse_Kinematic_Elbow_Up
                                                                         F(n) = G(n) + H(n)
                                                                  End For (n)
    Read Number, Shape, Size, Position of Obstacles;
                                                               Remove (min_cost_Node, Open_List);
    Identify Acceptable Points;
                                                               Insert (min_cost_Node, Close_List);
    Identify Forbidden Points;
                                                                  IF the Node is the Target_Node, then
    While (All Points in Workspace are Analyzed)
                                                                        Write: The Path from Targrt_Node to
      IF Manipulator Collide the Obstacles, then
                                                                        Start_Node
              Repeat Process
                                                                  ELSE
      ELSE
                                                                         Find Node Successor that NOT in
              Write: Free Workspace Analysis
                                                                         Close_List, put in Open_List and
      End IF
                                                                         calculate the cost functions.
//Path Planning Generation:
                                                                  End IF
   Set Search Space Parameter;
                                                                While (All Nodes are Analyzed)
    Set Search Space Parameter;
                                                           End
    Set Open_List = (), Close_List = ();
```

Fig. 7. Chaos A\* algorithm Pseudo Code.

#### VII. CIRCULATION HEURISTIC SEARCH

The Circulation Heuristic Search (CHS) is a modification of standard A\* algorithm which extend searching neighborhoods of the current node. Instead of using searching nodes of 8-nodes, the expansion strategy uses deploying all nodes inside a circle whose center is the current node, and its diameter is determined in advance based on the unit of measurement used in the work space. Of course, this will reduce the sharp edges as indicated in *Fig.* 8.



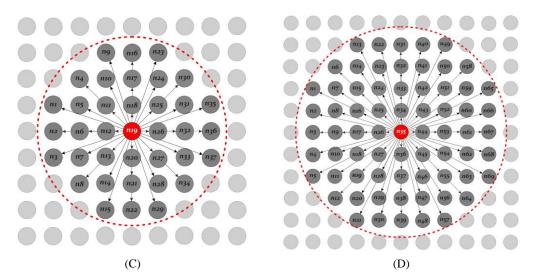


FIG. 8. CHS ALGORITHM SEARCHING DIAGRAM (A) 2-UNIT RADIUS (B) 3-UNIT RADIUS (C) 4-UNIT RADIUS (D) 5-UNIT RADIUS.

However, the evaluation function is calculated in the same principle as in Eq. 10. For path generation, the selection of the node inside the searching circle is performed based on the presence of the obstacles or the rational calculation of each node, see *Fig.* 8B, C, D. The Pseudo code which represents the steps of CHS algorithm taking into account the planar manipulator and obstacle avoidance is developed in *Fig.* 9.

```
Circulation_Heuristic_Search_WSA()
                                                                Insert (Start_Node, Open_List);
Begin
//Workspace Analysis Generation:
                                                                Current Node = Start Node;
    Set Workspace Parameter;
                                                                Read Search Circle Size from Current_Node;
    Set Manipulator Parameter;
                                                                Find all the Nodes inside the search Circle and
    Initiate Workspace;
                                                                   Consider them as Neighbor_Nodes of
                                                                   Current_Node;
      For i=1 to All Point in Workspace, do
                                                                Insert (Neighbor_Nodes, Open_List);
       Calculate: Inverse_Kinematic_Elbow_Up
                                                                  For n=1 to Neighbor_Nodes, do
                                                                         F(n) = G(n) + H(n)
      End For (i)
    Read Number, Shape, Size, Position of Obstacles;
                                                                  End For (n)
    Identify Acceptable Points;
                                                                Remove (min_cost_Node, Open_List);
    Identify Forbidden Points;
                                                                Insert (min_cost_Node, Close_List);
    While (All Points in Workspace are Analyzed)
                                                                  IF the Node is the Target_Node, then
                                                                         Write: The Path from Targrt_Node to
      IF Manipulator Collide the Obstacles, then
              Repeat Process
                                                                         Start_Node
      ELSE
                                                                  ELSE
              Write: Free Workspace Analysis
                                                                         Find Node Successor that NOT in
      End IF
                                                                         Close_List, put in Open_List and
//Path Planning Generation:
                                                                         calculate the cost functions.
   Set Search Space Parameter;
                                                                  Fnd IF
    Set Search Space Parameter;
                                                                 While (All Nodes are Analyzed)
    Set Open_List = (), Close_List = ();
                                                           End
```

Fig. 9. The Pseudo Code to execute Path Planned of 2 DOF manipulator based on CHS Algorithm.

## VIII. SIMULATION RESUTLS

In this study, the up-elbow configuration is addressed and the generated path planning algorithms consists of three parts. The first part is the workspace in Cartesian space. The workspace is defined as a space made of all points that can only be reached by a specified end-effector configuration. Inverse kinematics has been used to obtain these points which are related with joint angles. As illustrated in

Fig. 10, the generation of free cartesian space is limited by mechanical and geometric constraints, which affect and limit the motion of the robotic manipulator as well as split the workspace into *acceptable* and *forbidden* zones. The generation of free cartesian space can be achieved by analyzing all possible solutions for *acceptable* points in the environment, which are dependent on the obstacles collision checking function as shown in Fig. 10B [20].

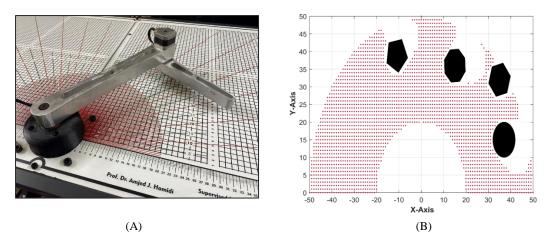


Fig. 10. (a) Manipulator Layout (b) Work space analysis with different obstacle shape based on elbow up manipulator.

The workspace has a dimension of (50 to 50) cm in the x-axis and (0 to 50) cm in the y-axis. The length of the manipulator links is 30 cm for link 1 and 20 cm for link 2. The obstacle type is static and its arrangement in the workspace has two cases for each proposed method. The cases are composed of four obstacles, each one of various shapes with a diameter of 10 cm and coordinates as shown in Table I.

TABLE I. OBSTACLES COORDINATES FOR THE PROPOSED PATH PLANNING ALGORITHMS

Configuration -	1st-Obstacle		2 <sup>nd</sup> -Obstacle		3 <sup>rd</sup> -Obstacle		4 <sup>th</sup> -Obstacle	
	X (cm)	Y (cm)	X (cm)	Y (cm)	X (cm)	Y (cm)	X (cm)	Y (cm)
Case 1	35	18	7	35	-13	35	-30	20
Case 2	41	10	7	40	-16	33	-	-

The second part of the proposed path planning algorithms is the workspace analysis for obstacle avoidance. This part is the same as the obstacle-free space excluding all the points which make contact with obstacle area. In other words, this part includes all points of workspace where there is no collision of manipulator's links with resident obstacles during the path planning from start to destination points. Accordingly, one can detect three forbidden regions; one is due to allowable lengths of arms (outer region), the second area is due to presence of obstacle, while the third area (inner region) is due to singularity and mismatch in length of the first and second arms. The latter area has a radius equal to the length of second link as shown in *Fig. 10*B.

The third part of path planning is the path planning algorithm. This process is restricted only to an acceptable area. The algorithms have to find the shortest path from start to destination point within the acceptable area in a shortest time. *Fig. 11*, shows the implementation of two cases of obstacle configurations based on A\* algorithm.

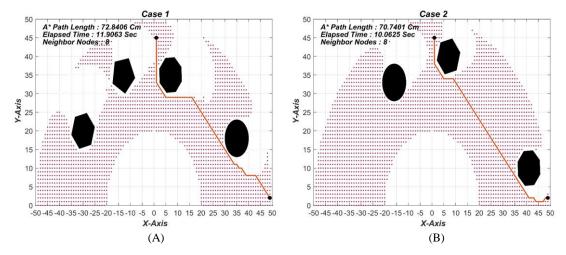


FIG. 11. A\* PATH PLANNING WITH TWO OBSTACLE CONFIGURATIONS: (A) CASE 1, (B) CASE 2.

As shown in Fig. 11, the generated paths are due to searching in 8 neighbor nodes around the current node, where in case 1 the total length of the path from start to destination point is 72.8406 cm, in total estimated time 11.9063 sec, whereas in case 2, the total length of the path is 70.7401 cm, in total estimated time 10.0625 sec. The variation in length between the two cases is due to the location change and shape of the obstacles. Fig. 12, shows the variation of the joint's angles with respect to time of manipulator movement from start to destination for both cases.

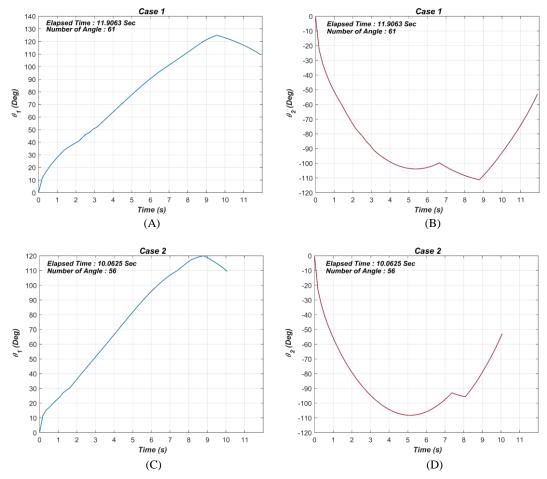


Fig. 12. A\* path planning joint variation  $m{ heta_1}$  (a , c) and  $m{ heta_2}$  (b , d) for both cases.

In the next scenario, the Modified A\* path planning is considered as shown in Fig. 13. for two cases. In this study, 24 neighbor nodes are used for searching purposes. In case 1, the total length of path, from start to destination point, is equal to 72.6559 cm, which is done in estimated time 11.4844 sec. In case 2, the total length of the path is 69.2297 cm with estimated time equal to 9.2656 sec. The variation in length and time between the two cases is due to the change in obstacle locations and shapes.

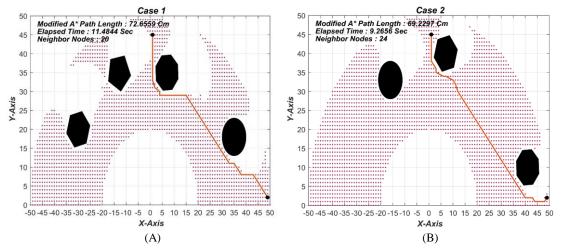


FIG. 13. MODIFIED A\* PATH PLANNING: (A) CASE 1, (B) CASE 2.

Fig. 14 shows the variation of the joint's angles for both cases.

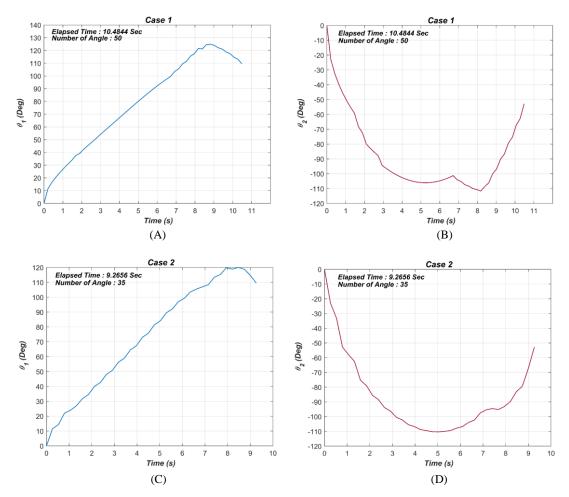


Fig. 14. Modified A\* path planning joint variation  $\theta_1$  (a , c) and  $\theta_2$  (b , d) for both cases.

Now, the chaos A\* path planning is applied as shown in *Fig. 15*, for two cases. In this study, 23 random nodes of 44 neighbor nodes are used for searching purposes. In case 1, the total length of path, is equal to 72.6706 cm, which is done in estimated time 5.9844 sec. In case 2, the total length of the path is 69.2297 cm with estimated time equal to 3.6406 sec. *Fig. 16*, shows the variation of the joint's angles for both cases.

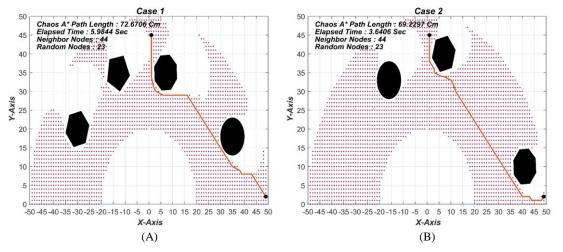


FIG. 15. CHAOS A\* PATH PLANNING: (A) CASE 1, (B) CASE 2.

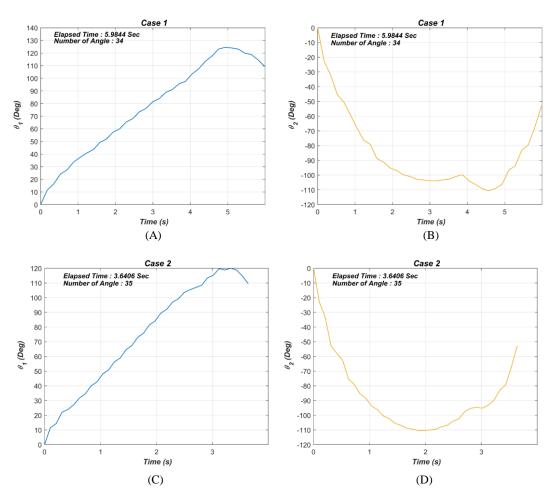


Fig. 16. Chaos A\* path planning joint variation  $\theta_1$  (a , c) and  $\theta_2$  (b , d) for both cases.

As illustrated in *Fig. 17*, the CHS path planning is evaluated for two scenarios. In this work, a search circle with a radius of 5 units and 56 neighbor nodes inside it is employed. In Case 1, the entire length of the path from start to target node is 68.984 cm, which is accomplished in an estimated time of 11.6563 sec. In Case 2, the entire length of the path is 68.325 cm, with an estimated time of 10.0313 sec.

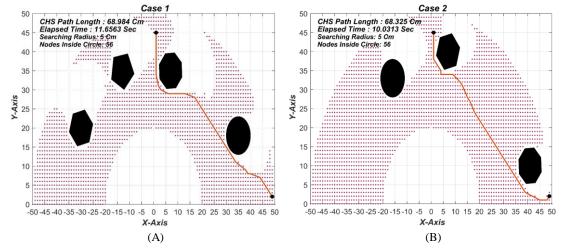


FIG. 17. CHS PATH PLANNING: (A) CASE 1, (B) CASE 2.

Fig. 18, depicts the fluctuation of the joint angles in both circumstances.

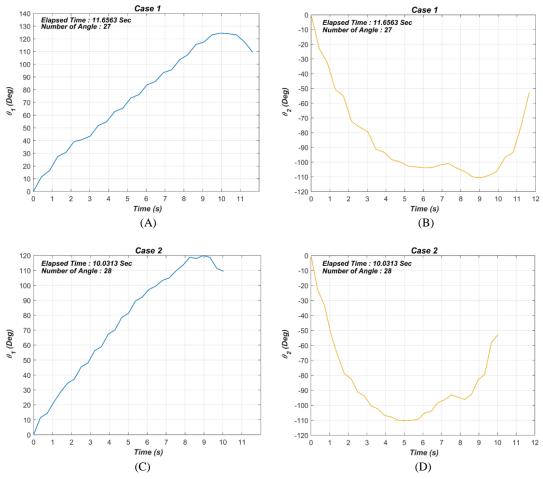


Fig. 18. CHS path planning joint variation  $\theta_1$  (a , c) and  $\theta_2$  (b , d) for both cases.

Based on simulated results, the length and the time taken by proposed path planning algorithms are listed in Table II. The table indicates that the length of path based on CHS algorithm is shorter than that based on A\* algorithm and other modifications for both cases. But, in term of estimation time, the chaos A\* algorithm beats the other modified algorithms including the classic A\* algorithm.

-		Cas	se 1		Case 2			
Algorithms	Length (cm)	Improvement (%)	Time (sec)	Improvement (%)	Length (cm)	Improvement (%)	Time (sec)	Improvement (%)
A* Path Planning	72.8406	0	11.9063	0	70.7401	0	10.0625	0
Modified A* Path Planning	72.6559	0.25	11.4844	3.67	69.2297	2.18	9.2656	8.60
Chaos A* Path Planning	72.6706	0.23	5.9844	98.95	69.2297	2.18	3.6406	176.39
CHS Path Planning	68.984	5.59	11.6563	2.14	68.325	3.53	10.0313	0.31

TABLE II. COMPARISON OF THE PROPOSED PATH PLANNING ALGORITHMS

The block diagram describing the signal flow between PC and the robot manipulator is shown in Fig. 19. The computer hosts the path which is generated by A\* algorithm. The path is in cartesian space and it converted joint steps according to samples required movements. The samples of angular positions are fed to micro-stepping motors via Arduino-Uno microcontroller. Due to low power of output signals for microcontroller, the drive is necessary to actuate the motor for desired step angular position.

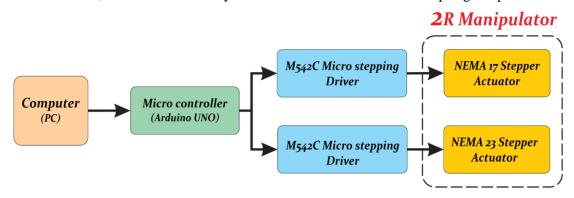


FIG. 19. BLOCK DIAGRAM OF REAL-TIME IMPLEMENTATION FOR PATH PLANNING ALGORITHMS.

Other hardware embedded design can be applied to implement the optimization algorithms in real-time environment. The Arduino microcontroller used in this work can be replaced by other single-board computers like Raspberry-Pi, or semiconductor devices like Field Programming Gate Array (FPGA) to implement the scenarios of proposed path planning techniques for 2R manipulator. It has been shown that has new hardware technologies can enhance the time cost to large extent [21]–[24].

This study can be extended for future work to include the dynamic model of the manipulator and to apply advanced control techniques in implementation of path planning methods[25]–[31]. Another update of this work is to in-cooperate modern optimization techniques in finding the optimal path in the presence of obstacles. One may propose recent optimization algorithms like particle swarm optimization (PSO), social spider optimization (SSO), Whale optimization algorithm (WOA), Butterfly optimization algorithm (BOA), Grey-wolf optimization (GWO) [32]–[36].

## IX. CONCLUSIONS

This work analyzes path planning techniques for 2R planar manipulators in the presence of static obstacles in a known environment as well as their implementation. The classic A\*, modified A\*, chaos A\*, and CHS algorithms have been proposed as path-planning algorithms. All techniques have been evaluated in a MATLAB simulation environment. The results reveal that the path generated by the CHS algorithm is shorter than the paths generated by the other approaches. In addition, the chaos A\* algorithm could execute the robot gripper in significantly less time than its counterparts.

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