

## **An improvement of Haar wavelet transform compressor**

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### **Abstract:**

Images compression are just decreasing the quantity of data necessary to represent images. for compressing the images efficiently and effectively we used a Different method to reducing the space and increasing the transfer efficiency of the image by the networks for superior access. This work aimed to create an image compression using modified Haar wavelet transform based on eight nodes to calculate the differencing and averaging in data transformation.

The suggested procedure is to get maximum image compression ratio(C.R), high peak signal tonoise ratio (PSNR) ratio and less Mean Square Error (MSE). The proposed work has been examined through many experiments, the results show very interestingresults in compression rates and the reconstructed image.The numerical work has been done by using matlab software.

**Keywords:** Image Compression, wavelet transform, HaarWavelet, modified fast Haar wavelet

## 1. Introduction:

Image compression considers one of the most significant parameters to increase the probability of saving images or transmitting it by different communication devices. The advantage of compressing the image is to make it easy to save, treat and transfer. There are two groups which the image compression is limited by them. The two groups named lossless and lossy. In the methods, it is possible to recreate image construction after compressing; where it is happened without any missing of data of the whole process in lossless method. Lossy techniques considered as reversible processes because the processes consist of performance quantization, which lead to data missing, the compression rate (C.R.) in lossy technique we get higher compression rate than lossless technique [1].

Wavelet is a mathematical function that divides data to several frequency elements then matches the resolution to them scales [2]. Wavelet transform decomposes a signal into a set of basic functions. These basic functions are called wavelets. The properties of wavelets are short time localized waves with zero integral value and possibility of time shifting and flexibility with work.

Many papers are published related to the field of Haar wavelet, Adnan khashman et al [3] used the neural network to compress of an image. Two different neural networks with different input image sizes were used and a comparison between the performances according to Haar-based compression. Gaurav Vijayvargia et al [4], suggested a paper where analysis on different kinds of image compression techniques has been completed. After looking on all strategies, it is known that image files resulting from lossless compression techniques are better than resulting from lossy compression techniques. Lossy provides higher compression percentage than lossless. Gagandeep Kour et al [5], used different wavelet transforms with different levels of decomposition to decompose image on wavelet decomposition technique. A super resolved image was generated from the decomposed.

Piyush Kumar Singh et al [7], the paper study a comparison between DCT based image compression and wavelet based image compression using CDF9/7 wavelet as used in JPEG-2000 Standards based on common encoding scheme known as Huffman encoding for both. Also analyzed a trend based on different level of wavelet transform on image size and image quality based on MSE.

**Mousume Samad** et al [6], Original image reconstructed from destroyed image using Haar Wavelet transform established from the compressed image and the pixel position of the original image. In spite of lossy compression after reconstruction there is no psycho visual redundancy. **Mohannad Abid Shehab Ahmed** et al [1], made a comparison between standard JPEG, Haar, and modified Haar techniques, and approved the capability of modified Haar over other techniques.

In this paper we introduce a modification of Haar wavelet transform Haar based on eight nodes to calculate the differencing and averaging in data transformation.

The paper is organized as following: Section 2 describes the statement of the problem. Section 3 describes the Haar wavelet transform. Section 4 introduced the proposed procedures of the work for modified Haar wavelet transform (HWT). Section 5 is the implementation and result analysis.

## 2. The Statement of the Problem

Dealing with image file need huge memory space; large transmission bandwidths; long transmission times and fast processing. One of the main applications of digital signal processing is the compression of signal. Wavelet algorithm had been solved most of the image processing applications. But modern application needs more compression rates, high PSN ratios and less MSE. Haar wavelet may be considered as the simplest form of wavelet techniques. The main disadvantage of this method is that it is not continuous in all domain; longer compression time and low compression rates.

## 3. Haar Wavelet

At recent days, the wavelet transformation is displayed as a cutting edge method, within a domain of analyzing image. The Haar wavelet is a sequence of functions in mathematics forms. It is first invention by Alfred Harrin 1990. The Haar wavelet is as simple as possible wavelet transformation classis [1].

The benefits of Haar Wavelet transform is as follow [8]:

1. Best execution as far as calculation time.
2. Fast calculation speed.
3. Effective compression method
4. Memory effective, because it computed in-place without a temporary array.

The disadvantage of Haar Wavelet transform is as follow:

1. low compression rates
2. longer compression time

The aim of wavelet transformation is convert the input signal from time domain to frequency domains. The Haar wavelet function is defined as follow [9]:

$$\Psi(x) = \begin{cases} 1 & \text{for } 0 \leq x < 1 \\ -1 & \text{for } 1 \leq x < 2 \\ 0 & \text{elsewhere} \end{cases} \quad (1)$$

equation (1) can be represented in figure 1.

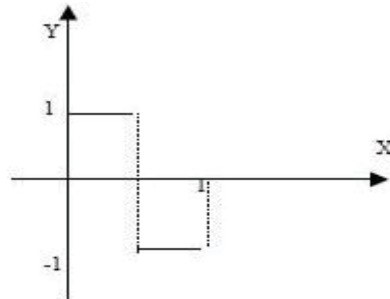


Figure 1: The Haar wavelet [3]

The scale function of wavelet  $\phi(x)$  is defined as [3]:

$$\phi(x) = \begin{cases} 1 & \text{for } 0 \leq x < 1 \\ 0 & \text{elsewhere} \end{cases} \quad (2)$$

The Haar wavelet transform could be mixed of a consequence of low pass and high pass filter, they are named filter bank. The scale functions of wavelet with various scales that perform the filter bank are [8]:

$$\phi(x) = \phi(2x) + \phi(2x - 1) \quad (3)$$

$$\psi(x) = \phi(2x) - \phi(2x - 1) \quad (4)$$

The low pass filters which perform averaging/blurring operations, can be described as follow [1].

$$L = \frac{1}{2} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \quad (5)$$

The high-pass filters perform the difference operations, could be described as [1]:

$$H = \frac{1}{2} \begin{bmatrix} 1 & -1 \\ 1 & -1 \end{bmatrix} \quad (6)$$

The simultaneous formulate of previous equations can be done by four filters i.e., (HH, LH, HL, and LL) each of (2 x 2) pixels as shown in figure (2).

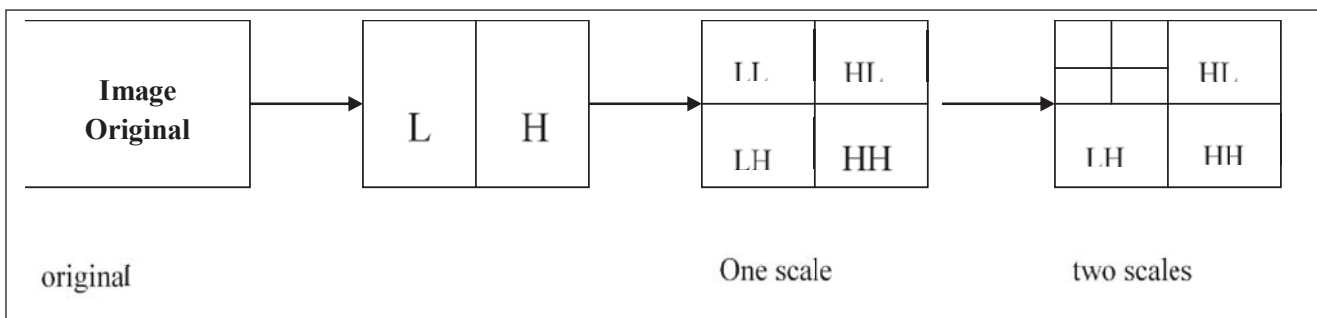


Figure 2: The four filters of Haar wavelet transform representation [13]

In this transformation, the base of above four filters are described as the following[1]:

- a- The horizontal low pass filter which followed by the vertical low pass filter is equal to:

$$LL = \frac{1}{2} \begin{pmatrix} 1 & \\ & 1 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ & \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \dots\dots\dots(7)$$

- b- The horizontal high pass filter, followed by vertical low pass filter can be described as:

$$HL = \frac{1}{2} \begin{pmatrix} 1 & \\ & -1 \end{pmatrix} \begin{pmatrix} 1 & 1 \\ & \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & 1 \\ -1 & -1 \end{pmatrix} \dots\dots\dots(8)$$

- c- The horizontal low pass filters, followed by vertical high pass filter is equal to:

$$LH = \frac{1}{2} \begin{pmatrix} 1 & \\ & -1 \end{pmatrix} \begin{pmatrix} 1 & -1 \\ & \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & -1 \\ 1 & -1 \end{pmatrix} \dots\dots\dots(9)$$

- d- The horizontal high pass filters, followed by vertical high pass filter can be:

$$HH = \frac{1}{2} \begin{pmatrix} 1 & \\ & -1 \end{pmatrix} \begin{pmatrix} 1 & -1 \\ & \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & 1 \\ -1 & -1 \end{pmatrix} \dots\dots\dots(10)$$

The original image is processed by using several operations to compress image for Haar wavelet, these processes are given below.

1. Read the image from the user.
2. the convert from RGB system to ycbcr system after than converts to matrices of (8\*8) pixels with using some sequence processes on the colors of image, the colors of image consist of one coordinate matrix and three colors matrices. The coordinate matrices include x,y coordinate value for the images. The Colors matrices were marked as blue(B), green (G), red(R) [10] and converted to matrices (8\*8) as following:

$$Y = 0.299R + 0.587G + 0.114B \dots\dots\dots(11)$$

$$Cb = -0.1687R - 0.3313G + 0.5B + 128 \dots\dots\dots(12)$$

$$Cr = 0.5R - 0.4187G - 0.0813B + 128 \dots\dots\dots(13)$$

3. The row column transforms matrices (x) calculated to prove works of wavelet transformation. In the first step, the transform data thread was distributed over equations 7-10, which is known as differencing and averaging. After completing this process on all rows, we move forward in doing the same transformation on columns. The final result is 8\*8 matrix x, called the Haar wavelet transform of the original image. And a sparse for the matrix with a high proportion of zero [11] and in this ways used three level for transform.
4. the gate of wavelet compression. Set non-negative threshold value  $\xi$  and order that the details coefficient of wavelet transformed data, which its account is less than or equal to  $\xi$ , will change to zero. Also, reconfigure an approximate of main data by using fake versions of wavelet transformation data. If the information is lost, the processes titled Lossy compression or else they called as "Lossless compression" [11].

5. Calculate MSE and PSNR values of different compression ratios for the reconstructed images.

#### 4. Modified Fast Haar Wavelet Transform

In Modified Fast Haar Wavelet Transform, start by calculating the average of sub signal,  $a^1 = (a_1, a_2, \dots, a_{N/2})$ , at one level for signal of length N i.e.  $f = (f_1, f_2, \dots, f_N)$  [12] :

$$Av_m = \frac{f_{4m-3} + f_{4m-2} + f_{4m-1} + f_{4m}}{4} \quad m = 1, 2, 3, \dots, N/4, \dots \dots \dots (14)$$

Then calculating the difference process sub signal,  $d^1 = (d_1, d_2, \dots, d_{N/2})$ , at the same level is given as

$$dm = \begin{cases} \frac{(f_{4m-3} + f_{4m-2}) - (f_{4m-1} + f_{4m})}{4} & m = 1, 2, 3, \dots, N/4, \\ 0 & m = \frac{N}{2}, \dots, N \end{cases} \dots \dots \dots (15)$$

Here four nodes are considered at a time instead of two nodes as in Haar Transform.

A modified Haar Wavelet Transform can be done by performing the following steps :

- a) Read the image and convert it to a matrix. Preserves the pixel values of the original input image as in Haar wavelet.
- b) Apply *Modified Fast Haar Wavelet Transform*, over the image matrix along all rows and columns wise.
- c) From (b) we get a one level of input image.
- d) To reconstruct image process, use FHT on the image matrix obtained in step(b).
- e) Calculate MSE and PSNR for reconstructed image.

#### 5. Proposed algorithm

In improved of modified fast Haar Wavelet transform (IMFHT),  $a^1 = (a_1, a_2, \dots, a_{N/4})$ , at one level for signal of length N i.e.  $F = (f_1, f_2, \dots, f_n)$ , start by calculating the average of sub signal,  $a^1 = (a_1, a_2, \dots, a_{N/2})$ , at one level for signal of length N i.e.  $f = (f_1, f_2, \dots, f_N)$  :

$$Av_m = \frac{f_{8m-7} + f_{8m-6} + f_{8m-5} + f_{8m-4} + f_{8m-3} + f_{8m-2} + f_{8m-1} + f_{8m}}{8} \quad m = 1, 2, 3, \dots, N/8 \dots (14)$$

Then calculating the difference process of sub signal,  $d^1 = (d_1, d_2, \dots, d_{N/4})$ , at the same level is given as

$$dm = \begin{cases} \frac{(f_{8m-7} + f_{8m-6}) - (f_{8m-5} + f_{8m-4}) - (f_{8m-3} + f_{8m-2}) - (f_{8m-1} + f_{8m})}{8} & m = 1, 2, 3, \dots, N/8 \\ 0 & m = \frac{N}{4}, \dots, N \end{cases} (15)$$

Here eight nodes are considered at a time instead of two nodes as in Haar Transform and four node as in modified fast Haar wavelet transform.

A *improve fast* modified Wavelet Transform can be done by performing the following steps

- (1) Read the image and convert it to a matrix. preserves the pixel values of that image as in HT
- (2) Apply IMFHT, along row and column wise on entire matrix of the image.
- (3) From (2) we get a one level of input image.
- (4) To reconstruct image process, use Haar transform on the image matrix obtained in step (2).
- (5) Calculate MSE and PSNR for reconstructed image.

Fig. 3 describes the flowchart of the proposed algorithm.

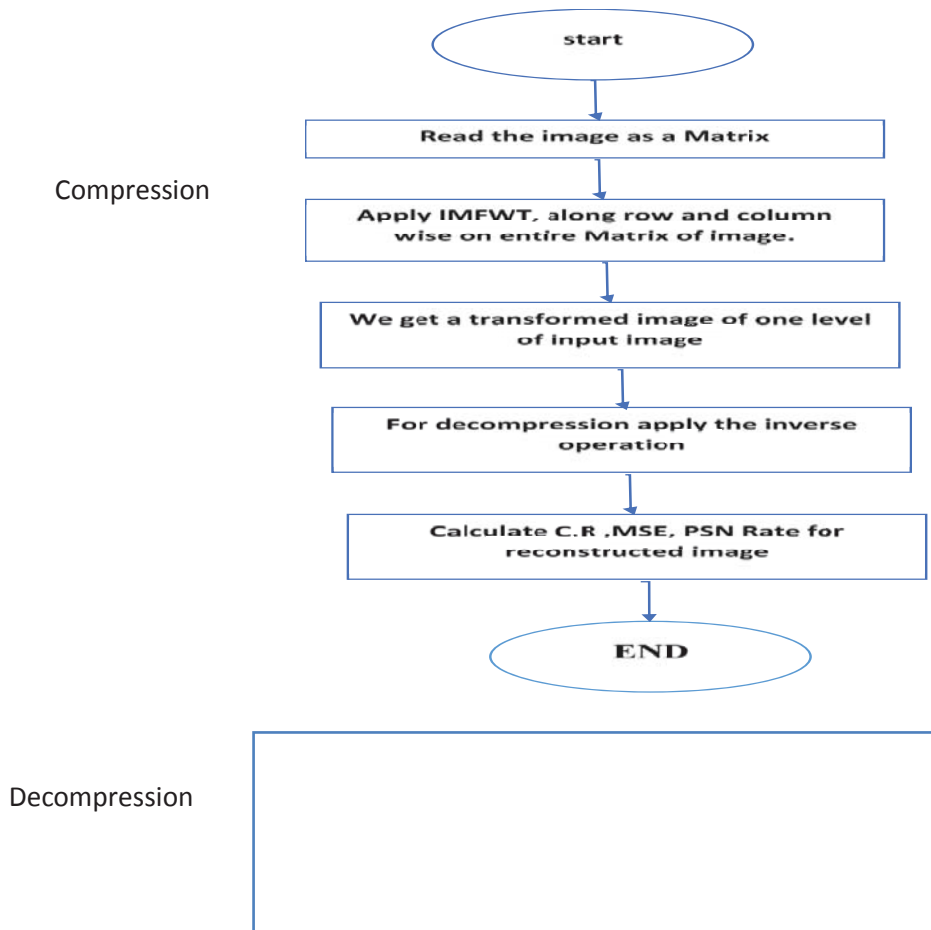


Figure 3: Flowchart for proposed algorithm

## 6. Implementation and result analysis

The presented work allows to compress image files. The peak signal to noise ratio (PSNR) and the compression ratio (CR) and Mean Square Error (MSE) [1,9] are computed using equations (14) and (15) and (16) for a number of experimental image files and compare with HT and MFHT.

Table 1 summarizes these results.

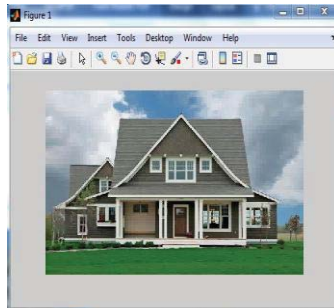
$$CR = \text{Original image size} / \text{compressed image size} \dots (14)$$

$$MSE = \frac{\sum_{M,N} [I1(m,n) - I2(m,n)]^2}{M * N} \dots \dots \dots (15)$$

where M and N are the number of rows and columns in the input images,

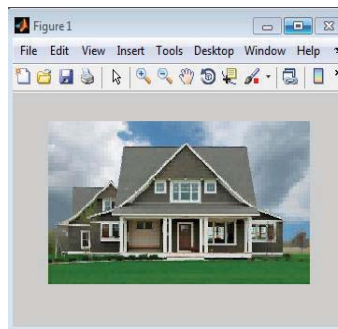
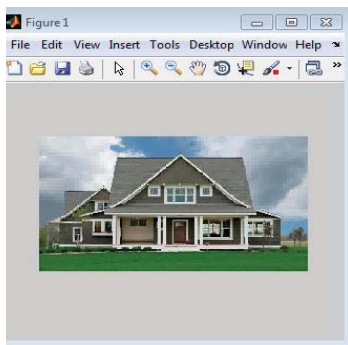
$$PSNR = 10 \log \frac{Max^2}{MSE} \dots \dots \dots (16)$$

where Max is the maximum fluctuation in the input color image, so max is 255. The original image is shown in the fig. (4 .a) and the image that is on the figure (4.b) shows constructed image that compressed by basic Haar wavelet, while the images in the figure(4 .c) and figure (4.d) show constructed image that compressed by using MFHT and IMFHT methods respectively.



a. Original Image(Home.jpg)

b. Compressed Image(Haar wavelet)








c. Compressed Image( MFHT)

d. Compressed Image( IMFHT)

Figure4: The image(home) before and after compression



Table 1: Experimental Results for HT and MFHT and IMFHT

NB	Image	Method	MSE	PSNR	C.R
1		HT	4.23	41.86	37.34
		MFHT	1.23	47.23	83.67
		IMFHT	0.98	48.21	89.13
2		HT	6.25	40.17	39.55
		MFHT	2.10	44.90	85.67
		IMFHT	1.06	47.87	89.98
3		HT	3.68	42.47	48.16
		MFHT	1.36	46.79	87.43
		IMFHT	0.8	49.09	91.66
4		HT	5.89	40.42	42.78
		MFHT	2.57	44.03	78.66
		IMFHT	1.7	45.82	86.29
5		HT	6.43	40.04	33.94
		MFHT	3.58	42.49	80.24
		IMFHT	1.58	46.14	92.22

We applied our algorithm with several images of different sizes, we compare the results with HT and MFHT. The proposed algorithm shows better results over other algorithms, the percentage compression rate 7% increase in IMFHT with compare with MFHT and 53% with HT, 2% increase PSNR rate with MFHT and 8% increase PSNR rate in HT, 1% decrease in MSE in MFHT and 3% decrease in MSE HT, we founded that the propose algorithm (IMFHT) has high compression ratio, best PSNR occurred in the compressed data and less MSE, as shown in image home in the figure 5 a comparison between HT, MFHT and IMFHT by used MSE and PSNR according the table above and figure 6 a comparison between HT and MFHT and IMFHT by used C.R.

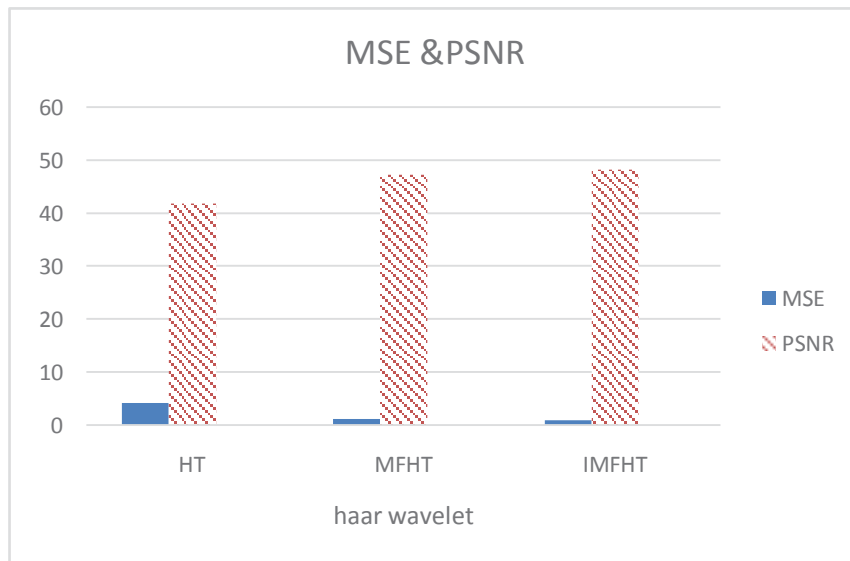


Figure 5: compare between HT and MFHT and IMFHT by used MSE and PSNR

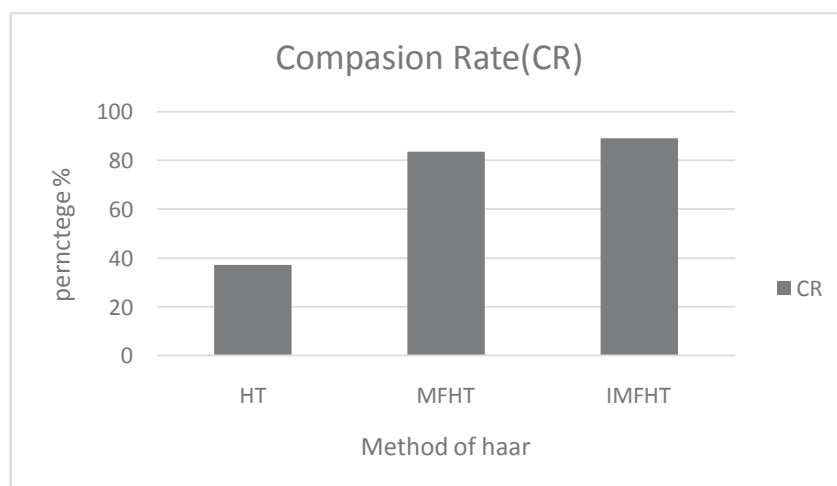


Figure 6: compare between HT and MFHT and IMFHT by used C.R

## 7. Conclusions

The paper show that the proposed algorithm that is improved by eight nodes instead of four nodes as in modified HaarTransform and two node as in Haar transform. The results showed a high image quality that rebuilt from compressed image. Also, the important details of images were saved. While it achieves a high compression rate. It may be concluded that with compare to HT and MFHT we got better results in IMFHWT, the percentage compassion rate 7% increase in IMFHT with compare with MFHT and 53% with HT, 2% increase PSN rate with MFHT and 8% increase PSN rate in HT, 1% decrease in MSE in MFHT and 3% decrease in MSE HT.

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