

Sub groups of a Symmetric group (S_6, \circ)

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Abstract:

This research deal with a form of elements of (S_6, \circ), and introduce some sub groups of symmetric group (S_6, \circ), also introduce some examples, results and properties about this symmetric group.

المستخلص:

تم في هذا البحث التعامل مع الزمرة التناظرية زمرة التباديل لسنة عناصر بتقديم عناصرها كاملة مع القوانين التي تحدد العناصر وكذلك الزمر الجزئية من هذه الزمرة مع تقديم بعض الامثلة والنتائج حول الموضوع.

Introduction;

In mathematics, the symmetric group on a set is the group consisting of all bijections of the set (all one-to-one and onto functions) from the set to itself with function composition as the group operation, and denoted S_n .

The symmetric group is important to diverse areas of mathematics such as Galois theory, invariant theory, the representation theory of Lie groups, and combinatory. Cayley's theorem states that every group G is isomorphic to a subgroup of the symmetric group on G .

The symmetric group on a set of n elements has order $n!$. It is abelian if and only if $n \leq 2$. For $n = 0$ and $n = 1$ (the empty set and the singleton set) the symmetric group is trivial (note that this agrees with $0! = 1! = 1$), and in these cases the alternating group equals the symmetric group, rather than being an index two subgroups.

The symmetric group on a set of size n is the Galois group of the general polynomial of degree n and plays an important role in Galois theory. In the representation theory of Lie groups, the representation theory of the symmetric group plays a fundamental role through the ideas of Schur functors. In the theory of Coxeter groups, the symmetric group is the Coxeter group of type A_n and occurs as the Weyl group of the general linear group. In combinatorics, the symmetric groups, their elements (permutations). Subgroups of symmetric groups are called permutation groups and are widely studied because of their importance in understanding group actions, homogenous spaces, and automorphism groups of graphs.

1)Some definitions and elementary things:

Definition(1-1): Let S_n is the set of all mappings of to itself, is a group called symmetric group with n elements in it.

Theorem (2-1): (Cayley's Theorem). Every group of order n is isomorphic to a subgroup of (S_n, \circ).

Definition(3-1): Let be the set of all maps from the six elements set $\{1, 2, 3,4,5,6\}$ to itself, (S_6, \circ) is a symmetric group under the operations of composition of maps 'o'.

Remarks(4-1);

- 1) (S_6, \circ) is not commutative group.
- 2) The symmetric group (S_6, \circ) is the group of all permutations of 5 elements. It has $5!=120$ elements .
- 3) There are subgroups of (S_6, \circ), including the group itself and the small subgroups.

Example(5-1):

The group (A_6, o) , which has order 360 .

Let $p = 8$, $q = 3.3.5 = 45$, clear $8 \nmid 45$

$360 = 8. 45 = 8.3.3.5$

have subgroups of order 8 , 3 and 5 .

2- A symmetric group (S_6, o) and it's subgroups ;

Definition(1-2): Let S_6 be the set of all maps from the six element set to itself, is a symmetric group under the operations of composition of maps 'o'.

$S(6)=\{i,(12)(34)(56),(13)(24)(56),(14)(23)(56),(24)(16)(35),(34)(16)(25),$
 $(15)(24)(36),(35)(26)(14),(45)(12)(36),(1423),(16)(23)(45),(26)(13)(45),$
 $(25),(46)(12)(35),(45),(56),(123),(132),(124),(142),(125), (152),(126),$
 $(162),(345),(354)(134),(143),(135),(153),(136),(163),(145),(154),(346),$
 $(364)(146),(164),(156),(165),(234),(243),(235),(253),(356),(465),(236),$
 $(263),(245),(254),(246),(264),(265),(456),(256),(365)(24)(65),(24)(35),$
 $(26),(12),(13),(23),(14),(15),(16),(24),(34),(12)(34),(12)(35),(12)(36),$
 $(12)(45),(12)(46),(34)(56),(13)(45),(13)(46),(13)(65),(32)(65),(13)(25),$
 $(13)(26),(35)(46),(62)(54),(14)(23),(14)(25),(14)(26),(14)(35),(14)(36),$
 $(36)(45),(62)(53),(14)(56),(15)(23),(15)(24),(15)(62),(15)(43),(13)(24),$
 $(25)(36),(15)(46),(15)(36),(16)(24),(16)(25),(12)(56),(25)(46),(62)(34)$
 $(16)(23),(16)(34),(16)(53),(23)(45),(23)(46),(42)(63), (25)(34)(1243),$
 $(1234),(1235),(1253),(1236),(1263),(1625),(1652),(1563),(1546),(1564),$
 $(1245),(1254),(1246),(1264),(1256),(1342),(1324),(1325),(1352),(1362),$
 $(1345),(1354),(1346)(1356),(1543),(1534),(1562),(1526),(1524),(1542),$
 $(35)(1432),(1523),(3245),(5136),(2365),(6354),(3645),(25),(1452),(1462),(1426),(1435),(1453),$
 $(1456),(1465),(1463),(1532),(1623),(1632),(1624),(1642),(1645),(1654),(3254),(1634),(1643),(16$
 $53),(2654),(5142),(6143),$
 $(2536),(2563),(5163),(6132),(4256),(2345),(2354),(2346),(2364),(2356),$
 $(3246),(3264),(3265),(2435),(2436),(4253),,(5264),(5246),(5263),(6254),(6245),(4263),(3456),(43$
 $56),(4365),(3465),(1243)(56),(1234)(56),(1235)$
 $(46),(1253)(46),(1236)(45),(1263)(45),(1564)(23),(1265)(34),(1345)(26),(1534)(26),(1625)(34),(1$
 $652)(34),(1536)(24), (1563)(24), (1546)(23),$
 $(1245)(36),(1254)(36),(1246)(35),(1264)(35), (1256)(34), (1342)(56),$
 $(1324)(56),(1325)(46),(1352)(46),(1362)(45), (1354)(26), (1346)(25),$
 $(1364)(25),(1356)(24),(1543)(26),(1562)(34), (1526)(34), (1524)(36),$
 $(1542)(36),(1423)(56),(1432)(56),(1456)(23),(1632)(45), (3245)(16),$
 $(6143)(25),(1452)(36),(1462)(35),(1426)(35),(1435)(26), (1453)(26),$
 $(1465)(23),(1463)(25),(1523)(46),(1532)(46), (1623)(45), (1624)(35),$
 $(1642)(35),(1645)(23),(1654)(23),(3254)(16),(1634)(25), (1643)(25),$
 $(1653)(24),(2654)(13),(5142)(36),(2536)(14),(2563)(14), (5136)(24),$
 $(5163)(24),(6132)(45),(4256)(13),(2365)(14),(4253)(16), (4263)(15),$
 $(3645)(12),(2345)(16),(2354)(16),(2346)(15),(2364)(15), (2356)(14),$
 $(3246)(15),(3264)(15),(3265)(14),(2435)(16),(2436)(15), (5264)(13),$
 $(5246)(13),(5263)(14),(6254)(13),(6245)(13),(3456)(12),(4356)(12),$
 $(4365)(12),(3465)(12),(6354)(12),(12345),(12354),(13254), (13245),$
 $(14352),(14325),(15234),(15243),(13542),(14523),(16243), (13642),$
 $(14623),(15263),(15324),(15342),(15423),(15432),(13425), (13452),$
 $(13524),(12453),(12435),(12534),(12543),(14235),(14253), (14532),$
 $(12346),(12364),(13264),(13246),(14362),(14326), (16234), (16324),$
 $(16342),(16423),(16432),(13426),(13462),(13624),(12463), (12436),$
 $(12634),(12643),(14236),(14263),(14632),(12365),(12356), (13256),$
 $(13265),(16352),(16325),(15236),(15326),(15362),(15623), (15632),$

(13625),(13652),(13526),(13562),(16523),(15246),(16542), (14526),
(15643),(13546),(12653),(12635),(12536),(12563),(16235) ,(16253),
(16532),(12645),(12654),(16254),(16245),(14652),(14625), (15264)
,(15624),(15642),(15426),(15462),(16425),(16452),(16524), (12456),
(12465),(12564),(12546),(14265),(14256),(14562),(16345), (16354),
(13654),(13645),(14356),(14365),(15634),(15364),(15346), (15463),
(15436),(13465),(13456),(13564),(16453),(16435),(16534), (16543),
(14635),(14653),(14536),(14563),(65243),(63542),(64523), (152346)
,(135246),(145326),(62345),(62354),(63254),(63245),(64352) ,(64325),
(65234),(65324),(65342),(65423),(65432),(63425),(63452), (63524),
(62453),(62435),(62534),(62543),(64235),(64253),(64532), (123456),
(123546),(132546),(132456),(143526),(143256),(153246),(153426),
(154236),(154326),(134256),(134526),(124536),(124356), (125346),
(125436),(142356),(142536),(123465),(123645),(132645), (132465),
(143625),(143265),(162345),(136245),(146325),(152364), (135264),
(135426),(163245),(163425),(164235),(164325),(134265), (134625),
(124635),(124365),(126345),(126435),(142365),(142635), (123654),
(123564),(132564),(132654),(163524),(163254),(153264), (153624),
(156234),(156324),(136254),(136524),(135624)(152634), (146235),
(136425),(162435),(145236),(126534),(126354),(125364), (125634),
(162354),(162534),(165324),(152463),(165243),(145623), (156342),
(135642),(126453),(126543),(162543),(146523),(146253), (152643),
(156243),(156423),(154263),(154623),(164253),(164523), (124563),
(124653),(125643),(125463),(142653),(142563),(163452), (163542),
(136542),(136452),(143562),(143652),(153642),(153462), (154632),
(154362),(134652),(134562),(164532),(164352),(165342), (165432),
(146352),(146532),(145632),(135462),(156432),(145263), (165423),
(624531),(12)(345),(12)(354),(13)(245),(13)(254),(14)(123),(14)(132),
(15)(243),(25)(134),(35)(642),(16)(243),(26)(134),(45)(623),(15)(234),
(23)(145),(23)(154),(24)(135),(24)(153),(25)(134),(34)(125),(34)(152),
(35)(124),(35)(142),(45)(123),(45)(132),(12)(346),(12)(364),(13)(246),
(13)(264),(14)(123),(14)(132),(16)(234),(23)(146),(23)(164),(24)(136),
(24)(163),(26)(134),(34)(126),(34)(162),(36)(124),(36)(142),(46)(123),
(46)(132),(12)(365),(12)(356),(13)(265),(13)(256),(16)(123),(16)(132),
(15)(263),(25)(136),(45)(632),(15)(246),(25)(164),(34)(625),(15)(236),
(23)(165),(23)(156),(26)(135),(26)(153),(25)(163),(36)(125),(36)(152),
(35)(126),(35)(162),(65)(123),(65)(132),(12)(645),(12)(654),(16)(245),
(16)(254),(14)(126),(14)(162),(15)(264),(26)(145),(26)(154),(24)(165),
(24)(156),(25)(164),(64)(125),(64)(152),(65)(124),(65)(142),(45)(126),
(45)(162),(16)(345),(16)(354),(13)(645),(13)(654),(14)(163),(14)(136),
(15)(643),(65)(134),(62)(345),(34)(652),(25)(634),(36),(46),(15)(634),
(63)(145),(63)(154),(64)(135),(64)(153),(65)(134),(34)(165),(34)(156),
(35)(164),(35)(146),(45)(163),(45)(136),(62)(354),(63)(245),(63)(254),
(64)(123),(64)(632),(65)(243),(65)(234),(23)(645),(23)(654),(24)(635),
(24)(653),(25)(634),(123)(456),(132)(456),(124)(356),(142)(356),(125)
(346),(152)(346),(153)(246),(164)(253),(164)(253),(142)(365), (126)
(345),(162)(345),(134)(256),(143)(256),(135)(246),(136)(245), (163)
(245),(145)(236),(154)(236),(146)(253),(156)(243),(165)(243)(123)(465),(132)(465),(124)(365),
(125)(364),(152)(364),(126)(354), (162)(354),
(134)(265),(143)(265),(154)(263),(152436),(23)(45)(16), (15)(23)(46),
(135)(264),(153)(264),(136)(254),(163)(254),(145)(263), (146)(235),

(164)(235),(156)(234),(165)(234),(35)(624),(145362),(652341),(25)(13)
 (46),(26)(15)(34),(1536),(1265),(1364) ,(36)(14)}
 , (S_6, o) is a symmetric group

Example(2-2):

The group , which has order 360 .
 Let $n = 6$, $r = 4$, $n-r=2$, $n!/r(n-r)! = 15$ cycle of two elements
 $360 = 4 \cdot 15 = 60$, clear $4 \nmid 90$
 $360 = 4 \cdot 90 = 4 \cdot 15 \cdot 6$
 have subgroups of order 4 , 15 and 6 .

Remarks(3-2):

There are 720 elements with identity of (S_6, o) of the form
 1) $n=6$, $r=2$, $n-r=4$ $(n!/r(n-r)!) = 15$ cycle of two elements.
 2) $n=6$, $r=3$, $n-r=3$ $(n!/r(n-r)!) = 40$ cycle of three elements.
 3) $n=6$, $r=4$, $n-r=2$ $(n!/r(n-r)!) = 90$ cycle of four elements.
 There are $(90/2)=45$ cycle of 2×2 elements.
 4) $n=6$, $r=5$, $n-r=1$ $(n!/r(n-r)!) = 144$ cycle of five elements.
 There are $(144/2) + (144/3)=120$ cycle of 2×3 elements.
 5) $n=6$, $r=6$, $n-r=0$ $(n!/r(n-r)!) = 120$ cycle of six elements.
 There are $(120/8) = 15$ cycle of $2 \times 2 \times 2$ elements.
 There are $(120/2) + (120/4)=90$ cycle of 2×4 elements.
 There are $(120/3) = 40$ cycle of 3×3 elements.

Some sub groups of a group (S_6, o) :

1) There are two sub groups of a group (S_6, o) which are:

(S_6, o) , $(\{i\}, o)$

2)The sub groups of (S_6, o) which has two elements are

$(\{i, (12)\}, o)$, $(\{i, (12)(34)\}, o)$, $(\{i, (12)(35)\}, o)$, $(\{i, (12)(34)(56)\}, o)$, $(\{i, (12)(46)\}, o)$,
 $(\{i, (13)\}, o)$, $(\{i, (12)(36)\}, o)$, $(\{i, (12)(45)\}, o)$, $(\{i, (16)\}, o)$, $(\{i, (13)(25)\}, o)$, $(\{i, (13)(45)\}, o)$, $(\{i, (13)(26)\}, o)$
 $(\{i, (13)(24)(56)\}, o)$, $(\{i, (13)(46)\}, o)$, $(\{i, (15)\}, o)$, $(\{i, (14)(35)\}, o)$,
 $(\{i, (13)(24)\}, o)$, $(\{i, (23)\}, o)$, $(\{i, (23)(15)(46)\}, o)$, $(\{i, (23)(54)\}, o)$, $(\{i, (23)(14)\}, o)$,
 $(\{i, (14)(23)(56)\}, o)$, $(\{i, (14)(56)\}, o)$, $(\{i, (14)(36)\}, o)$,
 $(\{i, (14)(25)\}, o)$, $(\{i, (14)(26)\}, o)$, $(\{i, (34)(16)(25)\}, o)$, $(\{i, (34)(56)\}, o)$, $(\{i, (35)\}, o)$, $(\{i, (12)(35)(46)\}, o)$, $(\{i, (24)\}, o)$, $(\{i, (24)(16)(35)\}, o)$, $(\{i, (35)(46)\}, o)$,
 $(\{i, (13)(25)(46)\}, o)$, $(\{i, (25)(36)\}, o)$, $(\{i, (45)\}, o)$,
 $(\{i, (16)(25)\}, o)$, $(\{i, (15)(24)(36)\}, o)$, $(\{i, (26)\}, o)$, $(\{i, (12)(36)(45)\}, o)$, $(\{i, (36)(45)\}, o)$,
 $(\{i, (25)\}, o)$, $(\{i, (23)(15)\}, o)$, $(\{i, (15)(24)\}, o)$, $(\{i, (15)(26)\}, o)$, $(\{i, (15)(34)\}, o)$,
 $(\{i, (26)(35)\}, o)$, $(\{i, (16)(23)(45)\}, o)$
 $(\{i, (23)(16)\}, o)$, $(\{i, (16)(34)\}, o)$, $(\{i, (16)(35)\}, o)$, $(\{i, (13)(26)(45)\}, o)$, $(\{i, (26)(54)\}, o)$,
 $(\{i, (14)(36)(25)\}, o)$, $(\{i, (15)(23)(46)\}, o)$, $(\{i, (46)\}, o)$, $(\{i, (23)(14)(56)\}, o)$, $(\{i, (56)\}, o)$,
 $(\{i, (26)(34)\}, o)$, $(\{i, (25)(46)\}, o)$,
 $(\{i, (15)(46)\}, o)$, $(\{i, (24)(36)\}, o)$, $(\{i, (24)(35)\}, o)$, $(\{i, (15)(36)\}, o)$, $(\{i, (12)(56)\}, o)$,
 $(\{i, (25)(34)\}, o)$, $(\{i, (23)(46)\}, o)$, $(\{i, (24)(56)\}, o)$,
 $(\{i, (34)\}, o)$, $(\{i, (16)(24)\}, o)$, $(\{i, (13)(65)\}, o)$, $(\{i, (23)(56)\}, o)$, $(\{i, (36)\}, o)$.

3)The sub groups of (S_6, o) which has three elements are;

$(\{i, (123), (132)\}, o)$, $(\{i, (124), (142)\}, o)$, $(\{i, (134), (143)\}, o)$,
 $(\{i, (234), (243)\}, o)$, $(\{i, (235), (253)\}, o)$, $(\{i, (345), (354)\}, o)$,
 $(\{i, (245), (254)\}, o)$, $(\{i, (125), (152)\}, o)$, $(\{i, (145), (154)\}, o)$,
 $(\{i, (135), (153)\}, o)$, $(\{i, (126), (162)\}, o)$, $(\{i, (146), (164)\}, o)$, $(\{i, (136), (163)\}, o)$,
 $(\{i, (236), (263)\}, o)$, $(\{i, (156), (165)\}, o)$, $(\{i, (246), (264)\}, o)$,
 $(\{i, (256), (265)\}, o)$, $(\{i, (346), (364)\}, o)$,
 $(\{i, (356), (365)\}, o)$, $(\{i, (456), (465)\}, o)$.

4)The sub groups of (S_6, o) which has four elements are

$\{i,(12),(34),(12)(34)\}, o, (\{i,(12),(35),(12)(35)\}, o), \{i,(12),(36),(12)(36)\}, o, (\{i,(12),(45),(12)(45)\}, o), (\{i,(13),(25),(13)(25)\}, o), \{i,(13),(45),(13)(45)\}, o, (\{i,(13),(26),(13)(26)\}, o), (\{i,(13),(46),(13)(46)\}, o), (\{i,(14),(35),(14)(35)\}, o), \{i,(13),(24),(13)(24)\}, o, \{i,(23),(54),(23)(54)\}, o, \{i,(23),(14),(23)(14)\}, o, (\{i,(14),(56),(14)(56)\}, o), (\{i,(14),(36),(14)(36)\}, o), (\{i,(14),(25),(14)(25)\}, o), (\{i,(14),(26),(14)(26)\}, o), (\{i,(34),(56),(34)(56)\}, o), (\{i,(35),(46),(35)(46)\}, o), (\{i,(25),(36),(25)(36)\}, o), (\{i,(16),(25),(16)(25)\}, o), (\{i,(36),(45),(36)(45)\}, o), (\{i,(23),(15),(23)(15)\}, o), (\{i,(15),(24),(15)(24)\}, o), (\{i,(15),(26),(15)(26)\}, o), (\{i,(15),(34),(15)(34)\}, o), (\{i,(26),(35),(26)(35)\}, o), (\{i,(23),(16),(23)(16)\}, o), (\{i,(16),(34),(16)(34)\}, o), (\{i,(16),(35),(16)(35)\}, o), (\{i,(26),(54),(26)(54)\}, o), (\{i,(26),(34),(26)(34)\}, o), (\{i,(25),(46),(25)(46)\}, o), (\{i,(15),(46),(15)(46)\}, o), (\{i,(24),(36),(24)(36)\}, o), (\{i,(24),(35),(24)(35)\}, o), (\{i,(15),(36),(15)(36)\}, o), (\{i,(12),(56),(12)(56)\}, o), (\{i,(25),(34),(25)(34)\}, o), (\{i,(23),(46),(23)(46)\}, o), (\{i,(24),(56),(24)(56)\}, o), (\{i,(16),(24),(16)(24)\}, o), (\{i,(13),(65),(13)(65)\}, o), (\{i,(23)(56)(23)(56)\}, o)$

5)The sub groups of a group $(S(6), o)$ with order five are:

$(\{i,(13),(24),(56),(13)(24)(56)\}, o), \{i,(23),(15),(46),(23)(15)(46)\}, o, (\{i,(34),(16),(25),(34)(16)(25)\}, o), \{i,(12),(35),(46),(12)(35)(46)\}, o, \{i,(24),(16),(35),(24)(16)(35)\}, o, (\{i,(13),(25),(46),(13)(25)(46)\}, o), (\{i,(14),(23),(56),(14)(23)(56)\}, o), (\{i,(15),(23),(46),(15)(23)(46)\}, o), (\{i,(15),(24),(36),(15)(24)(36)\}, o), (\{i,(14),(36),(25),(14)(36)(25)\}, o), (\{i,(12),(36),(45),(12)(36)(45)\}, o), (\{i,(23),(14),(56),(23)(14)(56)\}, o), (\{i,(16),(23),(45),(16)(23)(45)\}, o), (\{i,(13),(26),(45),(13)(26)(45)\}, o)$

6)The sub groups of (S_6, o) which has six elements are;

$(\{i,(23),(24),(34),(234),(243)\}, o), (\{i,(25),(35),(23),(235)(253)\}, o), (\{i,(25),(45),(24),(254),(245)\}, o), (\{i,(12),(14),(24),(124),(142)\}, o), (\{i,(15),(25),(12),(125),(152)\}, o), (\{i,(13),(14),(34),(134),(143)\}, o), (\{i,(15),(35),(13),(135),(153)\}, o), (\{i,(14),(15),(45),(145),(154)\}, o), (\{i,(12),(13),(23),(123),(132)\}, o), (\{i,(15),(25),(12),(125),(152)\}, o), (\{i,(13),(15),(35)(135),(153)\}, o), (\{i,(16),(26),(12),(126),(162)\}, o), (\{i,(13),(36),(16),(136),(163)\}, o), (\{i,(14),(16),(46),(146),(164)\}, o), (\{i,(16),(56),(15),(156),(165)\}, o), (\{i,(23),(26),(36),(236),(263)\}, o), (\{i,(24),(26),(46),(246),(264)\}, o), (\{i,(25),(26),(56),(256),(265)\}, o), (\{i,(34),(35),(45),(354),(345)\}, o), (\{i,(36),(46),(34),(346),(364)\}, o), (\{i,(35),(36),(56),(356),(365)\}, o), (\{i,(45),(46),(56),(456),(465)\}, o)$

7)The sub groups of (S_6, o) which has eight elements are;

$(\{i,(1234),(13)(24),(1432),(13),(24),(12)(34),(14)(23)\}, o), (\{i,(2345),(24)(35),(2543),(24),(35),(23)(45),(25)(34)\}, o), (\{i,(1245),(14)(25),(1542),(14),(25),(12)(45),(15)(24)\}, o), (\{i,(1345),(14)(35),(1543),(14),(35),(13)(45),(15)(34)\}, o), (\{i,(1235),(13)(25),(1532),(13),(25),(12)(35),(15)(23)\}, o), (\{i,(1236),(13)(26)\{1632,(13),(26),(12)(36),(16)(23)\}, o), (\{i,(1246),(16)(24),(1462),(16),(24),(12)(64),(14)(26)\}, o), (\{i,(1256),(15)(26),(1652),(15),(26),(12)(56),(16)(25)\}, o), (\{i,(1634),(13)(64),(1436),(13),(64),(16)(34),(14)(63)\}, o), (\{i,(1635),(13)(65),(1536),(13),(65),(16)(35),(15)(63)\}, o), (\{i,(1564),(16)(54),(1465),(16),(54),(15)(64),(14)(56)\}, o), (\{i,(2346),(63)(24),(6432),(63),(24),(62)(34),(64)(23)\}, o), (\{i,(6235),(63)(25),(6532),(13),(26),(62)(35),(65)(23)\}, o), (\{i,(6254),(63)(24),(6432),(63),(24),(62)(34),(64)(23)\}, o).$

8)The sub groups of (S_6, o) which has twelve elements are;

$\{i, (1234), (13)(24), (1432), (13)(24), (12)(34), (14)(23), (12)(34), (14)(23), (14)(23)\}, o$.
 $\{i, (2345), (24)(35), (2543), (24)(35), (23)(45), (25)(34), (23)(45), (25)(34)\}, o$.
 $\{i, (1245), (14)(25), (1542), (14)(25), (12)(45), (15)(24), (12)(45), (15)(24)\}, o$.
 $\{i, (1345), (14)(35), (1543), (14)(35), (13)(45), (15)(34), (13)(45), (15)(34)\}, o$.
 $\{i, (1235), (13)(25), (1532), (13)(25), (12)(35), (15)(23), (12)(35), (15)(23)\}, o$.
 $\{i, (1236), (13)(26), (1632), (13)(26), (12)(36), (16)(23), (12)(36), (16)(23)\}, o$.
 $\{i, (1246), (16)(24), (1462), (16)(24), (12)(64), (14)(26), (12)(64), (14)(26)\}, o$.
 $\{i, (1256), (15)(26), (1652), (15)(26), (12)(56), (16)(25), (12)(56), (16)(25)\}, o$.
 $\{i, (1634), (13)(64), (1436), (13)(64), (16)(34), (14)(63), (16)(34), (14)(63)\}, o$.
 $\{i, (1635), (13)(65), (1536), (13)(65), (16)(35), (15)(63), (16)(35), (15)(63)\}, o$.
 $\{i, (1564), (16)(54), (1465), (16)(54), (15)(64), (14)(56), (15)(64), (14)(56)\}, o$.
 $\{i, (2346), (63)(24), (6432), (63)(24), (62)(34), (64)(23), (62)(34), (64)(23)\}, o$.
 $\{i, (6235), (63)(25), (6532), (13)(26), (62)(35), (65)(23), (62)(35), (65)(23)\}, o$.
 $\{i, (6234), (63)(24), (6432), (63)(24), (62)(34), (64)(23), (62)(34), (64)(23)\}, o$.

9)The sub groups of (S_6, o) which has fifteen elements are;

$\{i, (1234), (13)(24), (1432), (13)(24), (12)(34), (14)(23), (12)(34), (14)(23), (13)(24), (1324)\}, o$.
 $\{i, (2345), (24)(35), (2543), (24)(35), (23)(45), (25)(34), (23)(45), (25)(34), (24)(35), (2435)\}, o$.
 $\{i, (1245), (14)(25), (1542), (14)(25), (12)(45), (15)(24), (12)(45), (15)(24), (14)(25), (1425)\}, o$.
 $\{i, (1345), (14)(35), (1543), (14)(35), (13)(45), (15)(34), (13)(45), (15)(34), (14)(35), (1435)\}, o$.
 $\{i, (1235), (13)(25), (1532), (13)(25), (12)(35), (15)(23), (12)(35), (15)(23), (13)(25), (1325)\}, o$.
 $\{i, (1236), (13)(26), (1632), (13)(26), (12)(36), (16)(23), (12)(36), (16)(23), (13)(26), (1326)\}, o$.
 $\{i, (1246), (16)(24), (1462), (16)(24), (12)(64), (14)(26), (12)(64), (14)(26), (16)(24), (1624)\}, o$.
 $\{i, (1256), (15)(26), (1652), (15)(26), (12)(56), (16)(25), (12)(56), (16)(25), (15)(26), (1526)\}, o$.
 $\{i, (1634), (13)(64), (1436), (13)(64), (16)(34), (14)(63), (16)(34), (14)(63), (13)(64), (1364)\}, o$.
 $\{i, (1635), (13)(65), (1536), (13)(65), (16)(35), (15)(63), (16)(35), (15)(63), (13)(65), (1365)\}, o$.
 $\{i, (1564), (16)(54), (1465), (16)(54), (15)(64), (14)(56), (15)(64), (14)(56), (16)(54), (1654)\}, o$.
 $\{i, (2346), (63)(24), (6432), (63)(24), (62)(34), (64)(23), (62)(34), (64)(23), (63)(24), (6324)\}, o$.
 $\{i, (6235), (63)(25), (6532), (13)(26), (62)(35), (65)(23), (62)(35), (65)(23), (63)(25), (6325)\}, o$.
 $\{i, (6234), (63)(24), (6432), (63)(24), (62)(34), (64)(23), (62)(34), (64)(23), (63)(24), (6324)\}, o$.

10)The sub groups of a group $(S(6), o)$ with order 24 are:

$\{i, (12), (13), (23), (14), (24), (34), (123), (132), (124), (243), (134), (143), (12)(34), (13)(24), (32)(14), (1234), (1243), (142), (234), (1324), (1342), (1423), (1432)\}, o$.
 $\{i, (12), (13), (23), (15), (25), (35), (123), (132), (125), (253), (135), (153), (12)(35), (13)(25), (32)(15), (1235), (1253), (152), (235), (1325), (1352), (1523), (1532)\}, o$.
 $\{(12), (13), (16), (23), (26), (36), (163), (136), (126), (162), (236), (263), (16)(23), (13)(26), (36)(12), (1632), (1623), (1326), (1362), (1236), (1362), (1263), (1236)\}, o$.
 $\{i, (12), (14), (24), (15), (25), (45), (124), (142), (125), (254), (145), (154), (12)(45), (14)(25), (42)(15), (1245), (1254), (152), (245), (1425), (1452), (1524), (1542)\}, o$.
 $\{i, (12), (16), (26), (14), (24), (64), (126), (162), (124), (246), (164), (146), (12)(64), (16)(24), (62)(14), (1264), (1246), (142), (264), (1624), (1642), (1426), (1462)\}, o$.
 $\{i, (12), (15), (16), (25), (26), (56), (165), (156), (126), (162), (256), (265), (16)$

,(25),(15)(26),(56)(12),(1652),(1625),(1526),(1562),(1256),(1562),(1265),(1256)},o).{i,(13),(14),(34),(15),(35),(45),(134),(143),(135), (354),(145)
 ,(154),(45),(14)(35),(43)(15),(1345),(1354),(153),(345),(1435),(1453)
 ,(1543)(1534), (13)}, o). { i,(14),(34),(16),(36),(46),(134),(143),(136),
 (364),(146),(1634), (1643),(164),(13),(46),(14)(36),(43)(16),(1346)
 ,(1364),(163),(346),(1436), (13),(1463)}, o). { i,(13),(15),(35),(16),
 (36),(56),(135),(153),(136),(365),(156),(165),(13),(56),(15)(36),(53)(16)
 ,(1356),(1365),(163),(356)(1536),(1563),(1635),(1653)}, o) { i,(14),(15),
 (45),(16),(46),(56),(145),(154),(146), (465),(156),(165),(14),(56),(15)(46)
 ,(54)(16),(1456),(1465),(164),(456),(1546),(1564),(1645),(1654)} , o)
 { i,(23),(24),(25),(34),(35),(45),(234),(243),(235),(253),(245),(254)
 ,(23),(45),(24)(35),(43)(25),(2345),(2354),(253),(235)(2435),(2453),
 (2534),(2543)},o).{i,(23),(24),(26),(34),(36),(46),(234),(243),(236),(263),
 (246),(264),(23),(46),(24)(36),(43)(26),(2346),(2364),(2634),(436)(463),(2463),(2436),(2643)} ,
 o). { i,(23),(25),(26),(35),(36),(56),(235),(253)
 ,(236),(263),(256),(265) ,(23),(56),(25)(36),(53)(26),(2356),(2365)
 ,(2635),(536),(563),(2563),(2536),(2653)},o).{
 i,(25),(24),(26),(54),(56),(46),(254),(245),(256),(265)
 ,(246),(264),(25),(46),(24)(56),(45)(26),(2546),(2564),(2654),(456),(465),(2465),(2456),(2645)},
 o). { i,(35),(34),(36),(54),(56),(46),(354),(345)
 ,(356),(365),(346),(364),(35),(46),(34)(56),(45)(36),(3546),(3564),(3654),(456),(465),(3465),
 (3456),(3645)}, o).

11)The sub groups of a group(S(6) ,o) with order 60 are:

- 1) {i,(12)(34),(125),(123), (124),(243),(134),(142),(234),(253),(135),
 (153),(152),(245),(354),(143),(235),(254),(145),(154),(345),(13)(24),
 (32)(14),(25)(34),(35)(24),(12)(35),(13)(25),(12)(45),(14)(25),(42)(15),
 (13)(45),(14)(35),(43)(15),(15)(23),(23)(45),(14352),(14325),(15234),
 (15243),(15324),(15342),(15423),(13425),(13452),(13524),(13542),
 (12453),(12435),(12534),(12543),(14235),(14253),(14532),(14523),
 (12345),(12354),(13254),(13245),(132)}
- 2) {i,(12)(34),(126),(123),(132),(124),(243),(134),(142),(234),(263),(136)
 ,(163),(162),(246),(364),(143),(236), (13264) ,(13)(24), (13624) ,(13246)
 (32)(14),(26)(34),(36)(24),(12)(36),(13)(26),(12)(46),(14)(26),(42)(16),
 (13)(46),(14)(36),(43)(16),(32)(16),(23)(46),(14362),(14326),(16234),
 (16243),(16324),(16342),(16423),(16432),(13426),(13462),(346) ,(164)
 ,(13642),(12463),(12436),(12634),(12643),(14236),(14263),(14632),
 (14623),(12346),(12364),(146), (264) }
- 3) { i,(12)(36),(125),(123),(132),(126),(263),(136),(162),(236),(253),
 (135),(153),(152),(265),(356),(163),(235),(256),(165),(156),(365),(13)(26),(32)(16),(25)(36),(35)(
 26),(12)(35),(13)(25),(12)(65),(16)(25),(62)(15),
 (13)(65),(16)(35),(63)(15),(32)(15),(23)(65),(16352),(16325),(15236),
 (15263),(15326),(15362),(15623),(15632),(13625),(13652),(13526),
 (13562),(12653),(12635),(12563),(16235),(16253),(16532),(16523),
 (12365),(12356),(13256),(13265), (12536) }
- 4) { i,(12)(64),(125),(126),(162),(124),(246),(164),(142),(264),(256)
 ,(165),(156),(152),(245),(654),(143),(265),(254),(145),(154),(645),
 (16)(24),(62)(14),(25)(64),(65)(24),(12)(65),(16)(25),(12)(45),(14)(25)
 ,(42)(15),(16)(45),(14)(65),(46)(15),(62)(15),(26)(45),(14652),(14625),
 (15264),(15246),(15624),(15642),(15426),(15462),(16425),(16452),
 (16524),(16542),(12456),(12465),(12564),(12546),(14265),(14256),
 (14562),(14526),(12645),(12654),(16254),(16245) }

5) { i, (16)(34),(165),(163),(136),(164),(643),(134),(142),(634),(653),
(135),(153),(156),(645),(354),(143),(635),(654),(145),(154),(345)
,(13)(64),(36)(14),(65)(34),(35)(64),(16)(35),(13)(65),(16)(45),(14)(65),
(46)(15),(13)(45),(14)(35),(43)(15),(36)(15),(63)(45),(14356),(14365),
(15634),(15643),(15364),(15346),(15463),(15436),(13465),(13456),
(13564),(13546),(16453),(16435),(16534),(16543),(14635),(14653),
(14536),(14563),(16345),(16354),(13654),(13645), }

6) { i, (62)(34), (625),(623), (632),(624),(243),(634),(642),(234),(253),
(635),(653),(652),(245),(354),(643),(235),(254),(645),(654),(345),
(63)(24),(32)(64),(25)(34),(35)(24),(62)(35),(63)(25),(62)(45),(64)(25),
(42)(65),(63)(45),(64)(35),(43)(65),(32)(65),(23)(45),(64352),(64325),
(65234),(65243),(65324),(65342),(65423),(65432),(63425),(63452),
(63524),(63542),(62453),(62435),(62534),(62543),(64235),(64253),
(64532),(64523),(62345),(62354), (63254),(63245) }

12)The sub groups of a group(S(6) ,o) with order 120 are:

1){i,(12),(13),(23),(14),(24),(34),(15),(35),(45),(12)(34),(125),(123),
,(124),(243),(134),(142),(234),(253),(135),(153),(152),(245),(354),(143)
,(235),(254),(145),(154),(345),,(13)(24),(32)(14),(25)(34),(35)(24),(12)
(35),(13)(25),(12)(45),(14)(25),(42)(15),(13)(45),(14)(35),(43)(15),(32)
(15),(23)(45),(14352),(14325),(15234),(15243),(15324),(15342),(15423),(25),(13425),(13452),(13
524),(13542),(12453),(12435),(12534),(12543),
(14235),(14253),(14532),(14523),(12345),(12354),(13254),(13245),,(12)
(345),(12)(354),(13)(245),(13)(254),(14)(532),(25)(134),(23)(154),(24)
(135),(25)(143),(14)(235),(45)(132),(35)(142),(15)(243),(15)(234),(23)
(145),(24)(153),(45)(123),(35)(124)(152)(34),(125)(34),(2354),(3245)
,(3254),(4253),(2435),(2345),(1234),(1324),(1342),(1423),(1432),(1253),(1254),(1523),(1532),(14
25),(1452),(1524),(1542),(1235),(1354),(1435),

(1453), (1534), (1543), (1345), (1325), (1352), (1245), (1243), (15432), (132) }

2) { i, (13), (23), (14), (24), (34), (16), (36), (46), (12)(34), (126), (123), (1243)
,(132),(124),(243),(134),(142),(234),(263),(136),(163),(162),(246),(364),
(143),(236),(264),(146),(164),(346),(13)(24),(32)(14),(26)(34),(36)(24),
(12),(36),(13)(26),(12)(46),(14)(26),(42)(16),(13)(46),(14)(36),(43)(16),
(32)(16),(23)(46),(14362),(14326), (16234),(16243), (16324),(16342),
(16423),(16432),(13426),(13462),(13624),(13642),(12463),(12436), (26)
(12634),(12643),(14236),(14263),(14632),(14623),(12346),(12364),(12)
(13264),(13246),(12)(346),(12)(364),(13)(246),(13)(264),(14)(632),(26)
(134),(23)(164),(24)(136),(26)(143),(14)(236),(46)(132),(36)(142),(16)
(243),(16)(234),(23)(146),(24)(163),(46)(123),(36)(124),(162)(34),(126)
(34),(2364),(3246),(3264), (4263),(2436) ,(2346)(1234),(1324),(1342),
,(1423),(1432),(1263),(1264),(1623),(1632),(1426),(1462),(1624),(1642),(1236),(1364),(1436),(14
63),(1634),(1643),(1346),(1326),(1362),(1246) }

3) { i,(12),(13),(23),(16),(26),(36),(15),(35),(45),(12)(36),(125),(123),
(132),(126),(263),(136),(162),(236),(253),(135),(153),(152),(265),(356)
,(163),(235),(256),(165),(156),(365),,(13)(26),(32)(16),(25)(36),(35)(26),
(12)(35),(13)(25),(12)(65),(16)(25),(62)(15),(13)(65),(16)(35),(63)(15),
(32),(15),(23)(65),(16352),(16325),(15236),(15263),(15326),(15362),
(15623),(15632),(13625),(13652),(13526),(13562),(12653),(12635),(125)(36),(12563),(16235),(1
6253),(16532),(16523),(12365),(12356),(13256),
(13265),,(12)(365),(12)(356),(13)(265),(13)(256),(16)(532),(25)(136),
(23)(156),(26)(135),(25)(163),(16)(235),(65)(132),(35)(162),(1263),(25)
(15)(236),(23)(165),(26)(153),(65)(123),(35)(126),(152)(36),(125)(36),

(2356),(3265),(3256),(6253),(2635),(2365),(1236),(1326),(1362),(1623),
 (1632),(1253),(1256),(1523),(1532),(1625),(1652),(1526),(1562),(1235),
 (1356),(1635),(1653),(1536),(1563),(1365),(1325),(1352),(1265),(15)(26)
 4) { i,(14),(24),(64),(15),(65),(45),(12)(64),(125),(126), (1245),(1246)
 (162),(124),(246),(164),(142),(264),(256),(165),(156),(152),(245),(654),
 (143),(265),(254),(145),(154),(645),,(16)(24),(62)(14),(25)(64),(65)(24),
 (12)(65),(16)(25),(12)(45),(14)(25),(42)(15),(16)(45),(14)(65),(46)(15),
 (62)(15),(26)(45),(14652),(14625),(15264),(15246),(15624),(15642), (25)
 (15426),(15462),(16425),(16452),(16524),(16542),(12456),(12465), (26)
 (12564),(12546),(14265),(14256),(14562),(14526),(12645),(12654), (12)
 (16254),(16245),,(12)(645),(12)(654),(16)(245),(16)(254),(14)(562), (16)
 (25)(164),(26)(154),(24)(165),(25)(146),(14)(265),(45)(162),(65)(142)
 ,(15)(246),(15)(264),(26)(145),(24)(156),(45)(126),(65)(124) ,(2645)
 (152)(64),(125)(64),(2654),(6245),(6254),(4256),(2465)(1264),(1624),
 (1642),(1426),(1462),(1256),(1254),(1526),(1562),(1425),(1452),(1524),
 (1542),(1265),(1654),(1465),(1456),(1564),(1546),(1645),(1625),(1652) }
 5) { i,(63),(14),(64),(34),(15),(35),(45), (16)(34), (165),(163) ,(1643)
 ,(136),(164),(643),(134),(142),(634),(653),(135),(153),(156),(645),(354)
 ,(143),(635),(654),(145),(154),(345),,(13)(64),(36)(14),(65)(34),(35)(64),
 (16)(35),(13)(65),(16)(45),(14)(65),(46)(15),(13)(45),(14)(35),(43)(15),
 (36)(15),(63)(45),(14356),(14365),(15634),(15643),(15364),(15346) ,(13)
 (15463),(15436),(13465),(13456),(13564),(13546),(16453),(16435), (16)
 (16534),(16543),(14635),(14653),(14536),(14563),(16345),(16354),(65)
 (13654),(13645),,(16)(345),(16)(354),(13)(645),(13)(654),(14)(536),(65)
 (134),(63)(154),(64)(135),(65)(143),(14)(635),(45)(136),(35)(146),(15)
 (643),(15)(634),(63)(145),(64)(153),(45)(163),(35)(164),(156)(34),(165)
 (34),(6354),(3645),(3654),(4653),(6435),(6345),(1634),(1364),(1346),
 (1463),(1436),(1653),(1654),(1563),(1536),(1465),(1456),(1564),(1546),
 (1635),(1354),(1435),(1453),(1534),(1543),(1345),(1365),(1356),(1645) }
 6) { i,(62),(63),(24),(65),(35),(45),(62)(34), (625),(623), (6243),(25)
 (632),(624),(243),(634),(642),(234),(253),(635),(653),(652),(245),(354),
 (643),(235),(254),(645),(654),(345),,(63)(24),(32)(64),(25)(34),(35)(24)
 ,(62)(35),(63)(25),(62)(45),(64)(25),(42)(65),(63)(45),(64)(35),(43)(65),
 (32)(65),(23)(45),(6432),(64325),(65234),(65243),(65324),(65342) ,(34)
 ,(65423),(65432),(63425),(63452),(63524),(63542),(62453),(62435) ,(64)
 ,(62534),(62543),(64235),(64253),(64532),(64523),(62345),(62354) ,(23)
 ,(63254),(63245),,(62)(345),(62)(354),(63)(245),(63)(254),(64)(532),(25)(634),(23)(654),(24)(635)
),(25)(643),(64)(235),(45)(632),(35)(642),(65)
 (243),(65)(234),(23)(645),(24)(653),(45)(623),(35)(624)(652)(34),(625)
 (34),(2354),(3245),(3254),(4253),(2435),(2345),(6234),(6324),(6342),
 (6423),(6432),(6253),(6254),(6523),(6532),(6425),(6452),(6524),(6542),
 (6235),(6354),(6435),(5453),(6534),(6543),(6345),(6325),(6352),(6245) }

13) The sub group of a group with order 360 are:

A={i,(123),(132),(124),(142),(125), (152),(126),(162),(345),(354)
 (134),(143),(135),(153),(136),(163),(145),(154),(346),(364),(146),(164),
 (156),(165),(234),(243),(235),(253),(356),(465),(236),(263),(245),(254),
 (246),(264),(265),(456),(256),(365)(26),(12),(13),(23),(14),(15),(16),(24),(34),(25),(56),(46),(123
 45),(12354),(13254),(13245),(14352),(14325),
 (15234),(15243),(13542),(14523),(16243),(13642),(14623),(15263),
 (15324),(15342),(15423),(15432),(13425),(13452),(13524),(12453),
 (12435),(12534),(12543),(14235),(14253),(14532),(12346),(12364),

(13264),(13246),(14362),(14326),(16234),(16324),(16342),(16423),
(16432),(13426),(13462),(13624),(12463),(12436),(12634),(12643),
(14236),(14263),(14632),(12365),(12356),(13256),(13265),(16352),
(16325),(15236),(15326),(15362),(15623),(15632),(13625),(13652),
(13526),(13562),(16523),(15246),(16542),(14526),(15643),(13546),
(12653),(12635),(12536),(12563),(16235),(16253),(16532),(12645),
(12654),(16254),(16245),(14652),(14625),(15264),(15624),(15642),
(15426),(15462),(16425),(16452),(16524),(12456),(12465),(12564),
(12546),(14265),(14256),(14562),(16345),(16354),(13654),(13645),
(14356),(14365),(15634),(15364),(15346),(15463),(15436),(13465),
(13456),(13564),(16453),(16435),(16534),(16543),(14635),(14653),
(14536),(14563),(65243),(63542),(64523),(62345),(62354),(63254),
(63245),(64352),(64325),(65234),(65324),(65342),(65423),(65432),
(63425),(63452),(63524),(62453),(62435),(62534),(62543),(64235),
(13)(245),(13)(254),(14)(523),(14)(532),(15)(243),(25)(134),(35)(642),
(16)(243),(26)(134),(45)(623),(15)(234),(23)(145),(23)(154),(24)(135),
(24)(153),(25)(134),(34)(125),(34)(152),(35)(124),(35)(142),(45)(123),
(45)(132),(12)(346),(12)(364),(13)(246),(13)(264),(14)(123),(14)(132),
(16)(234),(23)(146),(23)(164),(24)(136),(24)(163),(26)(134),(34)(126),
(34)(162),(36)(124),(36)(142),(46)(123),(46)(132),(12)(365),(12)(356),
(13)(265),(13)(256),(16)(123),(16)(132),(15)(263),(25)(136),(45)(632),
(15)(246),(25)(164),(34)(625),(15)(236),(23)(165),(23)(156),(26)(135),
(26)(153),(25)(163),(36)(125),(36)(152),(35)(126),(35)(162),(65)(123),
(65)(132),(12)(645),(12)(654),(16)(245),(16)(254),(14)(126),(14)(162),
(15)(264),(26)(145),(26)(154),(24)(165),(24)(156),(25)(164),(64)(125),
(64)(152),(65)(124),(65)(142),(45)(126),(45)(162),(16)(345),(16)(354),
(13)(645),(13)(654),(14)(163),(14)(136),(15)(643),(65)(134),(62)(345),
(34)(652),(25)(634),(36),(46),(15)(634),(63)(145),(63)(154),(64)(135),
(64)(153),(65)(134),(34)(165),(34)(156),(35)(164),(35)(146),(45)(163),
(45)(136),(62)(354),(63)(245),(63)(254),(64)(123),(64)(632),(65)(243),
(65)(234),(23)(645),(23)(654),(24)(635),(24)(653),(25)(634),(123)(456),
(132)(456),(124)(356),(142)(356),(125)(346),(152)(346),(153)(246),
(164)(253),(164)(253),(142)(365),(126)(345),(162)(345),(134)(256),
(143)(256),(135)(246),(136)(245), (64253),(64532),(12)(345),(12)(354),
(163)(245),(145)(236),(154)(236),(146)(253),(156)(243),(165)(243),
(123)(465),(132)(465),(124)(365),(125)(364),(152)(364),(126)(354),
(162)(354),(134)(265),(143)(265),(154)(263),(135)(264),(153)(264),
(136)(254),(163)(254),(145)(263),(146)(235),(164)(235),(156)(234),
(165)(234),(46)}

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