

-1961)

.(2002

Limit)

(K) (LIML)(Information Maximum Likelihood
(K-Class) (K-Class estimator)

(SAS.9)

**Estimating Simultaneous Equations System of the
World Prices of the Grains for the Period (1961-2002)**

ABSTRACT:-

The work in this paper estimates the simultaneous equations of the grains for the period (1961-2002).The estimation necessitate dealing with the variables that have direct effects on the world prices of the grains and then adding the economic crises to the system, which is finance and monetary crises, petrolic shocks, wars, and curtness. For estimation we have used limit information maximum likelihood (LIML) and K-Class estimator (K-Class). We depended on the results of the last method because it is more accurate and efficiently with the

تاريخ التسلم : 2007/10/ 22 تاريخ القبول : 2007/12/ 12

economic and statistic theory. The (SAS.9) Package is used to obtain the results.

-:

(Linear Regression)

(Causality)

(Dependent Variable)

(Explanatory Variables)

(2005) (Simultaneous Equation)

()

(2005)

(OLS) (Ordinary Least Squares)

.

()

(Biased)

(OLS)

(1998) (Unconsistent)

K-) (K)

(LIML)

.(Class

-1 -:

.(1978)

1-1 -:

.(1998)

K-) (LIML)

(CLASS

(Limit Information Maximum Likelihood)(LIML)-:

Least Variance) ()

(LVR) (Ratio

.(LISE) (Limited Information Single Equation)

(Consistent)

(LIML)

(Maximum Likelihood Function)

.(Intriligator,etal.,1996)

-(Koutsoyiannis,1987)

$$y_1 = \beta_2 y_2 + \gamma_1 x_1 + \gamma_2 x_2 + \varepsilon_1 \dots(1)$$

-:

- : y's

- : x's

- : \beta's

- : \gamma's

-: ε_1 (σ^2)

-:

$$\beta_1 y_1 - \beta_2 y_2 = \gamma_1 x_1 + \gamma_2 x_2 + \varepsilon_1 \dots (2)$$

 $(\beta_1 = 1)$

-:

$$y_2 = f(y_1, y_3, x_1, x_2, \dots) \dots (3)$$

 $(\beta_2 = 1)$

-:

$$y_1 = \pi_{11}x_1 + \pi_{12}x_2 + \pi_{13}x_3 + \pi_{14}x_4 + u_1 \dots (4)$$

$$y_2 = \pi_{21}x_1 + \pi_{22}x_2 + \pi_{23}x_3 + \pi_{24}x_4 + u_2 \dots (5)$$

-:

-: π^s -: u^s (OLS) (β_2) (β_1)

-:

$$\beta_1 y_1 + \beta_2 y_2 = \beta_1 (\pi_{11}x_1 + \pi_{12}x_2 + \pi_{13}x_3 + \pi_{14}x_4) + \beta_2 (\pi_{21}x_1 + \pi_{22}x_2 + \pi_{23}x_3 + \pi_{24}x_4) + (\beta_1 u_1 + \beta_2 u_2) \dots (6)$$

$$\begin{array}{l}
 (\beta_1 \mathbf{u}_1 + \beta_2 \mathbf{u}_2) \\
 (\mathbf{y}_1, \mathbf{y}_2) \quad \text{(Unexplained Variation)}
 \end{array}$$

-:

$$\sum_{i=1}^n (\beta_1 \mathbf{u}_{1i} + \beta_2 \mathbf{u}_{2i})^2 = \sum_{i=1}^n (\beta_1^2 \mathbf{u}_{1i}^2 + \beta_2^2 \mathbf{u}_{2i}^2 + 2\beta_1 \mathbf{u}_{1i} \beta_2 \mathbf{u}_{2i}) \dots (7)$$

($\mathbf{y}_1, \mathbf{y}_2$)

-:

$$\beta_1^2 \sum \mathbf{u}_{1i}^2 + \beta_2^2 \sum \mathbf{u}_{2i}^2 + 2\beta_1 \beta_2 \sum \mathbf{u}_{1i} \mathbf{u}_{2i} \dots (8)$$

(\mathbf{u}_2) (\mathbf{u}_1)

$$\text{-:} \quad (8) \quad (\hat{\mathbf{u}}_2) \quad (\hat{\mathbf{u}}_1)$$

$$\beta_1^2 \sum \hat{\mathbf{u}}_{1i}^2 + \beta_2^2 \sum \hat{\mathbf{u}}_{2i}^2 + 2\beta_1 \beta_2 \sum \hat{\mathbf{u}}_{1i} \hat{\mathbf{u}}_{2i} \dots (9)$$

(\mathbf{y} 's)

(\mathbf{x} 's)

(1)

$$\text{-:} \quad (\mathbf{x}_2) \quad (\mathbf{x}_1)$$

$$\mathbf{y}_1 = \pi_{11}^* \mathbf{x}_1 + \pi_{12}^* \mathbf{x}_2 + \mathbf{w}_1 \dots (10)$$

$$\mathbf{y}_2 = \pi_{21}^* \mathbf{x}_1 + \pi_{22}^* \mathbf{x}_2 + \mathbf{w}_2 \dots (11)$$

(10) (OLS)

$$\text{-:} \quad (\beta_2) \quad (\beta_1) \quad (11)$$

$$\begin{aligned}
 \beta_1 \mathbf{y}_1 + \beta_2 \mathbf{y}_2 = & \beta_1 (\pi_{11}^* \mathbf{x}_1 + \pi_{12}^* \mathbf{x}_2) + \beta_2 (\pi_{21}^* \mathbf{x}_1 + \pi_{22}^* \mathbf{x}_2) \\
 & + (\beta_1 \mathbf{w}_1 + \beta_2 \mathbf{w}_2) \dots (12)
 \end{aligned}$$

($\beta_1 \mathbf{w}_1 + \beta_2 \mathbf{w}_2$)

(\mathbf{y}_2) (\mathbf{y}_1)

$$\text{-:} \quad (\mathbf{x}_2) \quad (\mathbf{x}_1)$$

$$\sum (\beta_1 \mathbf{w}_{1i} + \beta_2 \mathbf{w}_{2i})^2 = \beta_1^2 \sum \mathbf{w}_{1i}^2 + \beta_2^2 \sum \mathbf{w}_{2i}^2 + 2\beta_1 \beta_2 \sum \mathbf{w}_{1i} \mathbf{w}_{2i} \dots (13)$$

$$\beta_2(\sum \hat{w}_{2i}^2 - I\sum \hat{u}_{2i}^2) + \beta_1(\sum \hat{w}_{1i}\hat{w}_{2i} - I\sum \hat{u}_{1i}\hat{u}_{2i}) = 0 \dots(19)$$

$$\beta_1 = \beta_2 = 0 \quad (19) \quad (18)$$

-:

$$\begin{vmatrix} (\sum \hat{w}_{1i}^2 - I\sum \hat{u}_{1i}^2) & (\sum \hat{w}_{1i}\hat{w}_{2i} - I\sum \hat{u}_{1i}\hat{u}_{2i}) \\ (\sum \hat{w}_{1i}\hat{w}_{2i} - I\sum \hat{u}_{1i}\hat{u}_{2i}) & (\sum \hat{w}_{2i}^2 - I\sum \hat{u}_{2i}^2) \end{vmatrix} = 0 \dots(20)$$

-:

$$(\beta_1 \neq 0, \beta_2 \neq 0)$$

$$(\sum \hat{w}_1^2 - I\sum \hat{u}_1^2)(\sum \hat{w}_2^2 - I\sum \hat{u}_2^2) - (\sum \hat{w}_1\hat{w}_2 - I\sum \hat{u}_1\hat{u}_2)^2 = 0 \dots(21)$$

-:

$$(21)$$

$$AI^2 + BI + C = 0 \dots(22)$$

-:

$$A = \sum \hat{u}_1^2 \sum \hat{u}_2^2 - (\sum \hat{u}_1\hat{u}_2)^2$$

$$B = 2\sum \hat{w}_1\hat{w}_2 \sum \hat{u}_1\hat{u}_2 - \sum \hat{w}_2^2 \sum \hat{u}_1^2 - \sum \hat{w}_1^2 \sum \hat{u}_2^2$$

$$C = \sum \hat{w}_1^2 \sum \hat{w}_2^2 - (\sum \hat{w}_1\hat{w}_2)^2$$

$$(I) \quad (22)$$

$$(I)$$

$$(\beta_1 = 1)$$

$$(I)$$

$$(\beta's)$$

$$(3) \quad (1)$$

$$(\beta's)$$

$$(\gamma's)$$

(OLS)

.($\gamma's$)

:(K-Class estimator) K

(K-Class)

k (2SLS) (Two stage least squares)

∴

$$y_1 = Y_1\beta_1 + X_1\gamma_1 + \varepsilon \dots(23)$$

(y₁)

(X₁) (Y₁)

∴(y₁)

(k-class)

∴

$$\begin{bmatrix} \hat{\beta}_1 \\ \hat{\gamma}_1 \end{bmatrix} = \begin{bmatrix} Y_1'Y_1 - k\hat{u}_1'\hat{u}_1 & Y_1'X_1 \\ X_1'Y_1 & X_1'X_1 \end{bmatrix}^{-1} \begin{bmatrix} Y_1' - k\hat{u}_1' \\ X_1' \end{bmatrix} y_1 \dots(24)$$

(Y₁)

(u₁)

(k-class)

k=0

(k-class)

k=1

(OLS)

∴(Intriligator,etal.,1996) (2SLS)

∴

-2

(2002-1961)

∴(2005)

$$Y_1 = a_0 + a_1 Y_2 + a_2 Y_3 + a_3 Y_4 + a_4 X_1 + a_5 X_2 + a_6 X_3 + a_7 X_4 + a_8 X_{17} + a_9 X_{18} + a_{10} X_{19} + a_{11} X_{20} + a_{12} X_{21} + a_{13} X_{22} + a_{14} X_{23} \dots (25)$$

$$Y_2 = b_0 + b_1 Y_1 + b_2 Y_3 + b_3 Y_4 + b_4 X_5 + b_5 X_6 + b_6 X_7 + b_7 X_8 + b_8 X_{17} + b_9 X_{18} + b_{10} X_{19} + b_{11} X_{20} + b_{12} X_{21} + b_{13} X_{22} + b_{14} X_{23} \dots (26)$$

$$Y_3 = c_0 + c_1 Y_1 + c_2 Y_2 + c_3 Y_4 + c_4 X_9 + c_5 X_{10} + c_6 X_{11} + c_7 X_{12} + c_8 X_{17} + c_9 X_{18} + c_{10} X_{19} + c_{11} X_{20} + c_{12} X_{21} + c_{13} X_{22} + c_{14} X_{23} \dots (27)$$

$$Y_4 = d_0 + d_1 Y_1 + d_2 Y_2 + d_3 Y_3 + d_4 X_{13} + d_5 X_{14} + d_6 X_{15} + d_7 X_{16} + d_8 X_{17} + d_9 X_{18} + d_{10} X_{19} + d_{11} X_{20} + d_{12} X_{21} + d_{13} X_{22} + d_{14} X_{23} \dots (28)$$

-:

.	-: Y ₂	.	-: Y ₁
.	-: Y ₄	.	-: Y ₃
.	-: X ₂	.	-: X ₁
.	-: X ₄	.	-: X ₃
.	-: X ₆	.	-: X ₅
.	-: X ₈	.	-: X ₇
.	-: X ₁₀	.	-: X ₉
.	-: X ₁₂	.	-: X ₁₁
.	-: X ₁₄	.	-: X ₁₃
.	-: X ₁₆	.	-: X ₁₅
.	-: X ₁₈	.	-: X ₁₇
.	-: X ₂₀	.	-: X ₁₉
.	-: X ₂₁	.	
.	-: X ₂₃	.	-: X ₂₂

... [217]
(Y₁, Y₂, Y₃, Y₄) (28) (25)

(LIML) (K-class) (2SLS)
(K-Class) (LIML) (2SLS)
(LIML) (1) : 1-2
(K-Class) (K-Class) (LIML)
(K-Class) (LIML)
F t (LIML)
(K-Class) (K-Class)

(2002-1961)

SAS .(9.0)

-(Y₁) -

(Y₂, Y₃, X₂, X₃)

(Y₂) (-15.5618) (Y₃)

(0.098669) (0.894452)

(0.894452)

(0.098669)

(-1.16208) (X₂)

(X₃) .(1.491778)

(t)

(F) (5%) (F)

(1%)

.(95%)

... [219]
 (Y₃, Y₄, X₇) -:(Y₂) -
 (Y₄) (Y₃)
 (0.458869) (0.140289)
 (X₇)
 (t) .(0.504039)
 (1%)
 (F) (F) (1%)
 .(81%)
 -:(Y₃) -
 (Y₁, X₉)
 (Y₁)
 (X₉) (2.358307)
 .(-0.5039)
 (43.10446) (X₂₃)
 (Y₂) (Y₁) (Y₂)
 .(2.717747)
 " (t)
 (5%)

[220]

المجلة العراقية للعلوم الاحصائية (14) 2008

(1%)	(F)	(F)
.(70%)		
	-(Y ₄)	-
		(Y ₁ , Y ₂ , X ₁₇ , X ₁₈ , X ₁₉)
	(Y ₂)	(Y ₁)
	(0.276298)	(0.203755)
(X ₁₇)		.
	(0.039585)	
	(X ₁₈)	
(X ₁₉)		(0.134601)
	. (-11.9584)	
	(t)	
	(5%)	
	(F)	(F)
.(87%)		(1%)

...

(LIML)

:(1)

(K-Class)

(2002-1961)

Methods	Dependent Variable	Variables	Parameter Estimate	Standard Error	t Value	Pr > t	k-class	F Value	Pr > F	R-Square	Adj R-Sq
Limited-Information Maximum Likelihood Estimation	Y ₁	Intercept	-15.2808	12.0022	-1.27	0.2109	-	74.36	<.0001	0.88937	0.87741
		Y ₂	1.604662	0.76169	2.11	0.042					
		Y ₃	-0.05353	0.2067	-0.26	0.7971					
		X ₂	-0.84277	0.83604	-1.01	0.32					
		X ₃	0.85806	0.97323	0.88	0.3837					
	Y ₂	Intercept	-123.758	358.736	-0.34	0.732	-	2.85	0.05	0.18391	0.11948
		Y ₃	0.672233	1.35836	0.49	0.6235					
		Y ₄	1.728408	4.52316	0.38	0.7045					
		X ₇	-1.32268	5.29758	-0.25	0.8042					
	Y ₃	Intercept	114.8715	30.0884	3.82	0.0005	-	23.63	<.0001	0.54788	0.5247
		Y ₁	2.085003	0.34399	6.06	<.0001					
		X ₉	-0.40805	0.15645	-2.61	0.0128					
	Y ₄	Intercept	-499.027	178.441	-2.8	0.0082	-	40.17	<.0001	0.848	0.82689
		Y ₁	0.091744	0.16252	0.56	0.5759					
		Y ₂	0.565958	0.25346	2.23	0.0319					
		X ₁₇	0.044724	0.00815	5.49	<.0001					
X ₁₈		0.177669	0.05965	2.98	0.0052						
X ₁₉		-15.6949	4.5878	-3.42	0.0016						
K-Class Estimator	Y ₁	Intercept	-15.5618	5.50502	-2.83	0.0075	0.714285714	205.7	<.0001	0.95697	0.95231
		Y ₂	0.894452	0.0974	9.18	<.0001					
		Y ₃	0.098669	0.02435	4.05	0.0002					
		X ₂	-1.16208	0.55668	-2.09	0.0438					
		X ₃	1.491778	0.56946	2.62	0.0127					
	Y ₂	Intercept	-3.50184	8.34363	-0.42	0.6771	0.714285714	62.58	<.0001	0.83167	0.81838
		Y ₃	0.140289	0.02404	5.84	<.0001					
		Y ₄	0.458869	0.14896	3.08	0.0038					
		X ₇	0.504039	0.1218	4.14	0.0002					
	Y ₃	Intercept	108.3656	29.1153	3.72	0.0006	0.6	57.31	<.0001	0.74613	0.73311
		Y ₁	2.358307	0.23144	10.19	<.0001					
		X ₉	-0.5039	0.12753	-3.95	0.0003					
	Y ₃ *	Intercept	72.90727	31.3815	2.32	0.0256	0.6	33.41	<.0001	0.72508	0.70338
		Y ₂	2.717747	0.35293	7.7	<.0001					
		X ₉	-0.31188	0.13062	-2.39	0.022					
		X ₂₃	43.10446	19.0963	2.26	0.0298					
	Y ₄	Intercept	-364.383	150.211	-2.43	0.0204	0.714285714	57.87	<.0001	0.88936	0.87399
		Y ₁	0.203755	0.07838	2.6	0.0134					
		Y ₂	0.276298	0.1073	2.58	0.0143					
X ₁₇		0.039585	0.00708	5.59	<.0001						
X ₁₈		0.134601	0.05058	2.66	0.0116						
X ₁₉		-11.9584	3.8195	-3.13	0.0035						

∴ Y₃*

(X₂₃)

-:

-:

(1)

(2)

-:

-

-

(3)

(43.10446) (X₂₃)

(Y₁)

(Y₂)

...

-:

(FIML) (3SLS)

-:

":(2005) (1

"(2002-1961)

"(1978) (2

.38

"

":(1998) (3

.520

"

" .(2005) (4

.258

- 5) Intrilligator, M.D.; Bodkin,R.G. and Hsiao,C. (1996). "Econometrics Models, Techniques and Applications", Prentice Hall.pp.368-369.
- 6) Koutsoyiannis, A. (1987). "Theory of Econometrics", 2nd ed. MaCmillan Education LTD. pp.454-457.