

دراسة العوامل المؤثرة على أداء الطالب باستخدام تحليل الارتباط القوييم

Canonical Correlation Analysis

$$Y_{ij} \quad X_{ij} \quad (\quad)$$

Abstract

Student performance may influence by several factors in all his study levels such as primary school, intermediate school and even in his collage; some of these factors are psychological factors, social factors, and the factors which correlate with student environament.

In this paper we study some of these factors to discover their influence by using canonical correlation analysis which is defined as a correlation that determine the relationship between two groups of variables by seeking the linear structure for original variables that has the maximum correlation, to analyze the data. Many conclusions are discovered to help who focuses student performance or to make it pest in future.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} -$$

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Canonical Correlation Analysis

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$Y_{ij} \quad X_{ij}$$

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[1][2][4] Canonical Correlation

$$(X)$$

$$(Y)$$

$$\begin{matrix} (q) & & (p) & & (n) \\ & P \geq q & n \geq p+q & & \end{matrix}$$

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$$X = x_{ij} \quad i = 1, 2, \dots, n \quad j = 1, 2, \dots, p$$

$$Y = y_{ik} \quad i = 1, 2, \dots, n \quad k = 1, 2, \dots, q$$

$$v = \underline{d}'Y \quad u = \underline{c}'X$$

$$\underline{d} \quad \underline{c}'$$

$$R \quad R = \min(p, q)$$

$$v \quad u$$

[1][2][4]

$$(M - \lambda I)d = 0 \dots\dots\dots(1)$$

$$M = S_{yy}^{-1}S_{yx}S_{xy}^{-1}S_{xy} \dots\dots\dots(2)$$

$$S_{XX}^{-1}S_{XY}S_{YY}^{-1}S_{YX} - \lambda I \dots\dots\dots(3)$$

$$S_{yy}^{-1}S_{yx}S_{xx}^{-1}S_{yy} - \lambda I \dots\dots\dots(4)$$

$$P \leq q$$

$$q \leq P$$

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X	Var-Cov	-: S _{xx}
Y	Var-Cov	-: S _{yy}
XY	Var-Cov	-: S _{xy}

[1][2]

$$H_{\circ} : R_{XY} = 0$$

$$H_1 : R_{XY} \neq 0$$

$$\chi^2$$

$$\chi_{cal}^2 = [-n + 0.5(P + q + 3)]Logw \dots\dots(5)$$

Wilk

w

$$Wilks \leftarrow W = \prod_{Zzi}^r (1 - R^2_{cz}) \dots\dots\dots(6)$$

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:R²c_z

[1][2] Structure Coefficients

Structure

(- +)

Coefficients

R_{yy}, R_{xx}

(+1,-1)

[1][2] Adequacy Coefficient

	Y1		X1
	Y2		X2
	Y3		X3
	Y4		X4
	Y5		X5
	Y6		X6
	Y7		X7

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	Y8		X8
	Y9		X9
	Y10		X10
	Y11		X11
	Y12		X12
			X13
			X14

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	Y1		X1
	Y2		X2
	Y3		X3
	Y4		X4
	Y5		X5
	Y6		X6
	Y7		X7
	Y8		X8
	Y9		X9
			X10
			X11
			X12
			X13
			X14
			X15
			X16
			X17
			X18

Statistica

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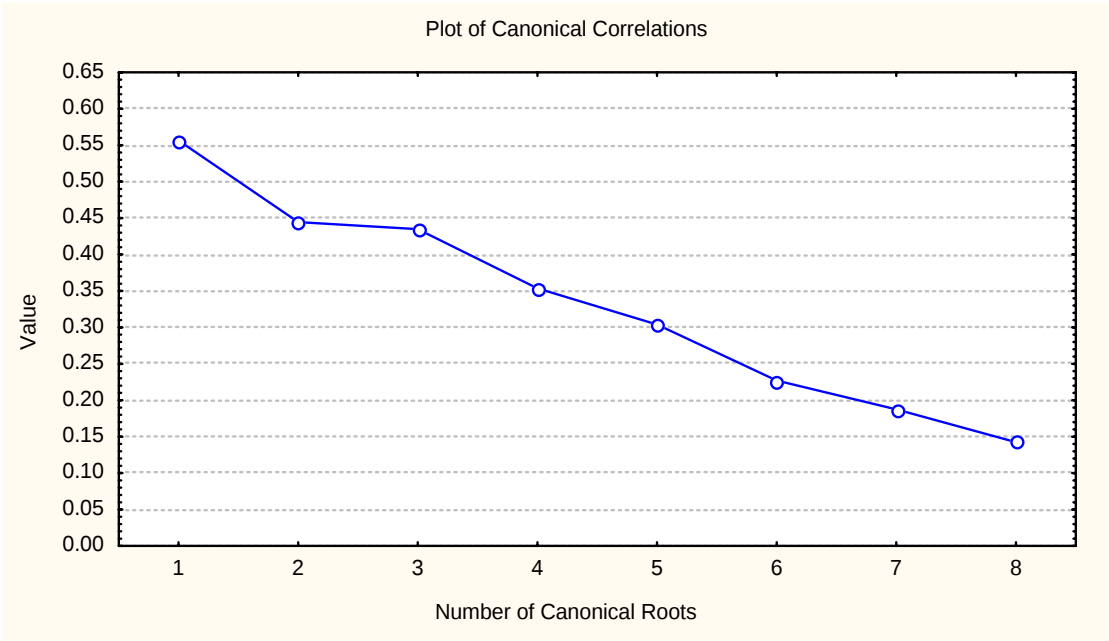
12.66196	74.91	Y1	9.627502	4.91	X1
12.90769	67.76	Y2	9.613096	4.95	X2
13.82317	65.03	Y3	9.610579	5.02	X3
13.54475	66.88	Y4	9.613564	4.94	X4
14.90219	70.16	Y5	9.925678	1.81	X5
13.79571	71.04	Y6	9.611919	4.93	X6
13.12985	72.53	Y7	9.616122	4.93	X7
13.73817	73.5	Y8	9.877119	2.59	X8
			9.745841	3.78	X9
			9.644405	4.66	X10
			9.622679	4.9	X11
			9.90302	1.97	X12
			9.901515	1.98	X13
			9.883539	2.25	X14

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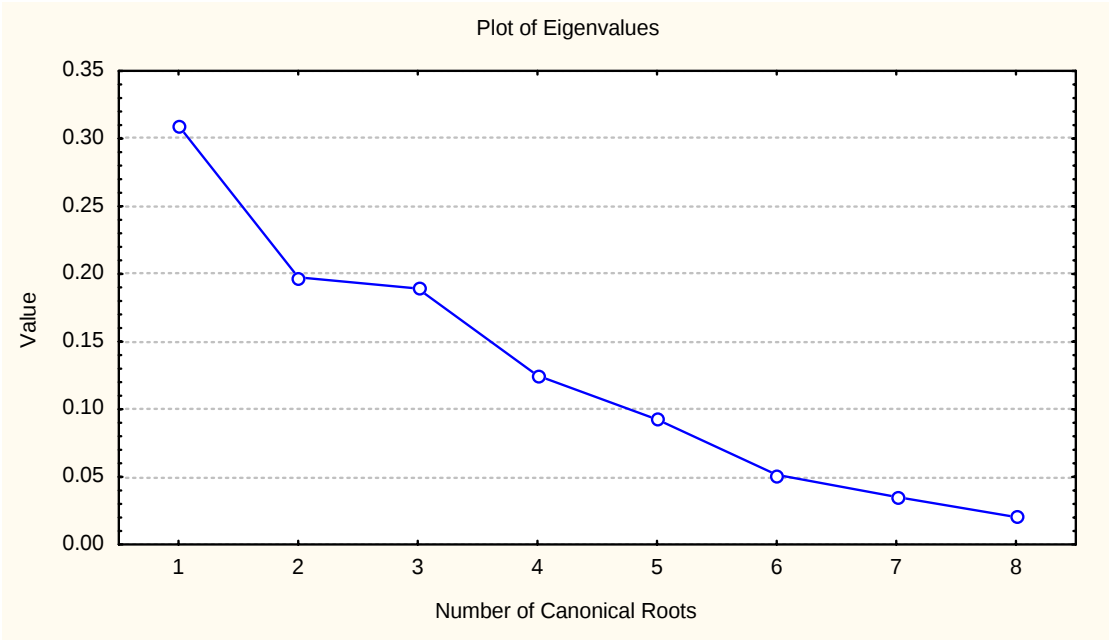
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Canonical R	Eigenvalues
0.55642	0.309603
0.444444	0.19753
0.434977	0.189205
0.353426	0.12491
0.303979	0.092403
0.226872	0.051471
0.187424	0.035128
0.142413	0.020281

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(99.72951)

χ^2

(0.55642)

(112)

Y X

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χ^2

Canonical R	Canonical R-sqr.	Chi-sqr.	Df
0.55642	0.309603	99.72951	112
0.444444	0.19753	67.31173	91
0.434977	0.189205	48.05639	72
0.353426	0.12491	29.70416	55
0.303979	0.092403	18.02915	40
0.226872	0.051471	9.54557	27
0.187424	0.035128	4.92182	16
0.142413	0.020281	1.79287	7

(% ,) X

X

Y

(X)

-(Y)

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13.69939		X1
12.1691		X5
11.7585		X6
7.024981		X2
5.48581		X4
4.780976		X8
4.771481		X12
		X7
4.400805		
3.1531		X13
3.05372		X9
2.783029		X11
2.45469		X10
2.15549		X3
1.22197		X14

X1)

) X6 () X5 ()

() X4 () X2 () X8
) X7 () X12 ()
X1

X6 X5
X4 X2
X7 X12 X8

) X14 X3 X10 X11
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0.8184771		Y4
0.8072899		Y6
0.5653906		Y7
0.5608076		Y5
0.3535092		Y1
0.244349		Y2
0.158985		Y8
0.0305101		Y3

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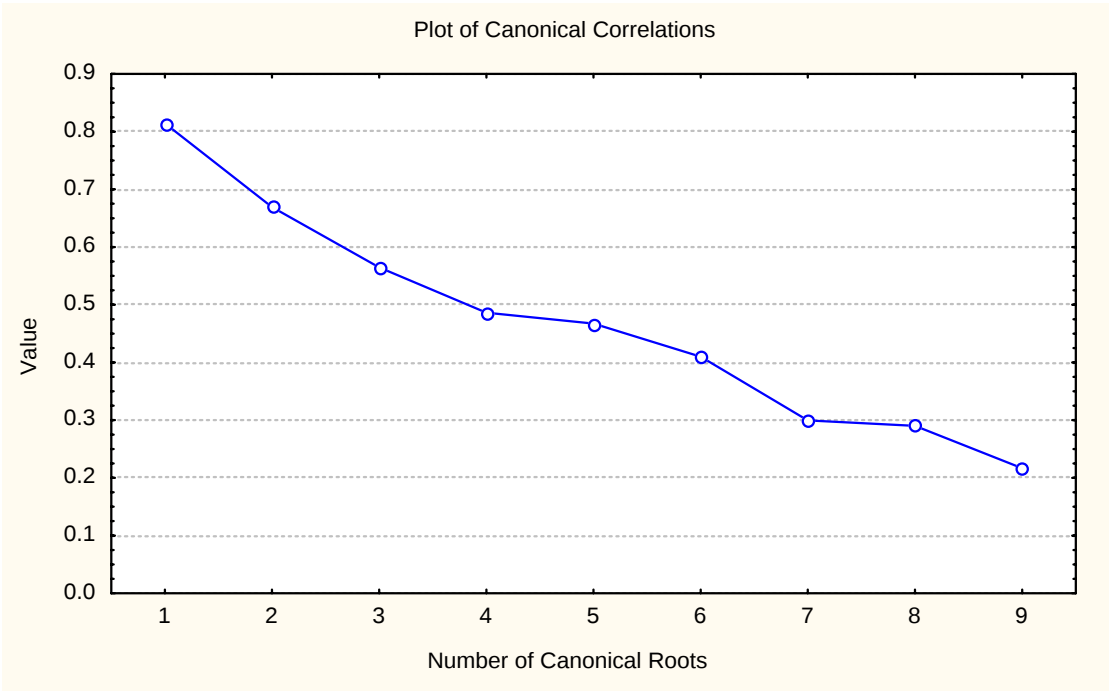
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9.38175	73.77000	Y1	.94730	3.46000	X1
7.19627	67.54000	Y2	.87033	3.51000	X2
11.15515	64.13000	Y3	.61101	3.48000	X3
13.87941	77.78000	Y4	.63373	3.32000	X4
12.29108	63.00000	Y5	.49757	.43000	X5
13.17564	66.72000	Y6	1.01797	2.71000	X6
14.57068	61.72000	Y7	1.05500	2.41000	X7
10.95487	64.47000	Y8	1.42882	2.67000	X8
13.30899	63.61000	Y9	1.27857	1.96000	X9
			.43333	4.21000	X10
			.19695	.96000	X11
			.17145	.97000	X12
			.30151	.10000	X13
			.71711	3.53000	X14
			.77401	3.37000	X15
			.71428	3.57000	X16
			.85818	3.47000	X17
			.17145	1.97000	X18

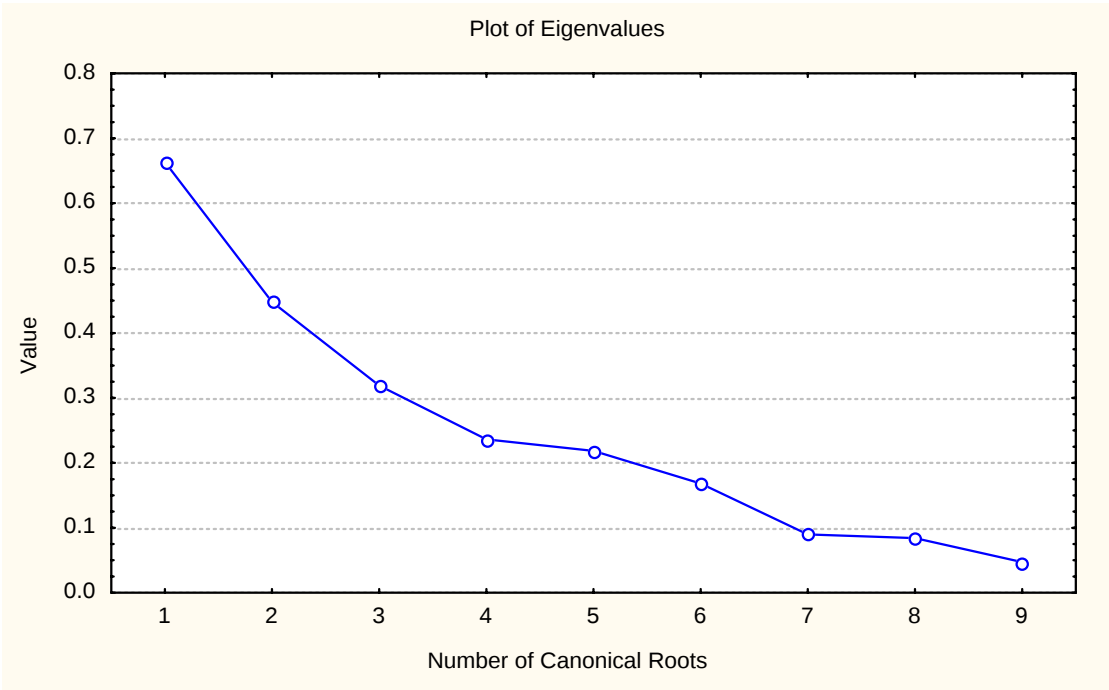
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Canonical R	Eigenvalues
0.814492	0.663398
0.669366	0.448051
0.564887	0.319097
0.486139	0.236332
0.467483	0.218541
0.410133	0.168209
0.299618	0.089771
0.290263	0.084253
0.216801	0.047003



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(254.838) χ^2 (0.814492)

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() () () -

Y X

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χ^2

Canonical R	Canonical R-sqr.	Chi-sqr.	df
.814492	.663398	254.8380	162
.669366	.448051	162.2854	136
.564887	.319097	111.7699	112
.486139	.236332	79.1014	90
.467483	.218541	56.1836	70
.410133	.168209	35.2232	52
.299618	.089771	19.5685	36
.290263	.084253	11.5734	22
.216801	.047003	4.0922	10

(60.4725%) X

X Y

(X)

-: (Y)

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0.298991		X6
0.295920		X12
0.248168		X1
0.242991		X13
0.210146		X7
0.191652		X16
0.178706		X15
0.172666		X3
0.138479		X8
0.135857		X4
0.134240		X14
0.128499		X17
0.126372		X9

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0.065199		X10
0.054937		X11
0.054707		X2
0.052116		X18
0.051939		X5

) X1 () X12 ()X6)
 X16 ()X7 () X13 ()
 () X15 ()
 () X8 () X3
 X6
 X12
 X1
 X13
 X7
 X16
 X15
 X8 X3

) X2 () X11 () X10)
 () X5 ()X18 (

()
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0.393006		Y9
0.370144		Y8
0.237756		Y3
0.235339		Y7
0.186729		Y5
0.170129		Y4
0.165792		Y2
0.129575		Y1
0.078655		Y6

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- 3- Francis R. Bach & Michel, Jordan (2005) "A probabilistic Interpretation of Canonical Correlation Analysis" Technical report 688 university of California.
 - 4- Anderson T. (1958) "An Introduction to multivariate statistical Analysis" Wiley & sons.
 - 5- Flarian M. (2003) "Canonical Correlation Analysis with kernel" computational diagnostic group seminar.