



SEISMIC EVALUATION AND RETROFITTING CODAL PROVISIONS –STATE OF THE ART

Haider A. Abass¹ and Husain K. Jarallah²

¹ M.Sc. Student at Department of Civil Engineering, College of Engineering, Mustansiriyah University, Baghdad – Iraq. E-mail: hiaderaabass@uomustansiriyah.edu.iq

² Asst.Prof.Dr at Department of Civil Engineering, College of Engineering, Mustansiriyah University, Baghdad – Iraq. E-mail: khalfdce1@gmail.com

[HTTPS://DOI.ORG/10.30572/2018/KJE/130103](https://doi.org/10.30572/2018/KJE/130103)

ABSTRACT

Seismic evaluation is one of the important ways to validate that buildings can resist the earthquake loads. The seismic evaluation is classified into global and local checking; the global includes the overall lateral deflection and inter-story drift, the local involves the plastic hinge formed in the structural elements (beams, columns, shear wall, etc.) of the buildings. This paper includes the seismic evaluation techniques according to previous international codes. These codes include ATC-40, FEMA-273, FEMA-356, FEMA-440, ASCE41-13, Euro code 8, Japanese standard code, and Newzland code. This study showed that the seismic evaluation techniques introduced in FEMA-440 and the Japanese standard code are almost complete compared with the other techniques in the other codes.

KEYWORDS: Capacity Spectrum Method, Seismic Evaluation, Displacement Coefficient Method, Capacity Curve, Pushover Analysis.

1. INTRODUCTION

Although an elastic analysis gives a good indication of the elastic capacity of structures and indicates where first yielding will occur, it cannot predict failure mechanisms and account for redistribution of forces during progressive yielding (Giordano M., et al., 2008). Practicing engineers use inelastic analysis procedures for the seismic evaluation and design of upgrades of the existing building and other structures, as well as the design of new construction. The use of inelastic procedures helps to demonstrate how the building behaves by identifying modes of failure and the potential for progressive collapse (Hamraj M. 2014). It helps engineers to understand how the structures will behave when subjected to major earthquakes, where it is assumed that the elastic capacity of the structure will be exceeded. Pushover methods are especially useful for the evaluation of existing buildings (usually not originally designed with seismic requirements) (Mwafy A.M. and Elnashai. A.S. 2001). Pushover analysis is based on the assumption that the dynamic response of the structure is controlled by the elastic fundamental mode, which is the case for most regular buildings (Elnashai A. S. and Di Sarno L. 2008). In this study, the important codes will be reviewed for the seismic evaluation and retrofitting of the existing buildings.

2. RESEARCH SIGNIFICANCE

This research illustrates the differences and the sensitivity of seismic performance levels of the buildings due to the use of various techniques of seismic evaluation and retrofitting relied on various international codes.

3. CODAL PROVISIONS

It is widely recognized that ground shaking in existing buildings located in seismic regions may induce unacceptable levels of damage. Several reasons have been attributed to this vulnerability, such as insufficient strength and stiffness, poor detailing of reinforcement, plan and elevation irregularities, the dominance of brittle failure modes over ductile ones, etc. (Yön, B., et al., 2017). Various codes display the principle concepts to find the seismic performance level of the buildings.

3.1. APPLIED TECHNOLOGY COUNCIL (ATC-40, 1996)

Capacity Spectrum Method (CSM) has gained considerable popularity amongst pushover users and the ATC40 guidelines included the nonlinear static procedure that should be applied. The CSM was created to describe a structure's first mode response based on the

assumption that the first mode response of the structure is the fundamental mode of vibration..

The steps of the capacity spectrum method are described herein:

Step (1): Seismic Data

A MDOF model of the building must be developed including the nonlinear force-deformation relationship for structural elements under monotonic loadings (see Fig. 1a). An elastic acceleration response spectrum is also required corresponding to the seismic action under consideration (see Fig. 1b).

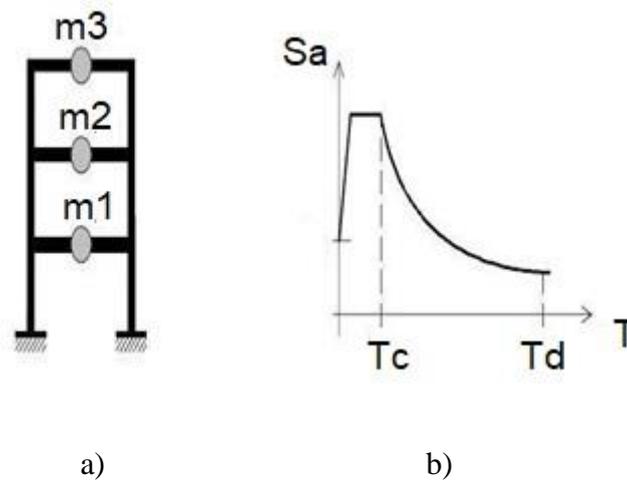


Fig. 1-a): MDOF Model of the Building; b) Elastic Acceleration Response Spectrum.

Step (2): Seismic demand in acceleration displacement response spectrum (ADRS) format.

The seismic demand is defined with a response spectrum in the format acceleration-displacement (ADRS). For SDOF, the displacement spectrum can be computed from the acceleration spectrum using equation (1):

$$S_d = \frac{T^2}{4\pi^2} S_a \quad (1)$$

Where S_a and S_d are the values for the elastic acceleration and displacement spectrum, respectively.

Step (3): Pushover Analysis.

A conventional non-adaptive force-based pushover analysis is performed by applying a monotonically increasing pattern of lateral forces to the structure. Lateral forces are applied in proportion to the story masses and the square height of the floor by using equation (2):

$$F_i = \frac{m_i h_i^2}{\sum_{j=1}^n m_j h_j^2} \quad (2)$$

where m_i and h_i are the mass and height of i^{th} floor. The symbol (i) reflects the story (mass and height) under consideration while the denominator (j) reveals the summation of stories (masses and heights) of the building.

From the pushover analysis, the capacity curve was obtained that represents the base shear and the displacement at the center of mass of the roof.

Step (4): Equivalent SDOF system

The structural capacity curve is expressed in terms of roof displacement and base shear. It is converted into a SDOF curve in terms of spectral displacements and spectral accelerations, which is called the capacity spectrum. The transformations are made using the following equations:

$$PF_1 = \frac{[\sum_{i=1}^N (w_i \phi_{i1})/g]}{[\sum_{i=1}^N (w_i \phi_{i1}^2)/g]} \quad (3)$$

$$\alpha_1 = \frac{[\sum_{i=1}^N (w_i \phi_{i1})/g]^2}{[\sum_{i=1}^N w_i/g][\sum_{i=1}^N (w_i \phi_{i1}^2)/g]} \quad (4)$$

$$S_a = \frac{V/W}{\alpha_1} \quad (5)$$

$$S_d = \frac{\Delta_{\text{roof}}}{PF_1 \phi_{\text{roof},1}} \quad (6)$$

(see Fig. 2), it shows that the participation factor and modal mass coefficient differ according to the relative inter-story drift over the height of the building. For example, the linear distribution of inter-story drift along with the height of the building $\alpha_1 \approx 0.8$ and $PF_1 \approx 1.4$.

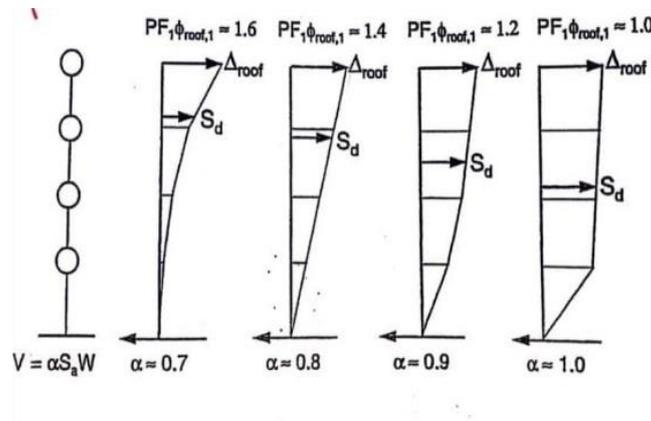


Fig. 2. Modal Participation Factors and Modal Mass Coefficients.

To convert MDOF capacity curve to SDOF capacity curve in the format (capacity spectrum) of the Acceleration-Displacement Response Spectra (ADRS) format (S_a versus S_d), the modal participation factor PF_1 and the modal mass coefficient α must first be calculated by using equations(3) and (4). Afterward, each point of the MDOF capacity curve (V , Δ_{roof}) was calculated the associated point (S_a , S_d) of the capacity spectrum according to equations (5) and (6).

Step (5): Estimation of Damping and Response Spectrum Reduction:

ATC-40 defines equivalent viscous damping to represent this combination; it can be calculated using equation (7):

$$\beta_{eq} = \beta_1 + 5 \tag{7}$$

ATC-40 introduces the concept of effective viscous damping that can be obtained by multiplying the equivalent damping by a modification factor k by using equation (8):

$$\beta_{eff} = k\beta_1 + 5 \tag{8}$$

Where 5% viscous damping is inherent in the structure (assumed to be constant). The hysteretic damping represented as equivalent viscous damping can be calculated by using equation (9):

$$\beta_1 = \frac{1}{4\pi} \cdot \frac{E_D}{E_{S0}} \tag{9}$$

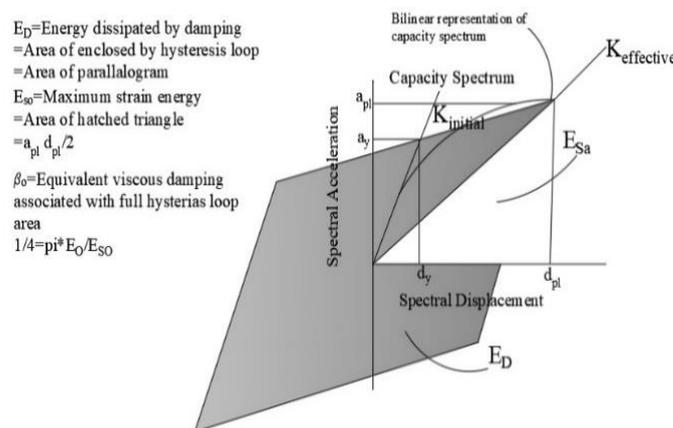


Fig. 3. Derivation of Damping for Spectral Reduction (ATC-40, 1996).

The physical meaning of both E_D and E_{S0} is represented in (see Fig. 3). E_D is the energy dissipated by the structure in a single cycle of motion, that is, the area bounded by a single hysteresis loop. E_{S0} is the maximum strain energy related to that cycle of motion ,that is, the

area of the hatched triangle. (see Fig. 4) shows the derivation of energy dissipated by damping.

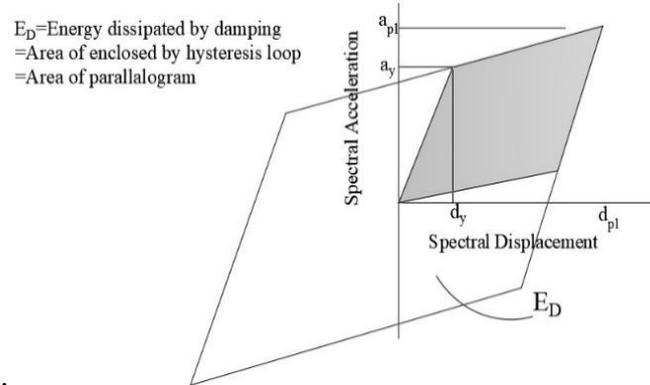


Fig. 4. E_D is the Energy Dissipated by Damping Derivation (ATC-40, 1996).

Therefore, β_1 can be written as in equation (10):

$$\beta_1 = \frac{63.7(a_y d_{pi} - d_y a_N)}{a_{pi} d_{pi}} \quad (10)$$

The effective damping can be written as equation (11):

$$\beta_{eff} = \frac{63.7k(a_y d_{pi} - d_y a_{pi})}{a_{pi} d_{pi}} + 5 \quad (11)$$

The k-factor depends on the structural behavior of the building, which is related to the seismic resisting system quality and the ground shaking duration. ATC40 defines three categories of structural behavior:

Type A represents stable, reasonably full hysteresis loops, type B represents a moderate reduction of area, and type C represents poor hysteretic behavior with a significant reduction of loop area (severely pinched). Table 1 indicates the ranges and limits for the values of k specified to the three structural behavior types.

Table 1. Modification factor k.

Structural Behavior Type	β_1	k
Type A	≤ 16.25	1.0
	> 16.25	1.13
	> 16.25	$\frac{0.51(a_y d_{pi} - d_y a_{pi})}{a_{pi} d_{pi}}$
	≤ 2.5	0.67

Type B		0.845
	>2.5	$-\frac{0.446(a_y d_{pi} - d_y)}{a_{pi} d_{pi}}$
Type C	Any value	0.33

Step (6): Numerical Derivation of Spectral Reductions

As seen in Equations (12) and (13), the spectral reduction factors are determined.

$$SR_A = \frac{3.21 - 0.68 \ln(\beta_{eff})}{2.12} = \frac{3.21 - 0.68 \ln \left[\frac{63.7k(a_y d_{pi} - d_y a_{pi})}{a_m d_{pi}} + 5 \right]}{2.12} \geq \text{Value in Table(2)} \tag{12}$$

$$SR_v = \frac{2.31 - 0.41 \ln(\beta_{eff})}{1.65} = \frac{2.31 - 0.41 \ln \left[\frac{63.7k(a_y d_{ri} - d_y a_{pi})}{a_{pi} d_{pi}} + 5 \right]}{1.65} \geq \text{Value in Table(2)} \tag{13}$$

Values for S_{RA} and S_{Rv} should be greater than or equal to those listed in Table 2.

Table 2. S_{RA} and S_{Rv} Values

Form of Structural Action	S_{RA}	S_{Rv}
Type (A)	0.33	0.50
Type (B)	0.44	0.56
Type (C)	0.56	0.67

Step (7): Calculation of the target displacement:

The calculation of the target displacement is an iterative process, where it is necessary to estimate a first trial performance point. For this purpose, there are several options one can use:

1. The first trial performance point can be estimated as the elastic response spectrum corresponding to the elastic fundamental period. The response spectrum is defined for the viscous damping level considered (in buildings are considered as 5%);
2. The first trial equivalent damping value was considered and calculated the respective reduction factor. By Multiplying the elastic spectrum by this reduction factor and intersect the capacity curve with the reduced spectrum. The intersection corresponds to the first trial performance point. The capacity curve is then bi-linearized for this point, new effective damping can be computed and hence a new reduction factor can be applied. The new intersection between the capacity curve and the new reduced spectrum leads to a new performance point. If the target displacement calculated within a tolerable range (for example within 5% of the displacement of the trial performance point), then the performance point can be obtained. (see Fig. 5) represents the process schematically.

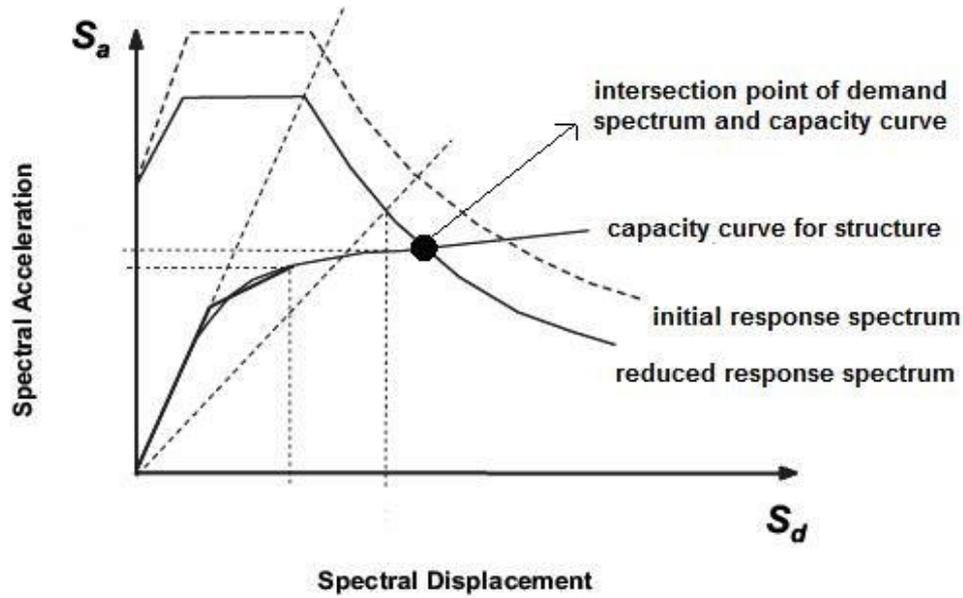


Fig. 5. Target displacement computed by CSM.

Step (8): Determination of MDOF response parameters in correspondence to the Performance Point (converted from SDOF to MDOF)

At this stage of the procedure, the MDOF pushover curve to the point consistent with the value of the SDOF target displacement (calculated in the previous step) multiplied by the transformation factor. For this step, building's performance results was obtained such as deformations, inter-story drifts, and chord rotations.

3.2. FEDERAL EMERGENCY MANAGEMENT AGENCY (FEMA273/356, 2001)

The Displacement Coefficient Method (DCM) is the primary nonlinear static procedure presented in FEMA 356. The target displacement δ , at each floor level shall be calculated by using equation (14):

$$\delta_t = C_0 C_l C_2 C_3 S_a \frac{T_e^2}{4\pi^2} g \quad (14)$$

where:

C_0 = Modification factor to associate spectral displacement of an equivalent SDOF system to the roof displacement of the building MDOF system determined using one of the following procedures:

1. The first modal participation factor at the control point level.
2. The appropriate value from [Table 3](#).

Table 3. Values for Modification Factor C_0 .

No.of stories	Modification factor
1.0	1.0
2.0	1.2
3.0	1.3
5.0	1.4
+10	1.5

C_1 = Modification factor to relate estimated maximum inelastic displacements to displacements calculated for linear elastic response:

$$= 1.0 \text{ for } T_e \geq T_s$$

$$= [1.0 + (R-1)T_s/T_e]/R \text{ for } T_e < T_s$$

C_1 is not greater than the values below, and no less than 1.0.

$$C_1 = \begin{cases} 1.5 & \text{for } T_e < 0.1s \\ 1.0 & \text{for } T_e \geq T_s \end{cases}$$

T_e = effective fundamental Period of the building under consideration.

$$T_e = T_i \sqrt{\frac{K_i}{K_e}} \quad (15)$$

R = Ratio of elastic strength demand to calculated yield strength coefficient.

$$R = \frac{S_a}{V_y/W} \cdot C_m \quad (16)$$

C_2 = Modification factor to represent the effect of pinched hysteretic shape, stiffness, and strength degradation on maximum displacement response. Values for different framing systems and structural performance levels shall be calculated from [Table 4](#).

Table 4. Values for Modification Factor C_2 .

Structural performance level	$T \leq 0.1$ second		$T \geq T_s$ second	
	Framing type 1 ¹	Framing type 2 ²	Framing type 1 ¹	Framing type 1 ²
IO	1	1	1	1
LS	1.3	1	1.1	1
CP	1.5	1	1.2	1

¹.Buildings in which any combination of the following components, elements, or frames resists more than 30% of the floor shear at an level.

². All frames that aren't categorized as Framing Form 1.

C_3 = Modification factor to represent increased displacements due to dynamic P- Δ effects. For buildings with a positive post-yield stiffness (maintains its strength during a given deformation cycle, but loses strength in subsequent cycles, the effective stiffness also decreases in subsequent cycles (degradation of cyclic strength)) the value shall be set at 1.0. For buildings with negative post-yield stiffness (Note that the degradation happens during the same cycle of deformation in which yielding occurs, resulting in a negative post-elastic stiffness, (in-cycle strength degradation)), values shall be calculated using equation (17).

$$C_3 = 1.0 + \frac{|\alpha|(R-1)^{3/2}}{T_e} \quad (17)$$

Where α is the ratio of post-yield stiffness to elastic stiffness when the nonlinear force-displacement relation is characterized by a bilinear relation.

3.3. FEDERAL EMERGENCY MANAGEMENT AGENCY (FEMA-440, 2004)

3.3.1. Improved Procedures for Displacement Modification

FEMA 440 (2005) recommends that the limitations (capping) allowed by FEMA 356 to the coefficient C_1 be abandoned, In addition, a distinction is recognized between two different types of strength degradation that have different effects on system response and performance, this distinction leads to recommendations for the coefficient C_2 to account for cyclic degradation in strength and stiffness. It is also suggested that the coefficient C_3 be eliminated and replaced with a limitation on strength (R).

a. Maximum Displacement Ratio (Coefficient C_1)

FEMA 356 currently accepts the coefficient C_1 to be restricted (capped) for relatively short-period structures. FEMA440 suggested that this limitation not be used. This may increase the estimation of the displacement for some structures. For most structures, the following simplified expression may be used for the coefficient C_1 :

$$C_1 = 1 + \frac{R-1}{aT_e^2} \quad (18)$$

For periods less than 0.2 s, the value of the coefficient C_1 for 0.2 s may be used. For periods greater than 1.0 s, C_1 may be assumed to be 1.0.

b. Degrading System Response (Coefficient C_2)

FEMA 356 suggested that the C_2 coefficient represents the effects of stiffness degradation only. FEMA440 recommended that the displacement prediction must be modified to account the cyclic degradation of stiffness and strength. It recommended that the C_2 coefficient must be as follows:

$$C_2 = 1 + \frac{1}{800} \left(\frac{R-1}{T} \right)^2 \quad (19)$$

For periods less than 0.2 s, the value of the coefficient C_2 for 0.2 s may be used. For periods greater than 0.7 sec, C_2 may be assumed equal to 1.0 for assumption includes the buildings with modern concrete or steel special moment-resisting frames, steel eccentrically braced frames, and buckling-restrained braced frames as either the original system or the system added during seismic retrofit.

c. P- Δ Effects (Coefficient C_3)

Because of dynamic P- Δ effects, the displacement modification factor C_3 is intended to account for increased displacements. FEMA 440 proposed that the current coefficient C_3 has been eliminated and replaced it with the maximum strength ratio, R , intended to calculate the dynamic instability. Where the value for R_{\max} is exceeded, a Nonlinear Dynamic Procedures (NDP) analysis is recommended to capture strength degradation and dynamic P- Δ effects to confirm the dynamic stability of the building. Nonlinear static procedures are not capable for distinguishing completely between cyclic and in-cycle strength losses. However, insight can be obtained by separating the in-cycle P- Δ effects from α_2 (see Fig. 5).

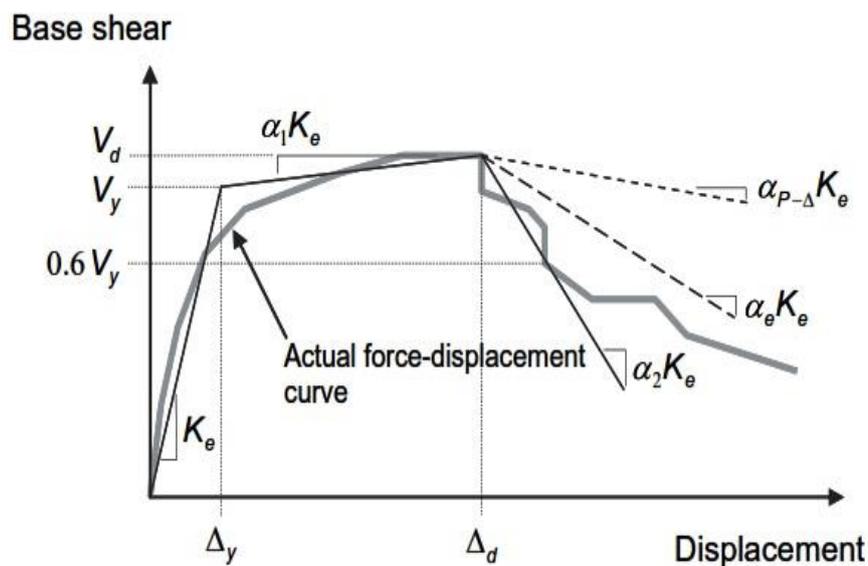


Fig. 6. Idealized Force-Displacement Curves.

After that, an acceptable post-elastic stiffness can be calculated as

$$\alpha_e = \alpha_{p-\Delta} + \lambda(\alpha_2 - \alpha_{p-\Delta}) \quad (20)$$

Where $0 \leq \lambda \leq 1.0$

FEMA 440 recommended that λ must be assigned the value of 0.2 for sites not subject to near field effects and 0.8 for those that are. Displacement amplifications increase as the post-yield negative stiffness (caused by in-cycle strength degradation) ratio α decreases (becomes more negative), as R increases. Minimum strength (maximum R) required avoiding dynamic instability. The recommended limit on the design force reduction, R_{\max} , is as follows:

$$R_{\max} = \frac{\Delta_d}{\Delta_y} + \frac{|\alpha_e|^{-t}}{4} \quad (21)$$

Where

$$t = 1 + 0.15 \ln T \quad (22)$$

The structural model must appropriately model the strength degradation characteristics of the structure and its components

3.3.2. Improved Procedures for Equivalent Linearization

An improved equivalent linearization procedure as a modification to the Capacity-Spectrum Method (CSM) of ATC-40. When equivalent linearization is used as a part of a nonlinear static procedure that models the nonlinear response of a building with a SDOF oscillator, the objective is to evaluate the maximum displacement response of the nonlinear system with an “equivalent” linear system using an effective period, T_{eff} , and effective damping, β_{eff} , (see Fig. 7).

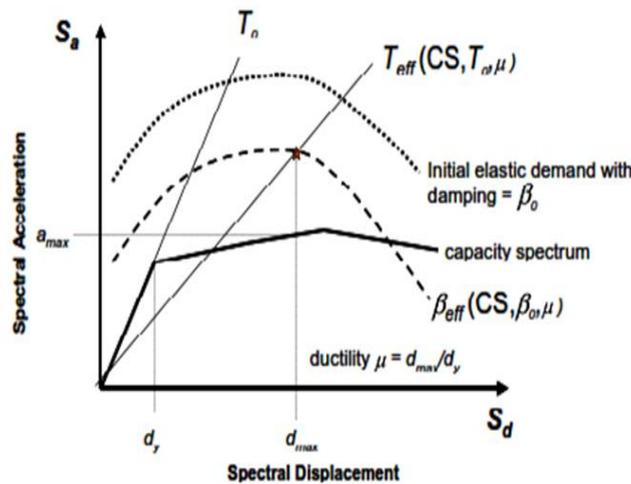


Fig. 7. Damping Values and Effective Period of the Equivalent Linear System.

a. Effective Damping

The formulas herein presented apply to any capacity curve, independent of the hysteretic model, type or post-elastic stiffness value (α) used. The effective damping is calculated using the Equations below depending on the structure's level of ductility μ .

For $\mu < 4.0$:

$$\beta_{eff} = 4.9(\mu - 1)^2 - 1.1(\mu - 1)^3 + \beta_0 \quad (23)$$

For $4.0 \leq \mu \leq 6.5$:

$$\beta_{eff} = 14.0 + 0.32(\mu - 1) + \beta_0 \quad (24)$$

For $\mu > 6.5$:

$$\beta_{eff} = 19 \left[\frac{0.64(\mu-1)-1}{[0.64(\mu-1)]^2} \right] \left(\frac{T_{eff}}{T_0} \right)^2 + \beta_0 \quad (25)$$

b. Effective Period

The following equations apply to any capacity spectrum independent of the hysteretic model form or post-elastic stiffness value. The effective period depends on the ductility level and is calculated using the Equations below:

For $\mu < 4.0$:

$$T_{eff} = \{0.20(\mu - 1)^2 - 0.038(\mu - 1)^3 + 1\} \quad (26)$$

For $4.0 \leq \mu \leq 6.5$:

$$T_{eff} = [0.28 + 0.13(\mu - 1) + 1]T_0 \quad (27)$$

For $\mu > 6.5$:

$$T_{eff} = \left\{ 0.89 \left[\sqrt{\frac{(\mu-1)}{1+0.05(\mu-2)}} - 1 \right] + 1 \right\} T_0 \quad (28)$$

Where μ is the ductility and α is the post-elastic stiffness, measured as follows:

$$\alpha = \frac{\left(\frac{a_{pi}-a_y}{d_{pi}-d_y} \right)}{\left(\frac{a_y}{d_y} \right)} \quad (29)$$

and

$$\mu = \frac{d_{pi}}{d_y} \quad (30)$$

c. Spectral Reduction Factor of Effective Damping

The spectral reduction factor is a function of the effective damping and is called the damping coefficient, B (β_{eff}) and is calculated using equation:

$$B(\beta_{eff}) = \frac{4}{5.6 - \ln \beta_{eff}(in\%)} \quad (31)$$

As seen in equation (32), it is used to adjust spectral acceleration ordinates.

$$(S_a)_\beta = \frac{(S_a)_{5\%}}{B(\beta_{eff})} \quad (32)$$

3.4. AMERICAN STANDARD OF CIVIL ENGINEERS (ASCE 41-13, 2013)

ASCE41-17 depends on the displacement coefficient method to capture the target displacement. The target displacement, δ at each floor level shall be determined by equation (33).

$$\delta_t = C_o C_1 C_2 S_a \frac{T_e^2}{4\pi^2} g \quad (33)$$

where

C_o = modification factor to relate spectral displacement of an equivalent single degree of freedom (SDOF) system to the roof displacement of multi-degree of freedom (MDOF) system determined using one of the following procedures:

1. The first mode mass participation factor is multiplied by the ordinate of the first mode shape at the control node.
2. The mass participation factor was calculated using a shape vector corresponding to the deflected shape of the building at the target displacement multiplied by the ordinate of the shape vector at the control node.
3. The appropriate value from [Table 5](#).

Table 5. Modification Factor C_o values.

No. of stories	Shear Buildings ¹		Other Buildings
	Triangular . load pattern	Uniform. load pattern	Any .load pattern
1	1.0	1.0	1.0
2	1.2	1.15	1.2
3	1.2	1.2	1.3
5	1.3	1.2	1.4
+10	1.3	1.2	1.5

¹Buildings in which story drift decreases with rising height for all stories.

C_1 = modification factor to relate the estimated maximum inelastic displacements to displacements calculated for the linear elastic response. For periods less than 0.2 sec, C_1 does not need not be taken greater than the value at $T = 0.2$ sec. For periods greater than 1.0 sec, $C_1 = 1.0$.

$$C_1 = 1 + \frac{R-1}{aT_e^2} \quad (34)$$

where , a = site class factor = 130 site Class A, B; = 90 site Class C, and = 60 site Class D, E, and F.

C_2 = modification factor to represent the effect of pinched hysteresis shape, cyclic stiffness degradation, and strength deterioration on maximum displacement response. For periods greater than 0.7 sec, $C_2 = 1.0$

$$C_2 = 1 + \frac{1}{800} \left(\frac{R-1}{T_e} \right)^2 \quad (35)$$

The strength ratio R must be determine using the equation (36).

$$R = \frac{S_a}{v_y/W} \cdot C_m \quad (36)$$

C_m taken as the effective modal mass participation factor determined for the fundamental mode using an eigenvalue analysis shall be acceptable. C_m shall be taken as 1.0 if the fundamental period, T , is greater than 1.0 sec.

The maximum strength ratio, R_{max} , must be determined by equation (37) for buildings with negative post-yield stiffness.

$$R_{max} = \frac{\Delta_d}{\Delta_y} + \frac{|\alpha_d|^{-h}}{4} \quad (37)$$

where

Δ_d = peak displacement or displacement at maximum base shear.

Δ_y = displacement at the effective yield strength.

$h = 1 + 0.15 \ln T$, and

α_e = equation (38) defines the effective negative post-yield slope ratio.

$$\alpha_e = \alpha_{p-\Delta} + \lambda(\alpha_2 - \alpha_{p-\Delta}) \quad (38)$$

where

α_2 = negative post-yield slope ratio. This include P- Δ effects, in-cycle degradation, and cyclic degradation;

$\alpha_{p-\Delta}$ = P- Δ effects cause a negative slope ratio; and

λ = near field effect factor:

= 0.8 if $S1 \leq 0.6$ (Maximum Considered Earthquake, MCE); = 0.2 if $S1 < 0.6$ (MCE).

3.5. Euro code 8 (EC-8, Part 3)

N_2 method, the first proposed by Fajfar and Fischinger, (1988) is represented the Nonlinear Static Procedures (NSP) adopted by Euro code 8 and considered as modifying version of the capacity spectrum method (CSM). Indeed, the estimation of seismic demand is based on the use of inelastic spectra in the N_2 method instead of highly damped elastic spectra, as per the CSM. The steps of the capacity spectrum method are defined herein:

Step (1) and Step (2) are the same steps of the capacity spectrum method with ATC-40.

Step (3): Pushover analysis

Pushover analysis is performed by applying a monotonically increasing pattern of lateral forces to the structure, (see Fig. 8). These forces represent the inertial forces induced in the structure by the ground motion. Any reasonable distribution of lateral loads can be used in the N_2 method. The Euro code 8 recommends that the use of at least two distributions: a first mode proportional load pattern and a uniform load pattern.

The vector of the lateral loads \bar{F} used in the pushover analysis proportional to the first mode is determined as:

$$\bar{F} = pM\Phi \quad (39)$$

The lateral force in the i -th level is proportional to the component Φ_i of the assumed displacement shape Φ_i weighted by the storey mass m_i

$$\bar{F} = pm_i\Phi_i \quad (40)$$

The vector of the lateral loads \bar{F} used in the pushover analysis with a uniform distribution is determined as:

$$\bar{F}_{uni} = pM \quad (41)$$

$$\bar{F}_{unij} = pm_i \quad (42)$$

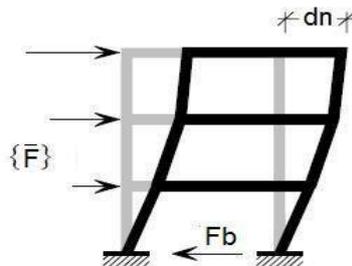


Fig. 8. Pushover Analysis of the MDOF Model.

The N_2 method prescribes that the figure above should represent the base shear (F_b) and the displacement at the center of mass of the roof (d_n).

Step (4): Equivalent SDOF system

The MDOF structure should be transformed into an equivalent SDOF system. The definition of the transformation factor Γ is based on the equation of motion of a MDOF system

$$M \cdot \ddot{U} + R = -M \cdot 1 \cdot a \quad (43)$$

Where U is the displacement vector, \ddot{U} is the acceleration vector, M is a diagonal mass matrix, R is the internal forces vector, 1 is a unit vector and a is the ground acceleration as a function of time. The deformed pattern Φ is assumed to be constant during the structural response to the earthquake. The displacement vector is then written as equation (44).

$$U = \Phi \cdot d_n \quad (44)$$

where d_n is the top displacement. The Φ is normalized to have its component at the top equal to 1. The internal forces R are equal to the statically applied external loads \bar{F} .

$$\bar{F} = R \quad (45)$$

Equations (39 and 44) into equation (45) and multiplying the equation by Φ , it follows:

$$\Phi^T \cdot M \cdot \Phi \cdot \ddot{d}_n + \Phi^T \cdot M \cdot \Phi \cdot p = -\Phi^T \cdot M \cdot 1 \cdot a \quad (46)$$

The SDOF system's equation of motion can be written as:

$$m^* \cdot \ddot{d}^* + F^* = -m^* \cdot a \quad (47)$$

where m^* is the equivalent mass of the SDOF system and it is calculated using equation (48)

$$m^* = \Phi^T \cdot M \cdot 1 = \sum m_i \Phi_i \quad (48)$$

The transformation of the MDOF to the SDOF, the system is made in the N_2 method using equations (49) and (50)

$$d^* = \frac{d_n}{\Gamma} \quad (49)$$

$$F^* = \frac{F_b}{\Gamma} \quad (50)$$

where d^* , F^* are the displacement and base shear of the SDOF system. According to equation (51), the transition element from the MDOF to the SDOF model is:

$$\Gamma = \frac{\Phi^T \cdot M \cdot 1}{\Phi^T \cdot M \cdot \Phi} = \frac{\sum m_i \Phi_i}{\sum m_i \Phi_i^2} = \frac{m^*}{\sum m_i \Phi_i^2} = \frac{\sum F_i}{\sum \left(\frac{F_i^2}{m_i} \right)} \quad (51)$$

The transformation factor Γ is usually called the modal participation factor. The SDOF capacity curve is defined by the displacement of the SDOF (d^*) and base shear of this system (F^*) as shown (see Fig. 9).

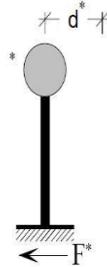


Fig. 9. Equivalent SDOF system.

Euro code 8 prescribes a simplified elastic-perfectly plastic bilinear approximation of the SDOF capacity curve (see Fig. 10). The smooth curve represents the bilinear of the SDOF capacity curve.

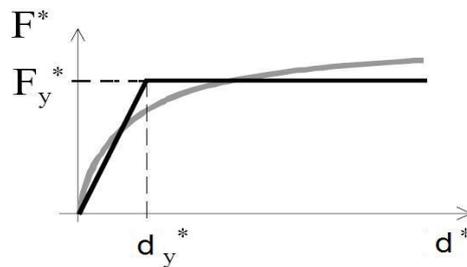


Fig. 10. SDOF capacity curve and its bi linearization

The elastic period of the idealized bilinear SDOF system T^* is computed according to equation (52):

$$T^* = 2\pi \sqrt{\frac{m^* d_y^*}{F_y^*}} \quad (52)$$

N_2 method assumes that in the medium/long period range ($T^* \geq T_c$) the equal displacement rule applies, i.e. the displacement of the inelastic system S_d is equal to the displacement of the associated elastic system S_{de} characterized by the same period T^* , where T_c is the characteristic period of the ground motion, which is defined as the transition period between

the constant acceleration section of the response spectrum (corresponding to the short period range) and the constant velocity segment of the response spectrum (corresponding to the medium period range) (see Fig. 11).

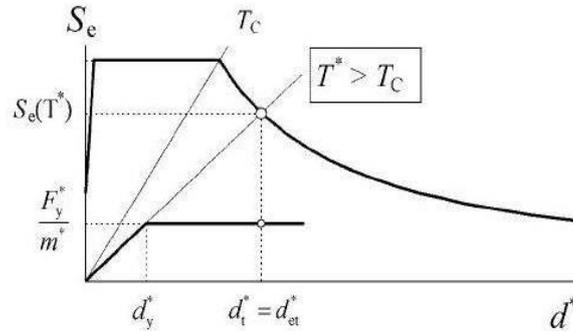


Fig. 11. Long-period range.

This means that in the above mentioned period range $R_\mu = \mu$. Seismic demand in terms of inelastic displacement can be obtained by intersecting the radial line with the elastic demand spectrum corresponding to the SDOF system period. In the case of short-period structures ($T^* < T_C$) the inelastic displacement is larger than the elastic one and the equal displacement rule does not apply anymore, (see Fig. 12). Consequently $R_\mu < \mu$ and it can be calculated as the ratio between the elastic acceleration demand capacity S_{ae} and the inelastic acceleration S_a . The inelastic displacement demand is, in this case, equal to $S_d = \mu \cdot D^*y$ being D^*y the yielding displacement of the SDOF system. The ductility factor can be derived from the reduction factor by the relation:

$$\mu = (R_\mu - 1) \frac{T_C}{T^*} + 1 \tag{53}$$

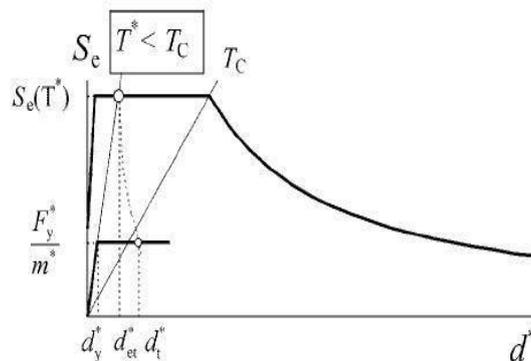


Fig. 12. Short period range.

In both cases ($T^* \geq T_C$ and $T^* < T_C$) the inelastic acceleration demand S_a is equal to the elastic one S_{ae} and it can be verified at the intersection of the radial line corresponding to the period of the SDOF system with the elastic demand spectrum.

3.6. Japanese Standard

Three screening levels have been introduced in the Japanese standard (Japanese code, 2001) for seismic capacity evaluation. Seismic index of the structure for each story

$$I_s = E_o \cdot S_D \cdot T \quad (54)$$

where E_o is the primary seismic index of screening levels. The primary seismic index of structure E_o of the i -th story in an n -story building is given as a product of the strength index C , ductility index F , and α is the effective strength factor, differently in each screening level as shown in the Table 6. S_D is introduced to adjust the basic seismic index by measuring the effects of horizontal, vertical shapes, and the mass and stiffness irregular distribution of the structure. T is a modification factor of the basic seismic index which evaluates the effects of cracks, deflection, and aging of the building. T value will be a range of 0.7 to 0.9 but if there is no defect, the T value is 1. Building older than 30 years have a T value of 0.8, but for newer buildings less than 19 years old the T value should be equals to 1.

Table 6. Values of the primary seismic index(E_o).

Screening	Primary Seismic Index(E_o)
First Screening	$E_o = \frac{n+1}{n+i} (C_w + \alpha_1 C_e) \times F_w$
Second Screening	$E_o = \frac{n+1}{n+i} (C_{sc} + \alpha_2 C_w + \alpha_3 C_c) \times F_{sc}$
Third Screening	$E_o = \frac{n+1}{n+i} \sqrt{E_1^2 + E_2^2 + E_3^2}$
Forth Screening	$E_o = \frac{n+1}{n+i} \left(C + \sum_j \alpha_j C_j \right) \times F_1$

Seismic demand index(I_{so}) regardless of the number of stories in the building:

$$I_{so} = E_s \cdot Z \cdot G \cdot U \quad (55)$$

where

E_s is the basic seismic demand index of the structure, standard values of which shall be selected as 0.8 for the first level screening and 0.6 for the second and third level screenings.

Z is the zone index, namely the modification factor accounting for the seismic activities and intensities expected in the region of the site.

G is a ground index, namely the modification factor accounting for the effects of the amplification of the surface soil, geological conditions, and soil-structure interaction on the expected earthquake motions. U is the usage index, namely the modification factor accounting for the building.

If

$$I_s \geq I_{so} \quad (56)$$

If equation 56 is satisfied, the building may be assessed to be “safe”. Otherwise, the building should be assessed to be “an uncertainty” in seismic safety and need to retrofit.

3.7. NZS1170.5 2004

The target displacement of (NZS1170.5, 2004) is calculated by using the coefficient method, as described in FEMA-356.

$$\delta = C_0 C_1 C_2 C_3 C(T) \frac{T_c^2}{4\pi^2} g \quad (57)$$

where the coefficients take the same roles in modifying the expected elastic displacement. Expressions for them are redefined here to better reflect the intent of NZS1170.5. C_0 will equal (1) as we plot the deflection of the dynamic center of mass.

C_1 accounts for the variation between the response of an elasto-plastic and elastic SDF systems and can be obtained from clauses 5.2 and 7.2.1.1 of the Standard expressed as

$$C_1 = \mu^* S_p / k_\mu \quad (58)$$

Since variations in the response of systems with a pinched hysteretic shape and stiffness and strength degradation are not taken into account in NZS1170.5, C_2 would equal “1”.

The increased displacements caused by dynamic P-delta effects are accounted for by C_3 . This can be calculated using the Standard as follows:

$$C_3 = 1 + \beta\theta \quad (59)$$

NZS1170.5 provides limitations as to which buildings require P- Δ effects included in the analyses. This is a pragmatic approach to allow simple regular buildings to be quickly designed with the knowledge that other conservative clauses in the Standard will provide for the shortfall in strength. It is recommended here, that where the NSP procedure is used in a seismic assessment procedure and the building has not been designed to modern Standards, C_3 as per equation 59 be included in the analysis of all buildings. $C(T)$ is the ordinate of the elastic hazard spectrum as per clause 3.1.1 of the Standard.

4. CONCLUSIONS

Referring to the review concerning the seismic evaluation and retrofiting, the following remarks can be concluded:

1. Japanese Standard depends on the numerical technique. It takes the strength and stiffness deterioration and torsional effect into account in the seismic assessment.
2. The improvement CSM and DCM of (FEMA-440) focused on the effect of degradation of stiffness and the dynamic properties changes associated with damage. It doesn't take the effect of irregularity in the plan or elevation into consideration.
3. ATC-40, FEMA273/356, FEMA440, and ASCE 41-13 are considered the most important than Euro code 8 – Part 3. FEMA440 also states that the procedures used in FEMA273/356 and ATC-40 are insufficient to capture the dynamic instability phenomenon.
4. Static nonlinear analysis (Pushover analysis) Procedures are considered to be a very realistic method for evaluating structural seismic performance, and it is introduced in this context as an effective tool for performance assessment.
5. Despite the large efforts of researchers aimed at the improvement of NSPs for a reliable application to irregular buildings. It is seen these developments have not yet transposed to both European and American codes. For this reason, these codes are still in need of improvement regarding specific prescriptions concerning the seismic analysis of irregular structures.
6. The results of the CSM method according to ATC-40 and an improved equivalent linearization procedure adopted by FEMA-440 differed because the equivalent linearization procedure relied on new expressions to assess effective period and effective damping.

5. ACKNOWLEDGMENTS

The authors would like to thank Mustansiriyah University (www.uomustansiriyah.edu.iq) Baghdad – Iraq for its support in the present work.

6. REFERENCES

- Giordano, M., Guadagnuolo and Faella G. (2008) “Pushover Analysis of Plan Irregular Masonry Buildings” The 14 World Conference on Earthquake Engineering, Beijing, China.
- Hamraj. M. (2014) “Performance Based Pushover Analysis of R.C.C Frames for Plan Irregularity”, International Journal of science, Engineering and Techonology, Vol.7.
- Mwafy A.M. and Elnashai.A.S. (2001) “Push Versus Dynamic Collapse Analysis of R/C Buildings”, International Journal of Modern Trends in Engineering and Science, Vol.4.

Elnashai A. S. and Di Sarno L., (2008), “Fundamentals of Earthquake Engineering”. Wiley and Sons, UK.

Yön, B., Sayın, E. and Onat, O. (2017), “Earthquakes and Structural Damages”, Earthquakes - Tectonics, Hazard and Risk Mitigation, DOI: 10.5772/65425.

Applied Technology Council, (1996), “Seismic Evaluation and Retrofit of Concrete Buildings”, Report No. SSC 9601: ATC-40, Vol.1, Redwood City, California.

Federal Emergency Management Agency, (1997) “NEHRP Guidelines for the Seismic Rehabilitation of Buildings”, FEMA-273”, Washington, D.C.

Federal Emergency Management Agency, (2000) “Prestandard and Commentary for the Seismic Rehabilitation of Buildings”, FEMA-356, Washington, D.C.

ATC, Applied Technology Council. (2005) “Improvement of Nonlinear Static Seismic Analysis Procedures”, FEMA440 Report. Redwood City, CA.

ASCE, “Seismic analysis of safety-related nuclear structures and commentary” (2013). ASCE standard no.004-98, American Society of Civil Engineering.

CEN (2005a), EN 1998-3 Eurocode 8; “Design of structures for earthquake resistance, part 3: assessment and retrofitting of buildings” (1998), European Committee for standardization.

Fajfar, P.; Fischinger, M.(1988), “N2—A Method for Nonlinear seismic analysis of regular buildings”, In Proceedings of the Ninth World Conference Earthquake Engineering, Tokyo, Japan.

The Japan Building Disaster Prevention Association (JBDPA), (2001), “Standard for Seismic Evaluation of Existing Reinforced Concrete Buildings” (JBDPA, Tokyo).

NZS1170.5. (2004), “Structural Design Actions Part 5: Earthquake Actions – New Zealand”, Standards New Zealand, 2004.