

Analysis of Induction Cooker Coil

Dr. A.K.M. Al-Shaikhli*

&

Hassan A. Al-Ssadi*

Received on:26/10/2009

Accepted on:6/5/2010

Abstract

The use of induction heating in industrial applications is old and wide. In recent years, this technology was entered to domestic use. This research deals with the analysis and applications of induction heating for cooking food, as these techniques have safe and economy, as well as cleanness and the atmosphere of work comfortable. Knowledge of the electrical resistance of induction heating system is very important to designers working in the high frequency-supplies. This research also analyzes and studies this resistance, by used solid, litz and twisted wire, and offers simplification of equations derivation help anyone interested in this subject. The MATHCAD V.14 program has been employed to obtain the results. The results presented as general curves for three types of wires (solid, litz and twisted wire) so that a designer can use them without lengthy and complex calculations.

Keywords: induction heating; cooker coil; induction cooker; eddy current; skin effect; proximity effect; solid wire; litz wire; twisted wire;

تحليل ملف الطهي الحثي

الخلاصة

أستعمال التسخين الحثي في للتطبيقات الصناعية قديم و واسع و في السنوات الأخيرة دخلت هذه التقنية الى الأستعمالات المنزلية. يتناول هذا البحث أستعمال التسخين الحثي في طهي الطعام, حيث أن هذه التقنية تمتاز بالأمان و الأقتصاد و النظافة و أجواء العمل المريحة.. أن معرفة المقاومة الكهربائية لمنظومة التسخين الحثي مهمه جداً في تصميم جهاز القدرة ذي الترددات العالية المستعمل فيها. هذا البحث يحلل و يدرس هذه المقاومة عند أستعمال (solid, litz and twisted wire) و يقدم تبسيط لأشتقاق المعادلات التي تساعد المهتمين بهذا الموضوع. لقد أستخدم برنامج MATHCAD V.14 لأستخلاص النتائج حيث قدمت هذه النتائج على شكل منحنيات لثلاثة أنواع من الأسلاك (solid, litz and twisted wire) تتيح للمصمم أستخدامها بدون ضياع للوقت و الحسابات المعقدة.

1. Introduction

The induction cookers use induction heating for cooking. The first research about induction cooker was Moreland's paper [1]. The principle of the work depends on the flow of ac. alternate current in the coil, which generates a time varying magnetic field intersects with cooking vessel metal leads to generate eddy currents and then heating the vessel of cooking. The induction cooker come in a variety of forms , from portable one-hob hot plates to full-sized four-

hob ranges . Each hob contains a coil. This means a flameless method of heating. This type of flameless cooking has many advantages over traditional hobs as it provides faster heating, higher efficiency, greater consistency and controllability. Induction cookers are safer to use than other hobs since there are no open flames and the hob itself only gets marginally hot (due to heat conduction from the pan). Also, no

heat is transferred from the hob to the air, keeping the kitchen cooler [2].

These cookers are also easier to clean because the food can not burn if it drops onto the cooking surface as it is not hot. Induction cooker coils are made of many types of wire such as solid, foil, hollow, litz and twisted.

Symbol	Explanation
ac	Conduction area or cross section area (m ²)
d	Distance between load and coil (m)
f	Frequency of current (Hz)
	Magnetic field created by the single circular turn
J_0, J_1	Bessel functions
J_{ϕ}	Current density (A/m ²)
n	Number of turns in coil
n _s	Number of strands
G	Packaging factor
r _b	Radius of bundle (m)
r _e	Radius of the equivalent solid wire for twisted wire
r _s	Radius of strand (m)
u	Radius of single loop (m)
u ₁	Radius of first Internal loop of multi turns coil (m)
u _f	Radius of final external loop of multi turns coil (m)
u _i	Radius of i- turn in multi-turns coil (m)
Z	Total impedance (Ω)
δ	Current penetration depth or skin depth(m)
η	Efficiency of coil+load (%)
Φ_c	Factor of Skin effect
Φ_{in}	Factor of proximity effect

Recently, the studies dropped to study main wires (solid, litz and twisted) which has lower losses, in high frequency operation, compared with other types of wire. The coil is connected to a medium / high frequency inverter . Knowing the inverter load is very important for its

design. The inverter resonant load consists of the pan and the induction coil. The coupling between the coil and the pan is modeled as the series connection of a resistor (R_{T-L}), see fig. (1), and to insulate the load from the coil, ceramic is very suitable to protect cooker coil from heat transfer which generated in the vessel, also see figure (1).

One of the main problems related to the design of the inductors is the calculation of the winding ac resistance. Many efforts, summarized in [2,3], have been made to derive expressions for (R_T).

The objective of this work is to study the variation of (R_{T-L}) as a function of frequency, radius of strands, number of strands ...etc. to be useful for different induction cookers. The main wires used for induction cooker coils are:

- 1. Solid wire:** also called solid-core or single-strand wire. At high frequencies, current travels near the surface of the wire because of the skin effect, resulting in increased power loss in the wire. Solid wire commonly used and consider the basic to all other wires or cables.
- 2. Litz wire:** is a special type of wire used in high frequency applications. The wire is designed to reduce the skin effect and proximity effect losses in conductors. It consists of many strand wires, individually coated with an insulating film and woven together, see fig. (2).
- 3. Twisted wire:** is also a special type of wire, like litz wire. It is clear from figure (3) transaction of strands, taking into account twisting strands only or the strands possess only angular transposition,

twisted wire different from litz wire in this point only.

2. Determination of the Resistance:

Figure (1) shows the equivalent circuit of a planar induction system defined by the values of $R_{T,L}$ which is defined as:

$$R_{T,L} = R_T + R_L \tag{1}$$

The ac resistance (R_T) of solid, litz and twisted wire consist of two components [3], the conduction and induction resistances.

$$R_T = R_c + R_{in} \tag{2}$$

Where R_c and R_{in} : conduction and induction resistance respectively.

In strands wire, the total field over a strand in a particular turn has two components: the field created by the another turns of the winding and the field created by the neighboring strands in the same turn. Therefore R_{in} will be [4]:

$$R_{in} = R_i + R_e \tag{3}$$

Therefore, the ac resistance of litz wire represent by three components: the resistance due to the skin effect which called conduction resistance " R_c ", the resistance due to the proximity effect of external fields which called external induction resistance " R_e " and the resistance due to the proximity effect of individual strands in the bundle on each other which called internal induction resistance " R_i ", i.e.:

$$R_T = R_c + R_i + R_e \tag{4}$$

As the solid wire does not have individual strands. Therefore, the ac resistance of solid wire is:

$$R_T = R_c + R_e \tag{5}$$

This is applied to ac resistance of twisted wire also; it is because the twisted wire can be considered as equivalent solid wire [3]. The ac resistance of twisted wire will be:

$$R_T = R_{ct} + R_{et} \tag{6}$$

3. Mathematical Formulation of the Resistances :

3.1. Analysis and Modeling of Litz-Wire Winding Resistance:

a. Conduction Resistance:

The conduction resistance per unit length R_{c_ul} , of (n_s) strands litz wire is given by [3]:

$$R_{c_ul} = \frac{k}{2 \cdot \pi \cdot r_s \cdot \sigma \cdot n_s} * \Phi_c(kr_s) \tag{7}$$

Where:

$$\Phi_c(kr_s) = \frac{ber_{(kr_s)} * bei'_{(kr_s)} - bet_{(kr_s)} * ber'_{(kr_s)}}{ber^2_{(kr_s)} + bet^2_{(kr_s)}} \tag{8}$$

$$k = \sqrt{\mu \omega \sigma} = \frac{\sqrt{2}}{\delta} \tag{9}$$

Where ber , bei , ber' , and bei' are Kelvin functions [5] and r_s the radius of strand, δ is the skin depth [6].

$$\delta = \sqrt{\frac{2}{\mu \omega \sigma}} \tag{10}$$

Where

σ : conductivity ($m\Omega$)⁻¹
 μ : permeability of the object
 ω : angular frequency of the current flowing through the object.

r_s : radius of strand.

b. Internal Induction Resistance:

Take a litz wire of (r_b) bundle radius, the resistance due to internal induction per unit length [3]:

$$R_{i_ul} = - \frac{n_s \cdot k \cdot r_s}{3 \cdot \pi \cdot r_b^2 \cdot \sigma} \Phi_{in}(kr_s) \tag{11}$$

$$\Phi_{in}(kr_s) = \frac{ber_2(kr_s) * ber'(kr_s) + bei_2(kr_s) * bei'(kr_s)}{ber^2(kr_s) + bei^2(kr_s)} \tag{12}$$

Pointing that $\Phi_{in}(kr_s) \neq \Phi_c(kr_s)$ where $\Phi_c(kr_s)$ is defined in equation (8). ber_2 and bei_2 are the second order of Kelvin functions [5].

c. External Induction Resistance:

The effect of the magnetic field of each turn (created by the rest of the turns) at other i -turns, see figure (4), can be calculated by different ways, numerically using a finite element analysis, or analytically.

This field may change by three different reasons: first, the presence of the load; second, the proximity of the neighboring turns; and third, depending on the conduction area of

the bundle and the packaging factor of litz wire.

$$\text{Packaging factor} = G = \frac{n_s r_s^2}{r_b^2} \dots(13)$$

Let a strand in the i -turn of the planar inductor as it is shown in Figure (5). The external field applied to each strand will be [7]:

$$H_{o,i} = H_{or,i} a_r + H_{oz,i} a_z$$

The external field in each turn is caused by the total current I in the inductor, and then we can associate these losses with a resistance. Let $H_{o,i}$ the magnetic field generated over the i -turn of the winding when a current amplitude of 1 A is circulating in the inductor. And can rewrite the average of the squared field as:

$$\langle H_{o,i}^2 \rangle = \langle \mathcal{H}_{o,i}^2 \rangle * I^2 \tag{15}$$

The external induction resistance per unit length [3] is:

$$R_{e_ul} = - n_s \frac{2\pi k r_s \langle \mathcal{H}_{o,i}^2 \rangle}{\sigma} \Phi_{in}(kr_s) \tag{16}$$

Total Resistance Calculation:

According to (4), (7), (11), and (16), and considering the length of the whole winding, we can calculate the total resistance as follows:

$$R_c = \frac{k \Phi_c(kr_s)}{2\pi r_s \sigma n_s} * \sum_{i=1}^n 2\pi u_i \tag{17}$$

$$R_i = - n_s \frac{k r_s \Phi_{in}(kr_s)}{3 \pi r_b^2 \sigma} * \sum_{i=1}^n 2\pi u_i \tag{18}$$

$$R_e = -n_s \frac{2\pi k r_s \Phi_{in}(i)}{\sigma} \sum_{i=1}^n [2\pi u_i * \langle J_l \rangle] \quad (19)$$

$$R_T = R_C + R_I + R_e \quad (20)$$

3.2. Analysis and Modeling of Twisted-Wire Winding Resistance :

Let r_b the radius of twisted wire containing n_s strand, each one of them having a radius r_s ,

The radius of the equivalent solid wire r_e (see figure (6)) is defined by:

$$r_e = \sqrt{n_s r_s^2 G} \quad (21)$$

Where G is the packing factor of wire given by eq. (13)

For bundle, the conduction resistance per unit length is:

$$R_{ct_ul} = \frac{\Phi_c(Qr_s) \Phi_c(Qr_s) k^2 G r_s}{8\pi \sigma r_e} \quad (26)$$

The factor $\Phi_c(Qr_s)$ takes into account the skin effect at bundle level and the factor $\Phi_c(Qr_s)$ accounts for skin effect at strands level.

b. External Induction Resistance of Twisted Wire:

a. Conduction Resistance of Twisted Wire:

The conduction resistance per unit length of the strand is [3]:

$$R_{cs} = \frac{k}{2\pi r_s \sigma} * \Phi_c(kr_s) \quad (22)$$

For the complete bundle of twisted wire, the currents were not equally distributed in every strand, as it occurs in true litz wire. Therefore, at equivalent solid wire, the current density at the coordinate r is given by [4]:

$$J_\phi(r) = \frac{Q \cdot I \cdot J_0(Qr)}{2\pi \cdot J_1(Qr) \cdot r_e} \quad (23)$$

Where I is the amplitude of the driven current and J_0 and J_1 are Bessel functions.

Q is a parameter related with the skin depth which defined as:

$$Q = k e^{J \frac{3\pi}{4}} \quad (24)$$

$$k = |Q| = \sqrt{\mu \sigma \omega} = \frac{\sqrt{2}}{\delta} \quad (25)$$

Twisted wire can be considered as an equivalent solid wire. Therefore, the internal induction resistance is negligent, and the external induction resistance only can be taken into account as an induction losses. The induction losses represents the power dissipation in a wire under a varying magnetic field, H_{o_i} , which created by the rest of i -turn. The induction losses are:

$$P_{is_ul} = \frac{-2\pi k r_s H_o^2 i \Phi_{in}(Qr_s)}{\sigma} \quad (27)$$

The $H_{o,i}$ is calculated analytically and the current density in equivalent solid wire is [3]:

$$J_{\theta(r,\theta)} = \frac{2 k H_D * J_1(Qr)}{J_0(Qr_0)} \sin(\theta) \quad (28)$$

The total induced losses will be the sum of the losses in each differential of area:

$$P_{st,i} = \frac{G \pi^2 k r_b (H_{o,i}^2)}{4\sqrt{2} r_s \sigma} \Phi_{in(Qr_s)}$$

At eq. (29), the average of $H_{o,i}$ are magnetic field applied due to the total current in the inductor. Let $\mathcal{H}_{o,i}$ magnetic field generated over the i -turn of the winding, when a current amplitude of 1A is circulating in the inductor as in equation (18).

The external induction resistance of whole inductor is:

$$R_{st_o} = \frac{G \pi^2 k r_b}{4\sqrt{2} r_s \sigma} \Phi_{in(Qr_s)} * \sum_{i=1}^n [2 n_s u_i (\mathcal{H}_{o,i}^2)] \quad (30)$$

a. Total Resistance of Twisted Wire:

The total resistance for whole winding from equations (6), (26) and (30) will be:

$$R_{st} = \frac{\Phi_c(Qr_s) \Phi_c(Qr_b) k^2 G r_s}{8\pi \sigma r_s} \sum_{i=1}^n 2\pi u_i \quad (31)$$

$$R_{st} = n_s \frac{G \pi^2 k r_b}{4\sqrt{2} r_s \sigma} \Phi_{in(Qr_s)} * \sum_{i=1}^n [2 n_s u_i (\mathcal{H}_{o,i}^2)] \quad (32)$$

$$R_T = R_{ct} + R_{et} \quad (33)$$

3.3. Analysis and Modeling of load resistance:

Assuming the electric field E_{θ} is linearity with n turns [7], the total voltage amplitude induced at the winding position $z = -d$ is the sum of the voltage induced in each turn, and it is calculated as follows:

$$v = \oint E_{\theta} dl = - \sum_{j=1}^n \int_0^{2\pi} E_{\theta}(r = r_j, z = -d) u_j d\theta \quad (34)$$

Therefore, the equivalent impedance is:

$$Z = \frac{v}{I} \quad (35)$$

The resistance of load will be the real part of impedance:

$$R_L = \text{real}(Z) \quad (36)$$

4. Computer Results and discussions:

MATHECAD V.14 was applied, which it possess the ability to solve Kelvin function and integral of Bessel function, to perform computer program. This program is prepared to calculate losses and efficiency of induction cooker and to compare among wire types too.

To check the validity of the proposed equations [3], The results are compared with published work [8] which it alone deals with three type of wire in this subject and other published work deals with one type of

wires separately. Very good correlation was obtained as shown in Fig. (7).

Coils of different number of turns have been considered in table (1). The specifications of wires are shown in table (2) these values taking from [9,10]. In this table, we are taking into account the same conduction area "ac = 3 mm²" or across section of copper base for the comparison between three types of wire (solid, litz and twisted wire), and the load properties are shown in table (3). Figs. (8 - 10) show the results of a 25 turns unloaded practical coil. Fig. (8) shows conduction resistance against frequency according to eq. (17) and eq. (31), fig. (9) shows internal induction resistance against frequency according to eq. (18), which only occur in litz wire. This is due to the angular and transpose of strands in litz wire, which making distribution of magnetic field in bundle level is equally.

Fig. (10) shows external induction resistance against frequency according to eq. (19) and eq. (32). At coil level, the external induction resistance R_e increase when number of turn increase as expected.

The total resistance R_T of litz wire ($R_c+R_i+R_e$), solid wire (R_c+R_e) and twisted wire ($R_{ct} +R_{et}$) shown in fig. (11).

The distance d between load (vessel) and the coil is limited by thickness of ceramic and radius of the wire. To avoid low efficiency, the practical value of d does not exceed 10 mm. varying the thickness of ceramic to this value does not affect the total resistance, see figure (12). Thickness of ceramic, in the calculation, is taken to be 5 mm, as a middle value.

The effects of the load are shown in figs. (13 - 15) for magnetic load, fig. (13) shows external induction resistance. At high frequency, the external induction resistance with load is less than the external induction resistance without load, this is clearly shown when compared figure (10) with figure (13).

The efficiency of induction cooker system shown in figure (16), that it when cooker coil loaded by magnetic load. The efficiency is calculated from:

$$\eta (\%) = \frac{R_L * 100}{R_{T,L}}$$

It is known that the different contributions of each kind of load being higher in the case of magnetic load one as expected see figure (17). This attribute to properties of load (Relative magnetic permeability μ_r and resistivity ρ_l) . Due to the difference of total resistance R_T of coil, loaded by magnetic or nonmagnetic load, is very small (proximity similar) the total resistance R_T in figure (14) can be considered as total resistance R_T of coil loaded by nonmagnetic load. Also the total resistance with load resistance $R_{T,L}$ is shown in figure (18). In addition, the efficiency of cooker coil loaded by nonmagnetic load shown in figure (19) which clearly shown the difference among wire types.

VI. Conclusions :

First, an extensive review of induction cooker was covered. The characteristics of the induction cookers, their benefits in compared with other types of cookers and types of wire, use in induction cooker coil, were presented too.

The loss mechanisms due to the skin and proximity effects on a single and multi strands were derived. This by used an analytical model to

calculate resistance in different wire planar windings for induction heating cooker. The resistance has been separated into two parts: conduction resistance and induction resistance (with internal and external components for litz wire). In order to compute the induction resistance, a calculation of the magnetic field in the inductor is required. In addition to the comparison of result with other work, discussion the obtained results and the used of resistance curves are presented.

In general, we can consider the twisted wire the best when compared with other wires for whole frequencies, this appear in efficiency cases in figures (16) and (19). Moreover, litz wire has all right efficiency but in limited frequencies, as appear in the same figures (16) and (19).

MATHECAD v.14 proved to be suitable, efficient and accurate in solving and calculating the complex equations of resistance.

References:

- [1] Moreland, W.C.: "The induction range: its performance and its development problems" , IEEE Trans. ,Vol. IA-9 , No. 1 , 1973 , pp 81 – 85 .
- [2] Al-Shaikhli , A.K.M. : " Application of induction heating in cooking", the 1st regional conference of Engineering Science, Nahrain University, college of Engineering, Baghdad - Iraq, 5-6 Nov. , 2008.
- [3] Hassan A. Al-Ssady " Analysis of Induction Cooker Using Planar Coil " MSC thesis, Electrical and Electronic department, university of technology, Baghdad - Iraq, Sep. , 2009.
- [4] Garcia , J.R. et al : "A method for calculating the workpiece power dissipation in induction heating processes" , Proc. of Applied Power Electronics Conf. and Exposition , 9th annual conf. , APEC' 94 , Vol. 1 , 13 – 17 Feb. 1994 , pp 302 – 307 .
- [5] Mclachlan, N. W.; "Bessel function for Engineers" ; Oxford: At the clarendon Press, 2nd ed., 1955.
- [6] Davies , J. and Simpson , P. : "Induction heating handbook" , McGraw – Hill , Maidenhead , U.K. , 1979 .
- [7] Hurley , W.G. and Duffy , M.C. : "Calculation of self and mutual impedances in planar magnetic structures" , IEEE Trans. , Mag. , Vol 31 , No. 4 , 1995 , pp 2416 – 2422 .
- [8] J. Acero, R. Alonso, J.M. Burdío, L.A. Barragán, and C. Carretero, "A model of losses in twisted-multistranded wires for planar windings used in domestic induction heating appliances", in *Proc. IEEE Appl. Power Electron. Conf. (APEC)*, 2007, pp. 1247-1253.
- [9] Technologic information of litz wire (<http://www.litz-wire.com>).
- [10] Technologic information of twisted wire (<http://www.hmwire.com>).

Table (1) shows the dimension of turns.

	Radius of internal turn u_i	Radius of external turn u_f
25-turns (mm)	25	109

Table (2) show the number and radius of strands, bundle, equivalent also include packing factor of each wire.

Load	$\rho_L (m\Omega)$	μ_{rL}
Magnetic material	$1.25 \cdot 10^{-7}$	150
Nonmagnetic material	$0.33 \cdot 10^{-7}$	1

Table (3) load properties

Wire type	Packing factor	Number of strand	Conduction area	Radius of strand	Radius of bundle
	p	n_s	$ac (mm^2)$	$r_s (mm)$	$r_b (mm)$
solid	1	1	3	0.980	0.980
litz	0.6	20	3	0.220	1.270
		50	3	0.140	1.270
twisted	0.25	1000	3	0.030	1.897
	0.2	2000	3	0.022	2.200

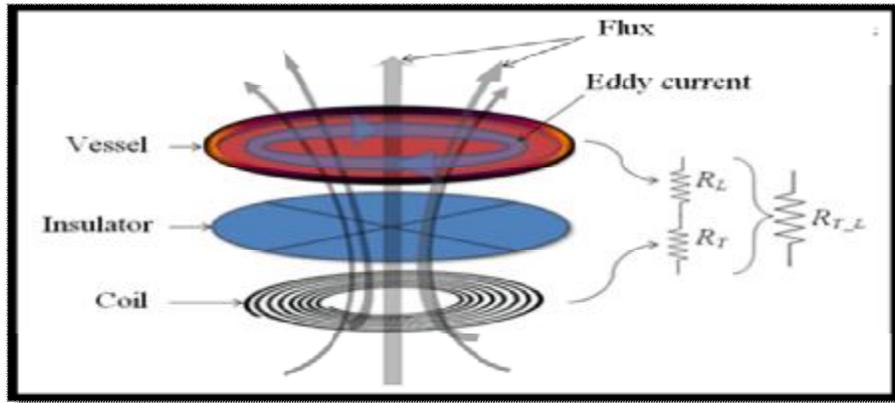


Figure (1) Elements of induction cooker. The flux and eddy current also shown.

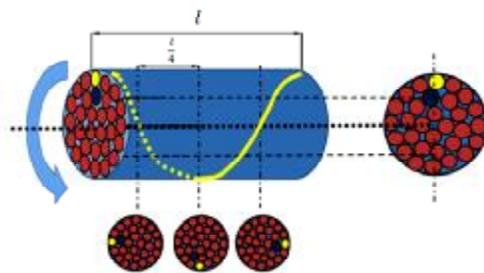


Figure (3) twisted wire structure.

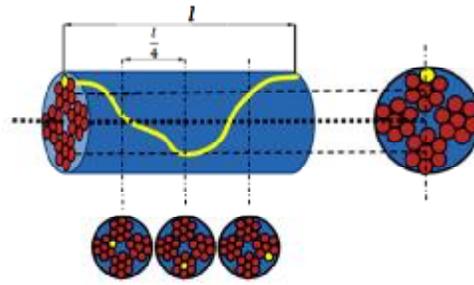


Figure (2) litz wire structure.

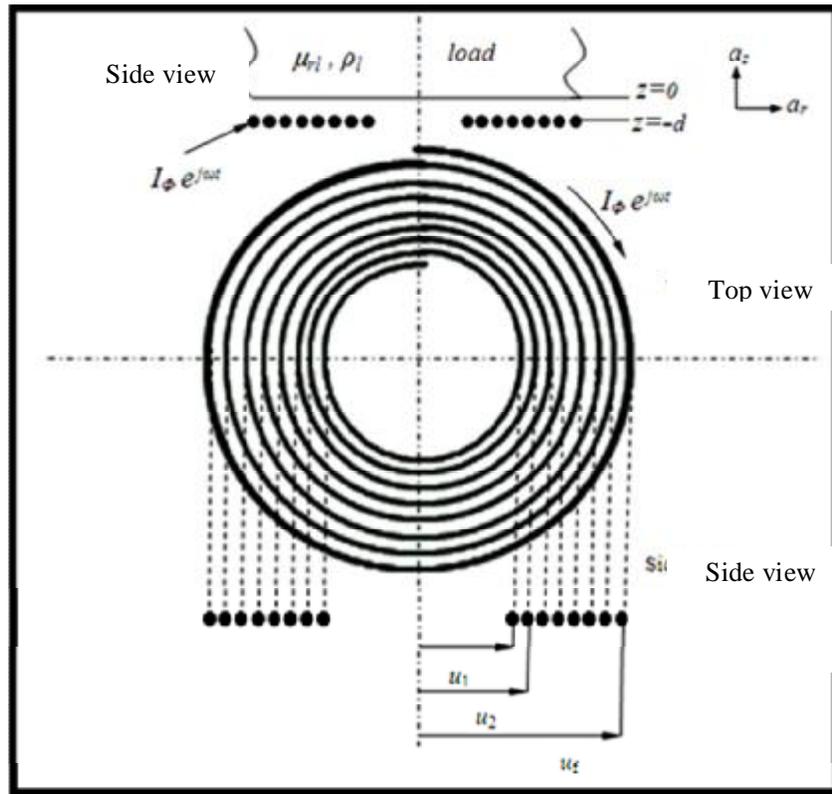


Figure (4) Planar inductor of n turns loaded by a medium characterized by its Conductivity σ_l and relative permeability μ_{rl} . The coordinate system is also shown.

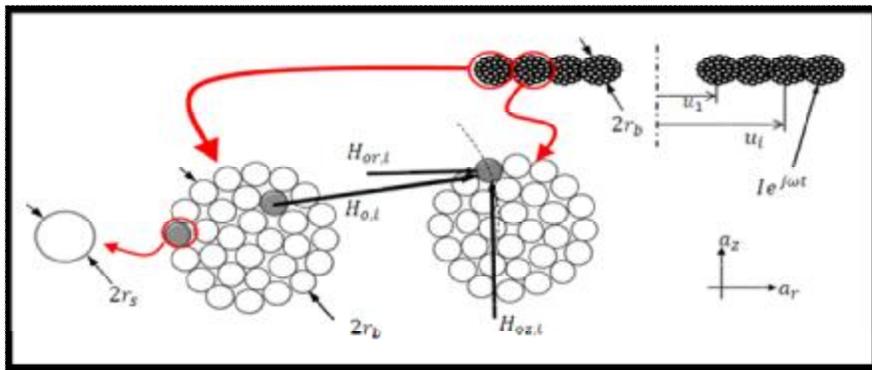


Figure (5) External magnetic field $H_{or,i}$, $H_{oz,i}$ in a strand situated in the i -turn.

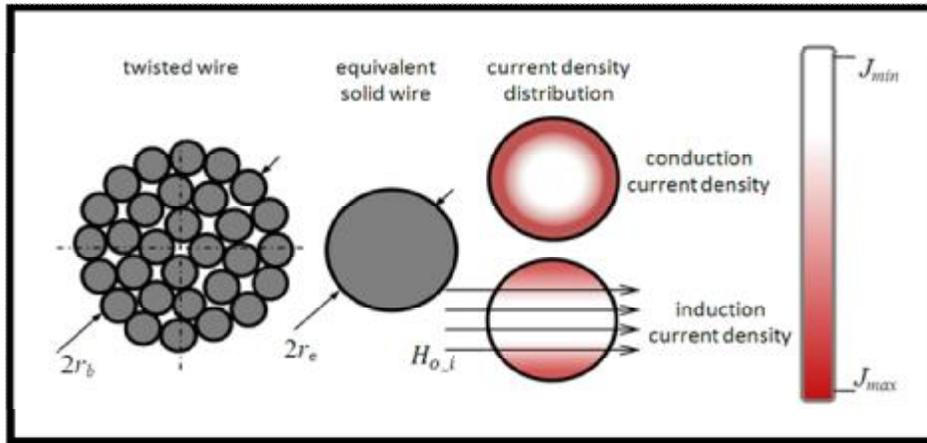


Figure (6) Equivalent solid wire of twisted wires as a function of its packing factor. The external magnetic field and distribution of the induced currents produced by the equivalent solid wires is also shown.

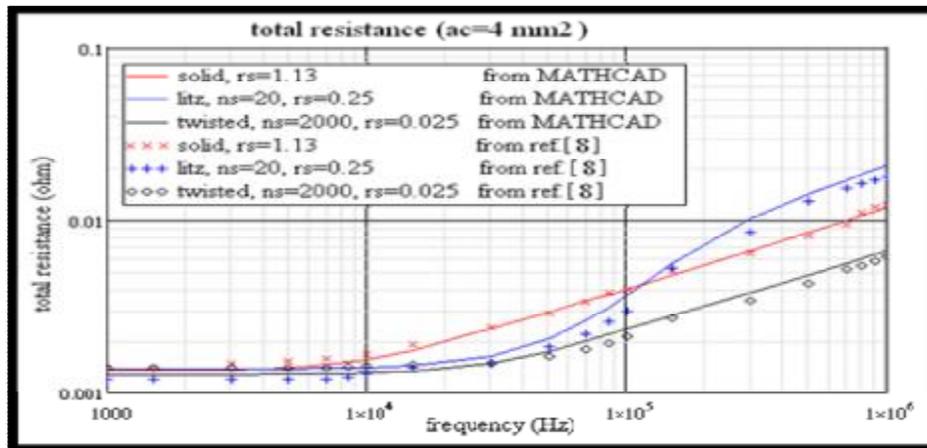


Figure (7) comparison between MATHCAD results and results of reference [8].

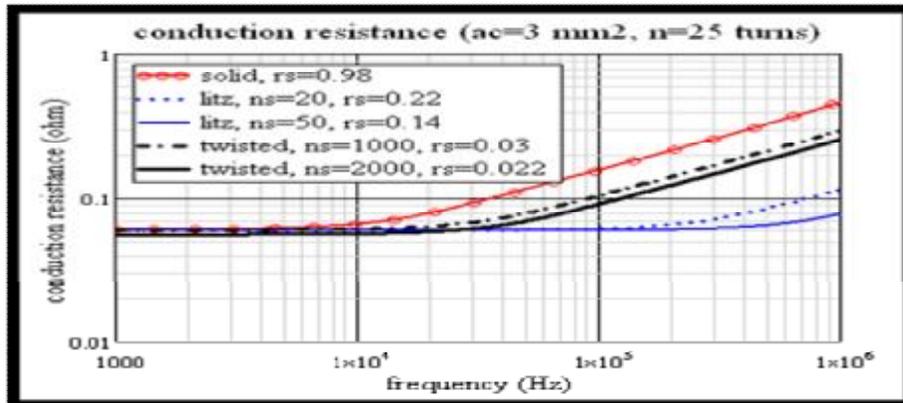


Figure (8) variation of conduction resistance R_c of 25-turn with frequency, $ac=3\text{mm}^2$.

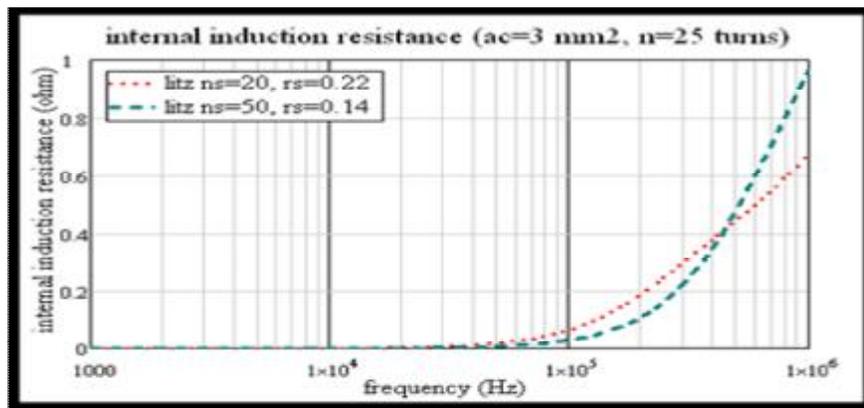


Figure (9) variation of internal induction resistance R_i of 25-turn with frequency, $ac=3\text{mm}^2$.

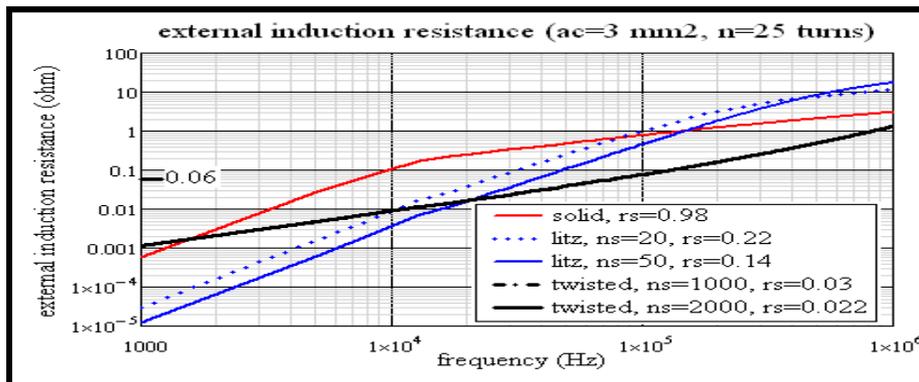


Figure (10) variation of external induction resistance R_e of 25-turn with frequency, $ac=3\text{mm}^2$.

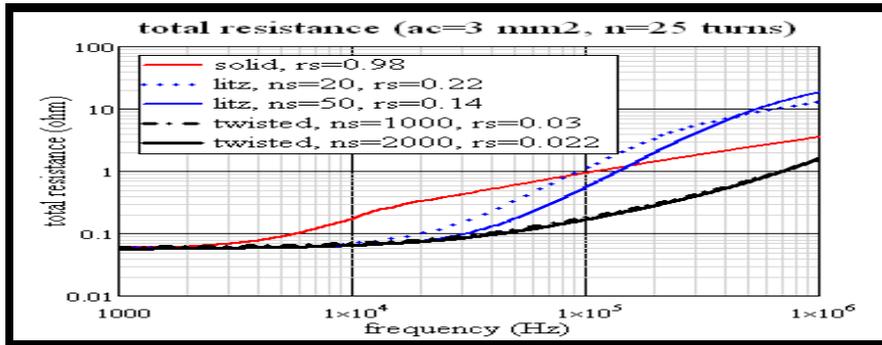


Figure (11) variation of total resistance R_T of 25-turn with frequency without load, $ac=3\text{mm}^2$.

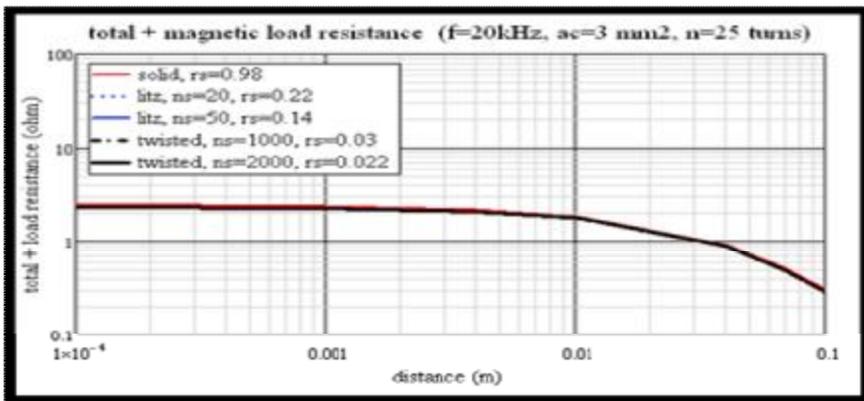


Figure (12) the resistance against distance between load and coil.

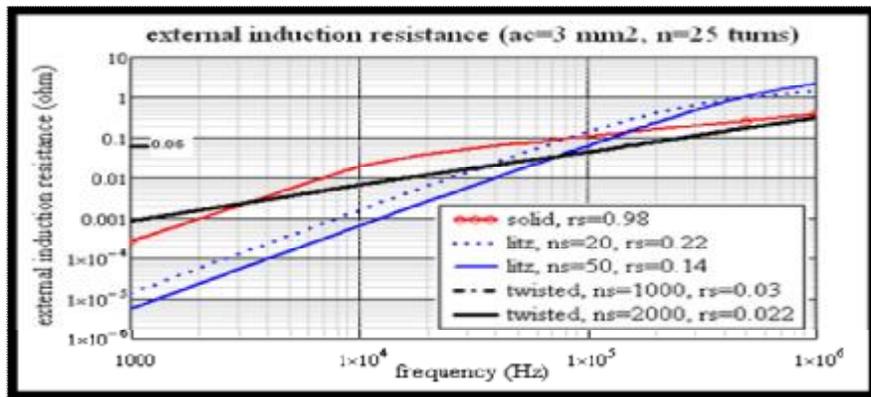


Figure (13) variation of external induction resistance R_e of 25-turn with frequency, $ac=3\text{mm}^2$ loaded coil by magnetic load.

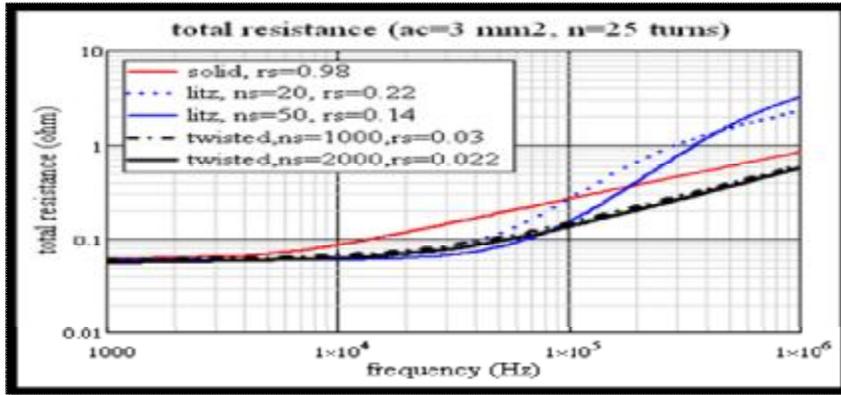


Figure (14) variation of conduction resistance R_c of 25-turn with frequency, when the coil loaded by magnetic load $ac=3\text{mm}^2$.

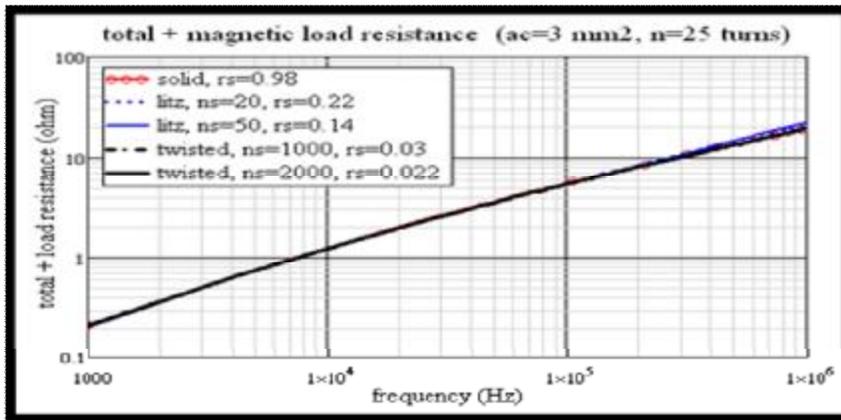


Figure (15) variation of (total+load) resistance R_{TL} of 25-turn with frequency, when the coil loaded by magnetic load, $ac=3\text{mm}^2$.

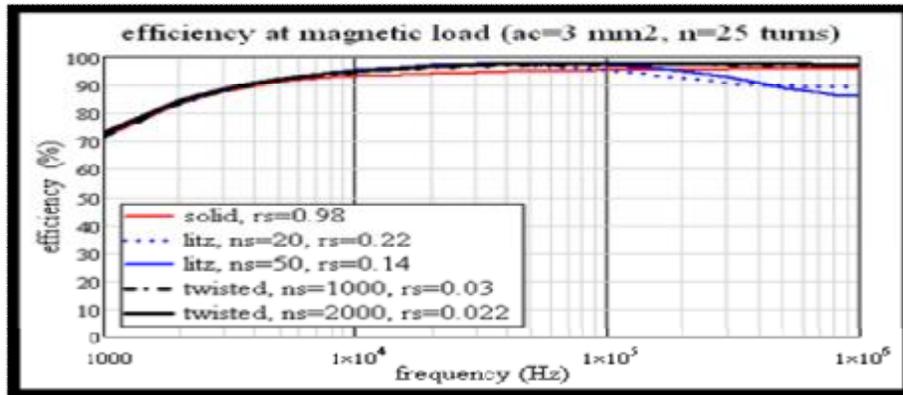


Figure (16) efficiency of induction cooker system when the coil loaded by magnetic load, 25-turn, $ac=3\text{mm}^2$.

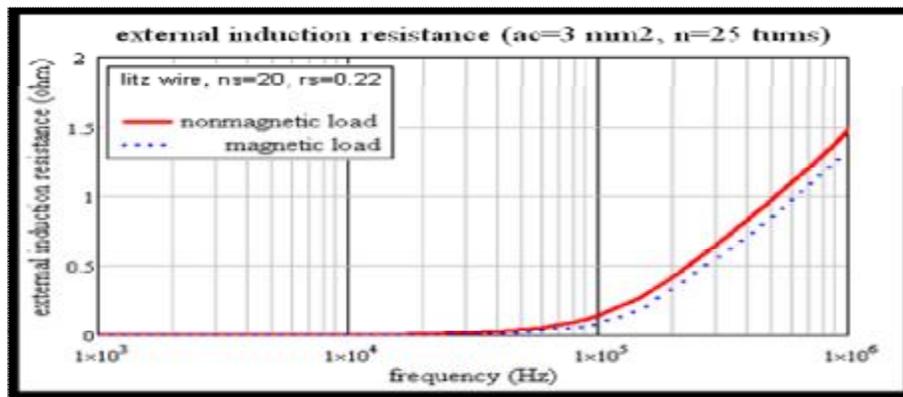


Figure (17) Comparison of external induction resistance R_c between magnetic (points) and non-magnetic (red line) load for coil has 25-turns by used litz wire $n_s=20$, $r_s=0.22\text{mm}$, $ac=3\text{mm}^2$.

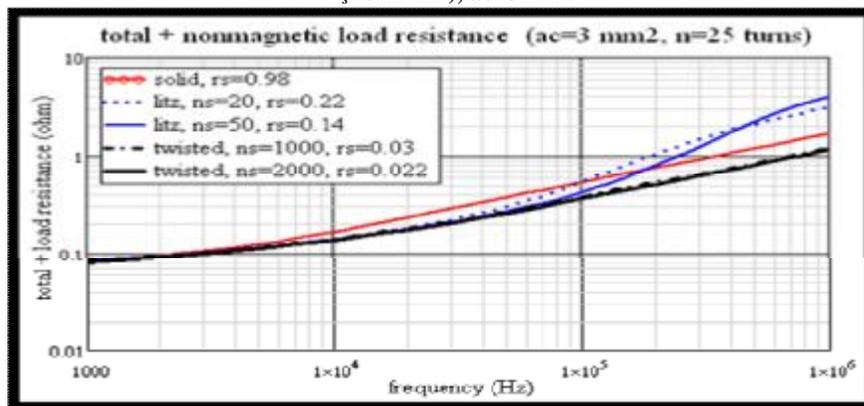


Figure (18) variation of (total+load) resistance $R_{T,L}$ of 25-turn with frequency. when the coil loaded by non-magnetic load, $ac=3\text{mm}^2$.

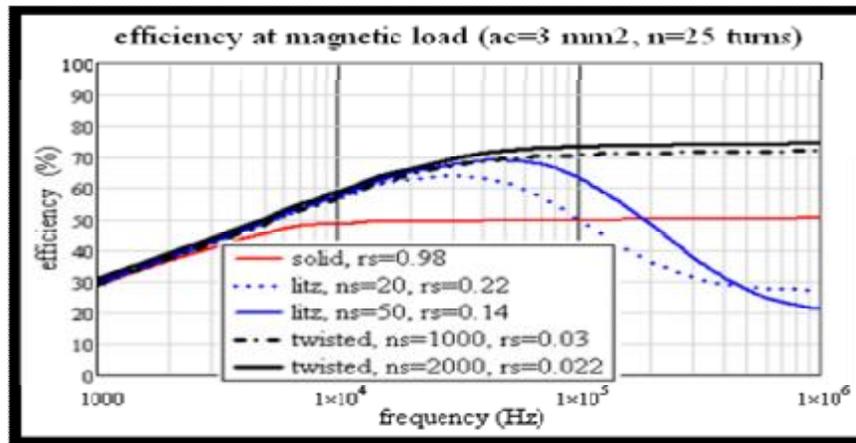


Figure (19) efficiency of induction cooker system when the coil loaded by non-magnetic load, 25-turn, ac=3mm².