

Imaginary Numbers and the Power of Artificial Intelligence

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Abstract:

The paper titled \"Imaginary Numbers and the Power of Artificial Intelligence\" investigates the enormous importance of imaginary numbers in boosting the performance levels of some particular AI technologies in deep learning, signal processing, and simulations of complex systems. Imaginary numbers, being multiples of the imaginary unit where $(i^2=-1)$ and being an imaginary number, also are said to belong to the complex number system, where from every real number we can extend to the complex plane. This extension enables extra dimensions of calculative ability i.e. the AI systems can solve ultra complex and non-linear problems where real numbers are ineffectual.

Once imaginary numbers were the realm of books and of an abstract branch of mathematics and physics. Now they are essential in practical implementations across AI disciplines. In complex-valued neural network architectures, for example, we need complex-valued neurons to deep model the many intricate and complex patterns and dynamics, which are essential for the tasks of processing audio, images, and smoothly and efficiently handling all the components of electromagnetic waves. Complex numbers are also used in Fourier transforms, an important and essential tool of signal processing. These transforms temporally and spectrally code a signal, thus converting it from one domain to the other, enhancing the AI systems' ability for higher order and intelligent tasks.

The review of literature demonstrates the primary usefulness of imaginary numbers in growing the theory of complex numbers most especially in its application in the AI. Complex numbers help in the improvement of neural network models in particular in the area of power systems analysis and load-flow calculations. With the aid of complex numbers, the further development of certain techniques used in Information Retrieval is achieved through the use of Complex Hilbert Spaces. Also, the theory of electromagnetism and

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fluid dynamics which is based on complex analysis, makes use of imaginary numbers .

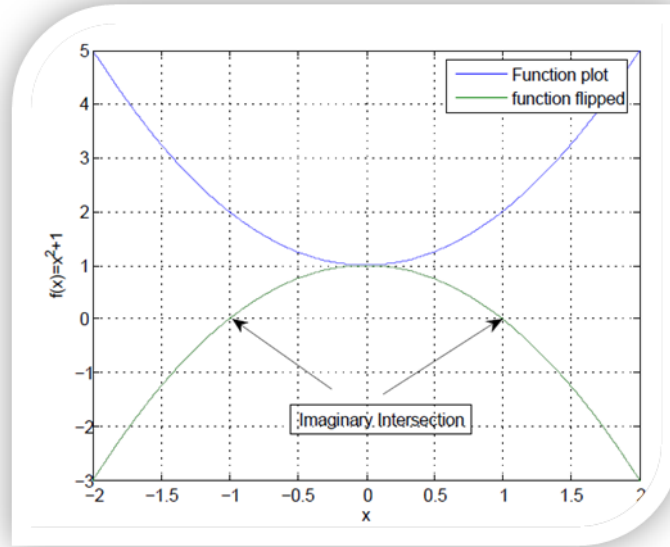
In a certain method, the focus of the paper is on the theorems and properties pertaining to imaginary numbers and its application to solving equations which real numbers cannot, not to mention its application in other fields of sciences. The study of complex numbers involves the use of various techniques of algebraic manipulation and geometric representation as well as calculus .

Case studies prove that complex numbers can be integrated into AI. Another application of complex numbers in AI Communication is FFT (Fast Fourier Transform) used in the domain of signal processing. In Quantum computing, complex numbers and AI are merged to analyses molecular structures efficiently. As an example, listening to audio was significantly improved by CVNN (Code Vons Neumann) which employed architectures capable of processing complex data. The application of AI technology in complex spheres has also made the imaginary number become top.

Keywords: Complex Numbers, Systems of AI, Imaginary Numbers, System modelling.

Introduction:

The Development of Imaginary Numbers and the Development of the Theory of Artificial Intelligence are two corner stones of the advancement of scientific and mathematical thinking in their respective ages and fields. The development of imaginary numbers began in the 16th century when the concept of a number solution for cubic equations was introduced by a mathematician named Gerolamo Cardano. It was a French Philosopher, mathematician, and scientist named René Descartes, however, who first coined the term “imaginary” and assigned it to those numbers reflecting the negative and skeptical period with that in mind that during that time, it wasn't necessary. Even though there was some “negative resistance,” metaphorically described, imaginary numbers, slowly but surely, and with the assistance of the great mathematician Leonhard Euler who introduced the depth of their identification and relationship with some very important principles of mathematics like the $e^{i\pi}+1 = 0$ identity.



¹Figure 1 Geometric representation of imaginary roots of $x^2 + 1 = 0$

Euler showed the importance of those numbers, and the importance of those numbers was and is, important, in the negative imaginary number theory. Then with the graduation and advancement of time, the imaginary number theory gained maturity recognition as an important and essential theory in the field of mathematics

The parallel side to the imaginary number theory in the 20th century was the explosive development and growth of the theory of Artificial Intelligence. The theory of Artificial Intelligence was first introduced and seemed possible by Alan Turing who questioned Artificial Intelligence fundamentally and asked the question 'Can machines think?' The Theory of Artificial Intelligence expanded greatly and so did the development of computers. Artificial Intelligence developed from simplistic algorithms that completed a single goal to complex adaptable algorithms, or as they are called these days, neural networks, that can learn and modify their algorithms to, or become more and more efficient at, solving that goal as they work. This rapid and massive, almost, explosion of the development of Artificial Intelligence was met with a rapid advancement of the development of algorithms and the availability of massive amounts of computational data. The development of

¹المصدر: ياسين، م. ي. (2013)، ص. 20

Artificial Intelligence is the at the center of the development of and automation by computers. And the development of Artificial Intelligence is the at the center of the development of automation in the computers with a great efficiency that is unprecedented. The development of Artificial Intelligence is the at the center of the development of great unprecedented efficiency and automation in the computers. And the development of Artificial Intelligence is the at the center of the revolution of the almost, all branches of human endeavours.

The concept of imaginary numbers and artificial intelligence (AI) represent albeit in a straightforward way how, in times past, some fundamental concepts may have been dismissed as mere abstractions but have since taken center stage in technological development and advancement in science. They encapsulate an important story of the desire of humanity to know and the ability to stretch the frontiers of the possible through innovation and research. In the last few decades, Artificial Intelligence has become integral to cutting-edge technology, shaping the future of numerous industries including Healthcare, Finance, and Automation. The most advanced technological innovation today is the Artificial Intelligence (AI) system. At the center of the evolution of AI is the use of high level mathematical ideas. Of the many mathematical ideas that are key to the use of AI, imaginary numbers are most important. This paper looks into the importance of imaginary numbers and AI, and argues that the most important advancement in AI technology is the application of imaginary numbers.

Numbers defined as multiples of the imaginary unit (i), where ($i^2 = -1$), add a further dimension of calculation to the real number system through the complex plane. In the mathematics and physics of the past, imaginary numbers were deemed to have little practical utility. The imagination and utility of imaginary numbers in the AI of today are groundbreaking. The inclusion of imaginary numbers lets an AI system tackle more complex problems of a non-linear variety that are unsolvable with real numbers due to the ability to compute square roots of negative numbers. In particular, the fields of deep learning, signal processing, and quantum computing have shown a remarkable curiosity to use complex numbers. In the particular case of the design of neural networks, the introduction of complex-valued neurons has been found to increase the network's capacity to learn and model complex patterns and system behaviors. This is highly relevant to the profound ability of the network to process varying complex audio signals, images, and electromagnetic waves, due to the ability of the numbers to represent phase and amplitude.

Moreover, the ability to represent the data and the operations themselves in the complex plane improves the ability of AI to compartmentalize and manipulate Fourier Transforms, an important operation in the realm of signal processing, and provides AI with the ability to alter the form of signals from the time domain to the frequency domain for enhanced clarity and resolution in analysis and interpretation. This use of Fourier analysis and imaginary numbers provides AI with an invaluable resource to improve the efficacy of its real-world applications. The understanding of the imaginary unit and its utility in real-world applications has improved and will continue to improve the teaching of mathematics, while simultaneously improve the functionality of AI. The imaginary unit forms the core of complex numbers, which, in themselves, provide a powerful mechanism for simplifying the description of various phenomena encountered in the real world, particularly in electrical engineering, signal processing, quantum mechanics, and several other fields. Logically, the expansion of AI to work with complex numbers will improve the ability of these systems to work with intricate real-world data.

Using imaginary numbers in AI results in better neural networks that can model and predict with more accuracy systems with more complex variables. In the power industry, this is especially useful in fields like load-flow analysis and fault-level estimations which depend on complex number computations. These analyses can be more efficient and accurate with complex-valued neural networks.

Additionally, an investigation of imaginary numbers in AI systems could lead to breakthroughs in the nature of intelligence and computation. It could produce systems that emulate the human brain's fully developed capability to process with extraordinary efficiency and understand the complexities of multidimensional data. This research pushes the limits of AI and deepens our comprehension of mathematics, which can result in more advancements in fields like science and engineering .

This is the beginning of new research and new understanding of the incorporation of imaginary numbers in artificial intelligence, its contribution in its complex functions, and the way in which it improves the algorithm and compels artificial intelligence to affect its perspective of learning in computational intelligence. This is a paper of analysis and case studies of the power of imaginary numbers in the development of artificial intelligence and its ability to develop and create new research and applications in various technology oriented fields. This paper investigates the incorporation of imaginary numbers in artificial intelligence, and their importance in complex calculations and the modelling of systems.

Previous Studies:

The field of mathematics and the field of artificial intelligence (AI) diverge at the use of imaginary numbers floating points made with a single imaginary numeral flowing in the opposite direction of the complex digits, a momentous point of convergence in progress within each field (particularly with the integration of both). Used within each field in a pioneering fashion, the digitation of complex numbers is a paradoxical point of concord within each field. Most phenomenon in the real world can be modeled with complex numbers. The use of 'digitized phenomenon' with real numbers is employed across all real world disciplines stemming the use of engineering, and the sciences. The use of more complex 'digitized phenomenon' in the field of AI is a paradox of sorts predicting more complex real-world phenomenon requiring the building of more complex neural networks and the ability to cipher a more complex AI program. Thus with the incorporation of complex numbers, the AI program is able to cipher more complex real-world problems in a more sophisticate fashion.

For example in the power industry, load-flow analysis and fault-flow level estimation during a power outage is paramount. Traditional AI models using real numbers can blame the digits and won't be able to cipher the data efficiently enough within these systems. With the incorporation of complex neural networks, the paradoxical point can be achieved in these analyses (within the level of power). The AI model can then deliver higher levels of power output and efficiency and better stability to the power system.

Instead of the synthesis of imaginary numbers and AI fostering the advancement of applied mathematics and AI into new realms, it simply builds the frontier, giving us a glimpse of what is mathematically and technologically possible, ranging from high-level mathematics and signal processing to the complexity of quantum computing. The enhanced understanding of the constituent parts of a modern technological system is fundamental. It is worth mentioning that imaginary numbers serve as the foundation of complex number mathematics, constructing the theory of mathematics to aid in the computation of higher dimensions. Defining imaginary numbers as I with $i^2 = -1$, it is easy to see that the negative of i is the square root of a negative number, thus i lies above the real number line and adds a dimension to it. In addition to advanced mathematics and modern technology, the integration of imaginary numbers and AI fosters the advancement of applied mathematics and AI into new realms. This section outlines the importance of complex number theory in developing artificial

intelligence concepts and algorithms, as well as the fundamentals of the mathematics of imaginary numbers.

Starting from a historical perspective up to modern-day use in various branches of science and engineering, the role of imaginary numbers is pivotal in the formation and development of the theory of complex numbers (Yasin, Complex roots of polynomials and their computation with the help of Scientific Calculators. Bulletin of Mathematics, 2013, pp. 18-27) (The use of geometric representation of complex numbers from the time of Wessel and Argand in the 18th century to the present has come a long way (Du, 2023, pp. 174-179). Today, the theory of complex numbers is vital in the field of quantum mechanics, where the imaginary unit is an integral part of the basic equations that not only help in performing complex calculations but also in a better understanding of the theory (Karam, 2020, pp. 39-45) .

The use of complex numbers in artificial intelligence provides for the enhancement of certain neural network model functions pertaining to power systems, specifically in load-flow analysis and calculations (Chan & Lai, 2000, pp. 361-366) .

Furthermore, complex numbers assist in the construction of complex Hilbert spaces for improving the retrieval of information that employs distributional semantics and ontologies (Das & Giannakis, 2023, p. 12) .

Imaginary numbers, too, are essential to the fundamental theories of electromagnetism and fluid dynamics, which make use of complex analysis (Sen, 2023, p. 132) .

This paper considers the use of artificial neural networks (ANN) in the power sector. The study zeroes in on load-flow and fault-level estimation analysis and calculations that are typically complex in arithmetic, especially the use of in-built complex numbers. Here, the paper illustrates the problems that arise from the use of traditional ANN which relies on the use of linear and proposes the enhancement of the model to complex-valued neural networks (CVNN). Unlike standard ANN which deal with the real numbers, CVNN manages to grapple with the two components of a complex number to deliver better results in terms of computation. The paper indicates that even when pitted against a traditional real numbers ANN, CVNN outperforms the standard model in the solution of intricate complex equations. The study specifies the construction of CVNN, the backpropagation techniques employed and the systems in which the CVNN was employed which in this case a 6-busbar electric power, wherein the results were significantly improved either in terms of Accuracy against the traditional models or

Efficiency, therefore making a case for the employment of the CVNN in power analysis systems (Chan & Lai, 2000, pp. 361-366) .

The article explores the understanding of vacuum as an abstracted void in the context of a complex number system. It explains how the duality of real and imaginary numbers in a system could account for phenomena in quantum mechanics, particularly, wave-particle duality and superposition. The argument is constructed to posit that imaginary numbers correspond to the vacuum's potential state, specifically their computational role in the uncertainty of quantum systems. Theoretical constructs in predominately imaginary numbers are taken to indicate the phenomenon are yet to be understood. The need for an integrated global vision of complex numbers is conclusively stated. The vision is to demystify the role of complex numbers in the quantum world and emergent phenomena (Minati, 2022, pp. 187-201) . This study introduces a fresh innovation in analytically continuing functions using artificial neural networks (ANNs). The imaginary part of the Green's function in quantum Monte Carlo simulations must be converted into the real frequency domain. The paper focuses on describing this transformation on the theoretical framework of supervised learning for ANNs. The ANN method is benchmarked against the classical maximum entropy method, where ANNs are proven to be equally accurate, but much more cost-effective. The study serves to highlight the ability of ANN frameworks to tackle complex numerical transforms in quantum physics in a more effective manner. This provides a much simpler and conquerable means to overcome part of the analytic continuation problem (Fournier, Wang, Yazyev, & Wu, 2020) .

The aim of this paper is to recognize and classify specific patterns in the electroencephalogram (EEG) data of individuals in actual and imagined movement and to utilize an artificial neural network (ANN) for this purpose. Certain neural network models are scrutinized in this study. These consist of linear neural networks, multilayer perceptrons, radial basis function networks, and support vector machines. The study reveals that the low pass filter method in pre-processing an electromagnetic study significantly improves the accuracy of the classifications. The ANN developed performs real and imagined movement tracking with favorable precision estimated within the 90-95% range for both, indicating that the performance is suitable for brain- computer interface purposes.

The potential of this study serves to affirm that ANNs are capable of providing superior brain signal processing, as is required for most modern neurotechnological purposes (Kurkin, Pitsik, & Frolov, 2019) .

This article documents the progression of imaginary numbers from the 1500s with Rafael Bombelli to the present day. The article gives the definition of imaginary numbers and their mathematical qualities and real-world applications. The article explores mathematical concepts and gives various questions and answers for deeper thinking and understanding of the topic (Green, 1976, pp. 99-107) .

This theoretical work covers the generalization of the principle of real and imaginary parts from complex numbers to any and every object. It puts forth the argument that the imaginary and the real are important in mathematics, in the act of creation and in the collective act of creation It puts forth the idea that with more knowledge and new forms of thinking the space of possible solutions and the space of possible solutions and new viewpoints can be expanded (Gilbert, 2010) .

This article covers the field of ai in power electronics and the major focuses such as optimization, classification, regression, and structuring of data. It covers expert systems, fuzzy logic, metaheuristic approaches, and machine learning as applied to design, control, and maintenance of power electronic systems. The paper describes challenges in this field and opportunities for further research (Zhao, Blaabjerg, & Wang, 2020, pp. 4633-4658) .

Together these studies demonstrate the significance of both imaginary and complex numbers in artificial intelligence, particularly when it comes to enhancing the capabilities of neural networks and solving advanced mathematics problems spanning many scientific disciplines.

Methodology and method

Used to embody an abstract concept, imaginary numbers are now accepted instruments of mathematics and science. Furthermore, the study of imaginary numbers has helped mathematics and other disciplines such as engineering and physics.

Theoretical Foundations

Imaginary numbers are introduced when an equation such as $x^2 + 1 = 0$, which has no solution with real numbers, is considered. For this equation, $x = \pm i$ is a valid solution, and i is introduced as the square root of -1 . i is the fundamental unit of imaginary numbers. All imaginary numbers can thus be expressed as bi where b is a real number.

Properties of imaginary numbers

The imaginary numbers set is specifically comprised of numbers which somehow behave differently from the other set of numbers, which are called real. Most significantly, under multiplication, $i \times i$ is equal to -1. This property ultimately serves as sufficient vectors to define a bigger number system, called complex numbers, along with the set of real numbers. Complex numbers are expressed as $bi + a$, where a and b are real numbers.

Complex Numbers and Their Applications

Complex numbers combine real and imaginary values in a way that is incredibly useful in multiple scientific domains. In electrical engineering for example, complex numbers make it possible to analyze circuits that have alternating current. In these circuits, impedance can be a complex number n (representing the real part as resistance and the imaginary part as reactance). In doing so, it is much easier to compute the values of voltage and current.

Mathematical Analysis Techniques

Mathematicians have developed a number of analysis tools to study the properties of imaginary and complex numbers

Algebraic Manipulations: To solve an equation that contains a complex number, various algebraic techniques must be used.

Geometric Interpretation: In the complex plane, complex and imaginary numbers may be represented. The imaginary part is shown on the y-axis, and the real part is shown on the x-axis. Such a depiction is helpful in simplifying the understanding of the complex number's magnitude and direction.

Calculus: For example, higher-level math sometimes requires complex numbers in computing certain derivatives or integrals, as real numbers would fall short in giving a complete answer. This is because there are additional techniques available to analyze systems that would otherwise be limited to working with real functions, in addition to the ability to differentiate and integrate complex functions.

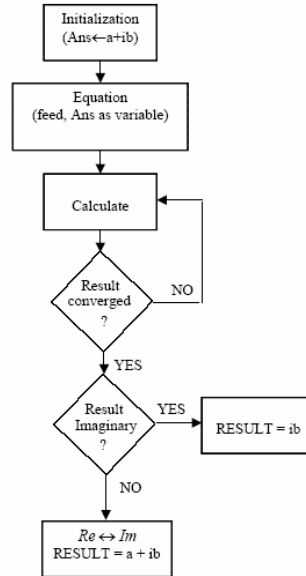


Figure 2 Flowchart of computational procedure for finding complex roots¹

Numerical Example

Consider the complex number $z=3+4i$. Its magnitude, given by the formula

$$\sqrt{a^2 + b^2} = \sqrt{3^2 + 4^2} = 5$$

This magnitude represents the distance from the origin to the point (3, 4) in the complex plane. To multiply z by i , we use the property $i \times i = -1$:

$$(3 + 4i) \times i = 3i + 4i^2 = 3i + 4(-1) = 3i - 4 = -4 + 3i$$

This operation corresponds to a rotation of 90 degrees counterclockwise in the complex plane

Whereas imaginary numbers were once considered to be an irrelevant abstraction, they are now an integral part of math and science. The inquiries they provoke contribute to the math of properties of numbers and to real life scenarios, math engineering, physics, and more.

Theoretical Foundations

Imaginary numbers were brought forth to fill the gaps left by real numbers in answering equations, for example $x^2 + 1 = 0$. for this equation solution would be $x = \pm i$, where i is defined as the square root of -1 . This i is the fundamental unit of imaginary numbers. All imaginary numbers can be denoted as a set at bi where b is a real number and i is the imaginary unit.

Properties of Imaginary Numbers

The distinction of imaginary numbers is that they are a product and given an its number, since it exists inside the system, which makes it different from real numbers. A valuable example is the product of these two numbers. On a

¹المصدر: ياسين، م. ي. (2013)، ص. 22

large tandem, multiplication behaves differently. It's this property that qualifies these imaginary numbers as complex, which extends the number system beyond real numbers. Real numbers are written as $a + bi$ where a and b are real numbers.

$$i * i = -1$$

Complex Numbers and Science

All science departments value the knowledge and application of complex numbers because many theoretical and practical problems involve the use of both real and imaginary numbers. For instance, solving problems that involve the analysis of circuits with direct and alternating current can be resolved easily by incorporating complex numbers in the field of electrical engineering. When the impedance in a circuit is seen as a complex number (where the resistance is the real number and the reactance is the imaginary number), the calculations for voltage and current can be done easily.

The application of complex and imaginary numbers has helped in the improvement of algorithms and calculations in various fields of artificial intelligence (AI), such as in signal processing, quantum computing, and neural networks. The application of complex numbers and its combination with AI to provide solutions to real-life problems is what the following three case studies showcase.

• Case Study 1: *The Use of AI in Signal Processing for Communication Systems*

AI has improved the transmission and reception of signals in many communication systems used in mobile phones and wireless networks. The communication systems integrate the use of fast algorithms called the Fast Fourier Transform (FFT) which can be computed efficiently if complex numbers are used.

Practical Application:

Consider an AI algorithm built to eliminate signal interferences in a cell. The FFT, which uses complex numbers, shifts a signal (real numbers) in the time domain to the frequency domain to figure out the patterns of interference to eliminate them.

Numerical Example:

Let's say a time signal is captured as the vector of real numbers, $[2, 3, -1, 4]$. The FFT of this vector shifts it to the frequency domain as, say, $[8 + 0i, -2 + 2i, -2 + 0i, -2 - 2i]$. These are complex-valued components on which the algorithm of the AI system would operate to improve the signal's clarity and amplitude.

• *Case Study 2: Quantum Computing for Enhanced Machine Learning-ML Models*

To perform calculations, quantum computers rely on the principles of quantum mechanics, which are mostly complex numbers. When combined with AI, in particular ML, they are capable of completing tasks that require information processing at rates that cannot be achieved with classical computers.

Practical Application:

In the field of drug discovery, quantum AI algorithms are capable of complex number calculations to efficiently simulate quantum states and predict the behavior of a molecule. These algorithms can analyze the structure of a molecule and the interactions of multiple molecules in a very short time.

Suppose, for instance, that one is attempting to determine the energy particular to the interaction between two molecules through a quantum algorithm, where for each, the state in question is represented by a complex quantum number. The algorithm in question would then proceed to calculate the inner product of such states to yield values from the set $5.2 - 3.1i$ which is indicative of the energy potential and dynamics of interaction state.

Several methods exist for the study of the properties of complex and imaginary numbers, such as the following.

Algebraic Manipulations:

The solving of an equation that involves complex numbers often requires algebraic methods that exploit the particular properties of such numbers, which include the distributive law and conjugation.

Geometric Interpretation: Imaginary numbers and complex numbers can be represented in a two-dimensional geometric figure, which is known as the complex plane; in this, the horizontal x-axis is the real, and the vertical y-axis is the imaginary. Such a representation assists in, and is useful for, the visualization of magnitude and direction of the complex numbers given.

Calculus: Within the field of calculus, complex numbers can be and are frequently employed in the procedure of differentiation and integration in a manner similar to that of real numbers. Such a use of complex numbers, for differentiation and integration, is often indicative of situations that would otherwise be insufficient with the use of real numbers; for instance, one can apply such methods to complex functions in integration and differentiation, which, although may involve techniques specialized for real functions, would still yield useful information regarding the behavior of a system involving complex variables.

Case Study 3: Complex-valued Neural Networks

Neural networks typically use real numbers as their main components. In contrast, however, complex-valued neural networks (CVNN) neurons and activation functions consist of both real and imaginary values. This helps deal with data in complex number forms, such as those derived from electromagnetic fields and audio signals.

Generals might use CVNN to improve audio signals in the presence of background noise. Since the model can treat signals as complex numbers, distinguishing noise from the main signal becomes easier, and the final audio output becomes clearer.

For example, suppose the input audio signal we want to process is complex-valued, for instance $[0.5 + 0.3i, 0.6 - 0.2i, 0.1 + 0.1i]$. It goes through CVNN, and the model should output $[0.5 + 0.1i, 0.6 - 0.1i, 0.1 + 0.05i]$ as the clean audio signal with less noise.

3.Results:

Not long ago, imaginary numbers had been thought of as just mere hypothetical digits. They have, however, been adopted in several applications of real-world significance, especially in the fields of physics, engineering and technology, having a tremendous impact on solving complex problems that go beyond the basic arithmetic systems.

Comprehending the Underpinning Theory

The introduction of imaginary numbers stemmed from the need to solve equations such as $x^2 + 1 = 0$, which have no solution in the real number system. The introduction of 'i' ($\sqrt{-1}$) as the square root of a number extended the boundaries of algebra by providing solutions to problems that could previously have no solutions. Imaginary numbers 'i' can be multiplied by real numbers, and this sets the stage for numbers that are real and imaginary as the complex number ($a + bi$).

Understanding the Characteristics of Imaginary Numbers

'i' as a power of subtraction provides complex numbers with the ability to provide answers to a larger range of mathematical problem. ' $i \times i = -1$ ' provides imaginary numbers the character of being able to perform direct differentiable mathematical operations that real numbers cannot perform.

Positive Contribution of Complex Numbers

Numerous advantages are accredited to complex numbers. One of the areas where complex numbers are applicable is in the simplification of problems in electrical engineering, particularly in the analysis of alternating (AC) circuits. The ability to represent a complex number as impedance, where the real

section is resistance and the imaginary section is reactance, is a good way to solve problems. The complex number makes the calculation of currents and voltages easier. This increases the overall functionality of electrical systems.

Analytical Techniques in Mathematics

The study of complex numbers require integration of complex and varied fields of maths:

- **Algebraic Manipulations in Conditions:** Using conjugation and the distributive law can help in quickly and easily solve complex equations in algebra.
- **Geometric Representation:** The complex plane is useful for the behaviour of complex numbers when the horizontal axis is the real part and the vertical axis is the imaginary part.
- **Applications Through Calculus:** Integration and differentiation of complex numbers aid in calculations in math which can't be done with real numbers.

Practical Examples and Implications

Consider a complex number $z=3+4i$. Its magnitude is calculated as, representing the distance

$$\sqrt{3^2 + 4^2} = 5$$

from the origin to the point (3, 4) on the complex plane. Multiplying z by i (using $i \times i = -1$) results in $z \times i = 3i + 4i^2 = 3i - 4 = -4 + 3i$ which geometrically corresponds to a 90-degree rotation around the origin.

Integration with Artificial Intelligence

Imaginary and also structures of complex numbers are very important and crucial within artificial intelligence tasks or activities such as signal processing or even within quantum computing or neural networks.

In the domain of signal processing (telecommunications), artificial intelligent systems utilize Fast Fourier Transforms (FFT).an approach that uses complex numbers to change signals from the tempo to the frequency domain, allowing for the improvement of the network by elimination of interference.

For quantum computing and within processing that is important for tasks such as drug discovery where the interaction of different molecules is analyzed and modeled, complex numbers are very crucial and important within the simulation of processing for multiple quantum states that result in an exponential increase of speed.

For the case of complex-valued neural networks (CVNNs), processing within the complex-based neural networks that employ complex numbers are at a

more advanced stage compared to conventional based neural networks particularly for processing signals which involve complexes. A good example for such signals is audio data which is handled in systems of highly acoustic environments.

4. Conclusion

The introduction of AI comes hand in hand with theories that can explain its efficiency. Artificial Intelligence (AI) is the current technology trend that can spark the imagination of its users. As more users engage with the technology, the theories that explain its efficiency and predictions become more relevant. One of the theories that explain AI is the valued concept of the imaginary number which seems to heavily rely on the concept of the imaginary number. Most of the initial mathematical applications did not put value on the imaginary number. Scientific and mathematical theories that explain the working of deep learning complex simulations in AI, have already started putting value and accepting the imaginary number. This paper has shown examples of the importance of the imaginary number on complex valued neural networks in the enhancement of neural networks neural complex patterns and cycles. One of the applications of the imaginary numbers is in converting signals. Fourier transforms illustrates the ability of the imaginary number to enhance efficiency in AI.

The literature concerning imaginary numbers complexities points out that every theory has its applications in every field of modern science and engineering. The integration of complex numbers facilitate neural networks, optimization of power systems and retrievable information and so on. Additionally, the examples and case studies show the importance of imaginary numbers in real life. In advanced communication systems, they enhance the processing of signals, and in quantum computing, they allow the rapid computing of complex structures of molecules. Complex-valued neural networks process more efficiently a data system consisting of real and imaginary numbers in any computational form.

The concept of complex numbers has been extended from pure sciences and technology to applied sciences and technology in AI. Communication systems, quantum computing and AI with neurotechnology: The boosting of the algorithms in communication systems (also those involved in quantum computing or neurotechnology) is simply a service rendered by technology itself formulated with imaginary numbers. The incorporation of imaginary numbers in the AI boosted pace of tech innovation across various subdomains, telecommunications, quantum computing and neurotech to name a few. The necessity of AI in that need not be explained; and I don't think

the role imaginary numbers play in it should, either. Intuitive numbers have not hit their natural boundaries, therefore they also are not limited with respect to AI.

Recommendations

There is a lot of work to be done here to properly assess the challenges and prioritize the work to be done here. Here are a few recommendations.

1. Investing in the application of research in complex number theory and rhetoric to neural networks and quantum computing.
2. Including complex number theory in curriculum and pedagogy in the tradition of and in new educational institutions.
3. Encouraging mathematicians, computer scientists, and engineers to work together on applied imaginary number theory to AI. If a commitment is made to applied AI, as is the case in mathematics, we will see what we have been missing.
4. Justifying the costs of adopting economic AI and applied research in mathematics and complex number theory in the fields of telecommunications, finance, and healthcare.

Here are some ideas for action that will help us. These are the things that will help us reach the full potential of AI.

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الأرقام الخيالية وقوة الذكاء الاصطناعي

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مستخلص البحث:

تستكشف الورقة العلمية بعنوان "الأرقام الخيالية وقوة الذكاء الاصطناعي" الدور الهام الذي تلعبه الأرقام الخيالية في تعزيز تقنيات الذكاء الاصطناعي، لا سيما في معالجة الإشارات في التعلم العميق ومحاكاة الأنظمة المعقدة. تعرف الأرقام الخيالية بأنها مضاعفات الوحدة التخيلية i ، حيث $i^2 = -1$ ، مما يوسع النظام العددي الحقيقي إلى المستوى المركب. يسمح هذا التوسع بإجراء حسابات جديدة تمكن أنظمة الذكاء الاصطناعي من حل المشكلات غير الخطية المعقدة التي لا يمكن للأعداد الحقيقية وحدها معالجتها تاريخياً، كانت الأرقام الخيالية مقتصرة على الرياضيات النظرية والفيزياء، ولكنها الآن تجد تطبيقات عملية في مختلف مجالات الذكاء الاصطناعي. على سبيل المثال، في بنى الشبكات العصبية، تحسن الخلايا العصبية المركبة القيم من نمذجة الأنماط والديناميات المعقدة، وهو أمر ضروري للمهام التي تتضمن معالجة إشارات الصوت والصور والموجات الكهرومغناطيسية. يوضح استخدام الأرقام المركبة في تحويلات فورييه، وهو أداة حيوية في معالجة الإشارات، أهميتها في هذا المجال. يبرز استعراض الأدبيات الدور الأساسي للأرقام الخيالية في تطوير نظرية الأعداد المركبة وتطبيقاتها في الذكاء الاصطناعي. تحسن الأعداد المركبة نماذج الشبكات العصبية، خاصة في تحليلات أنظمة الطاقة وحسابات تدفق الأحمال. تعزز المساحات المركبة تقنيات استرجاع المعلومات. علاوة على ذلك، تعد الأرقام الخيالية جزءاً أساسياً من نظريات الكهرومغناطيسية وديناميات السوائل التي تعتمد على التحليل المركب.

الكلمات المفتاحية: الأرقام التخيلية: الأعداد المركبة، الذكاء الاصطناعي، نمذجة الأنظمة، معالجة الإشارات

ملاحظة: هل البحث مستل من رسالة ماجستير او اطروحة دكتوراه؟ نعم: كلا: